



5<sup>th</sup> International Conference on  
X-ray and Neutron Phase Imaging with Gratings

# Tutorial Lectures

20 October, 2019  
Tohoku University, JAPAN



# Opening address

Since the first meeting in 2012 (Tokyo, Japan), XNPIG conferences were held worldwide almost every two years, and we are excited to meet again for XNPIG2019 in Sendai, Japan. The field relevant to XNPIG is growing steadily and young scientists, students, and new faces are joining the field of X-ray and neutron phase imaging and contributing to the development of this field.

This time at XNPIG2019, the international advisory committee (IAC) has organized a tutorial session for the first time prior to the main conference. Lectures on fundamentals and historical views of X-ray and neutron phase imaging, grating fabrication, and image processing are arranged. IAC aims at promoting and encouraging young scientists, students, and new faces with the lectures. Another merit of this trial must be that the presenters at the main part of XNPIG2019 can use time more for their specific subjects following brief introductions.

The number of registered attendees of the tutorial session is as much as 81 including 25 students at the time of writing, exceeding the estimation of the local organizing committee. Although we needed to find a larger room for the session in haste, it was a nice surprise.

I greatly appreciate our lecturers for their presentations and preparations for this handout in advance. Feedbacks from attendees about the organization and the contents of the session are welcome to LOC. I expect that this trial is effective and succeeded in the future XNPIGs. Finally I wish everybody enjoy XNPIG2019 and the stay in Sendai, Japan.

Prof. Atsushi Momose  
Chair of XNPIG2019

# **XNPIG2019 Tutorial Lectures**

**Sunday, 20 October 2019**

**(Auditorium at Bldg. 2, Institute for Material Research,  
Katahira Campus, Tohoku University)**

13:20 – 13:30 **Opening**

Atsushi Momose, *Tohoku University, Japan*

13:30 – 14:15 **Tutorial 1**

p.3

**Historical view of X-ray imaging especially using phase information**

Alessandro Olivo, *University College London, UK*

14:15 – 14:45 **Tutorial 2**

p.19

**Historical view of neutron radiography**

Dmitry A. Pushin, *University of Waterloo, Canada*

14:45 – 15:05

***Coffee Break***

15:05 – 15:50 **Tutorial 3**

p.33

**Introduction to phase imaging principles & potential applications**

Franz Pfeiffer, *Technische Universität München, Germany*

15:50 – 16:20 **Tutorial 4**

p.51

**Introduction to tomographic image reconstruction**

Marco Stampanoni, *Paul Scherrer Institut / Eidgenössische  
Technische Hochschule Zürich, Switzerland*

16:20 – 16:40

***Coffee Break***

16:40 – 17:10 **Tutorial 5**

p.65

**Fabrication technology of gratings**

Christian David, *Paul Scherrer Institut, Switzerland*

17:10 – 17:25 **Closing with expectation to XNPIG2019**

Atsushi Momose, *Tohoku University, Japan*

# **Tutorial 1**

**(13:30 – 14:15)**

**Historical view of X-ray imaging  
especially using phase information**

**Alessandro Olivo**

*University College London,*

*UK*



# Historical view of X-ray imaging especially using phase information

**Sandro Olivo**, Spokesperson, AXIm Group  
Medical Physics and Biomedical Engineering, UCL



<https://www.ucl.ac.uk/medical-physics-biomedical-engineering/research/groups-and-centres/advanced-x-ray-imaging-group-axim>



Nov 8, 1895 (a Friday, so Roentgen could continue working through the weekend...)

And only 2 weeks later:



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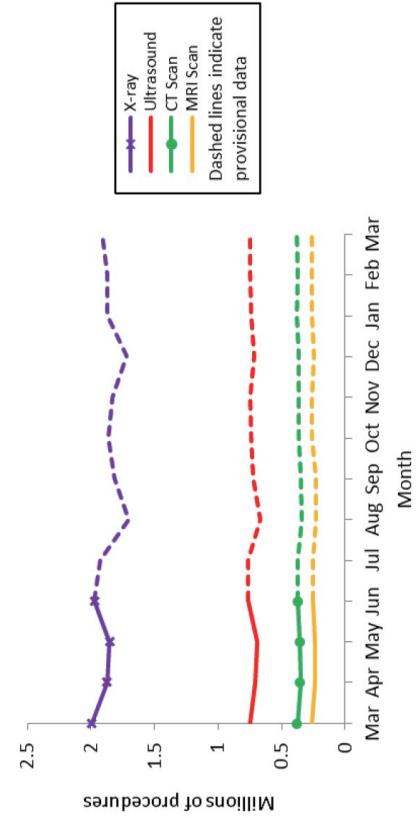
Nov 8, 1895 (a Friday, so Roentgen could continue working through the weekend...)

Many years later:

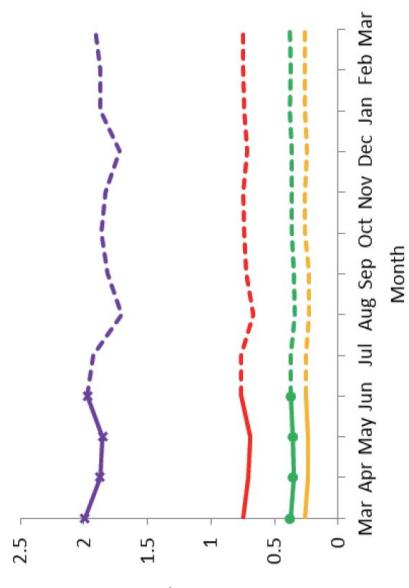
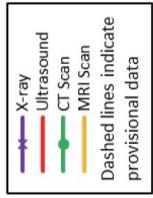


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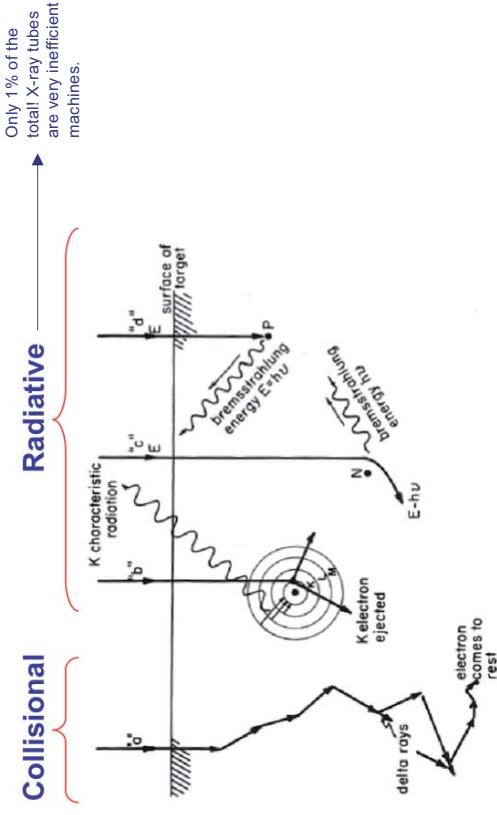
Diagnostic radiology



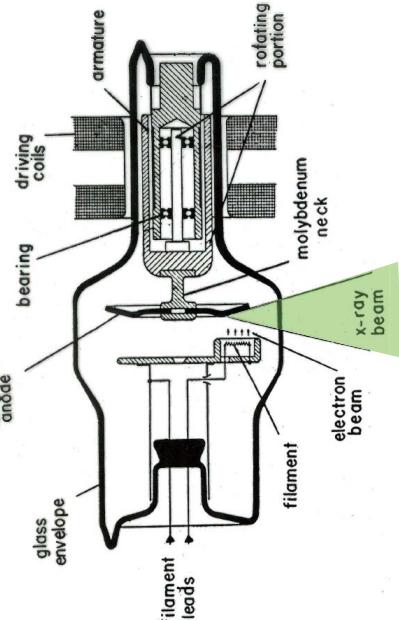
Graph 1: NHS imaging activity in England, March 2015 to March 2016



## How are x-rays generated?

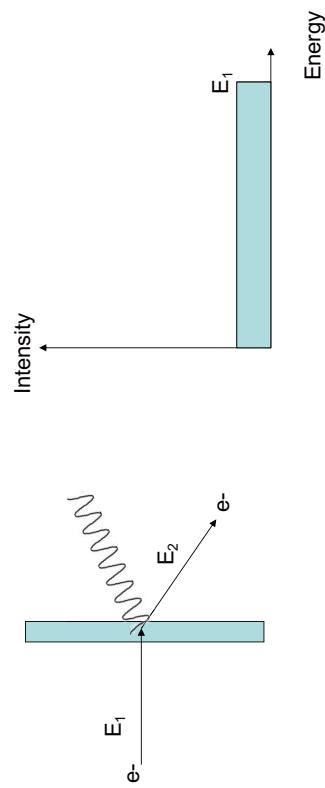
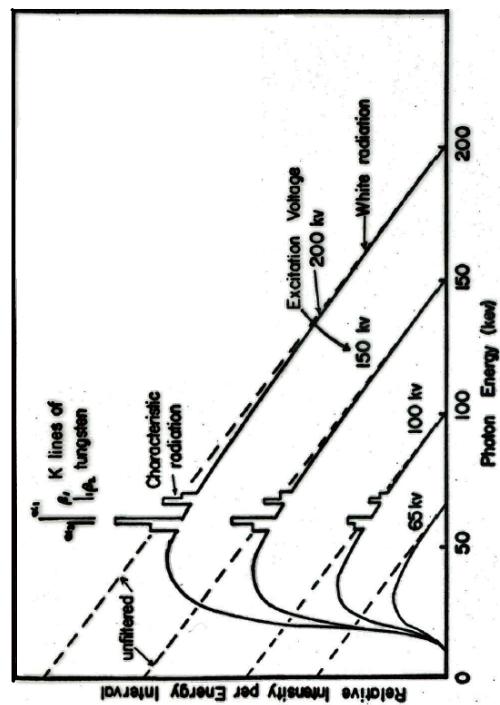


## The x-ray tube



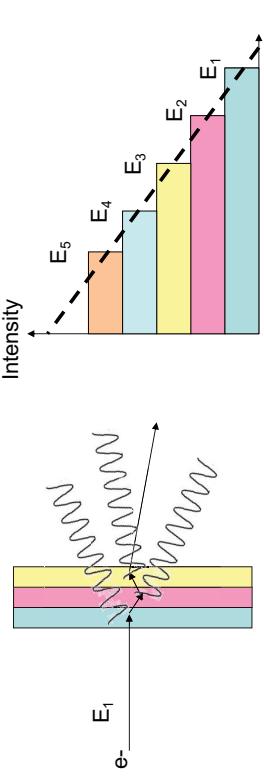
## Why triangular? Thin Target Theory

- Consider target thin enough so that every electron undergoes only **one** radiative interaction while passing through it
- Assume flat distribution for the energy of the emitted x-ray



## Thick Target

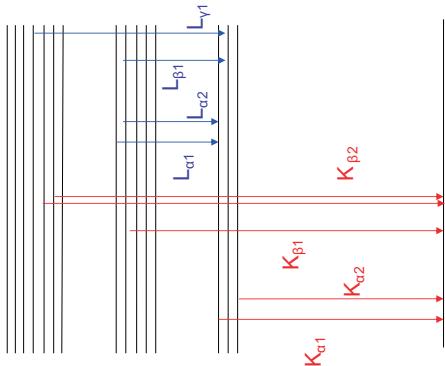
- Consider a thick target to be a number of thin targets superimposed, repeat process! (But with a lower energy every time because you've lost some in the previous step). You obtain a triangular shaped spectrum.



The triangle is “cut” at lower energies because of self-absorption

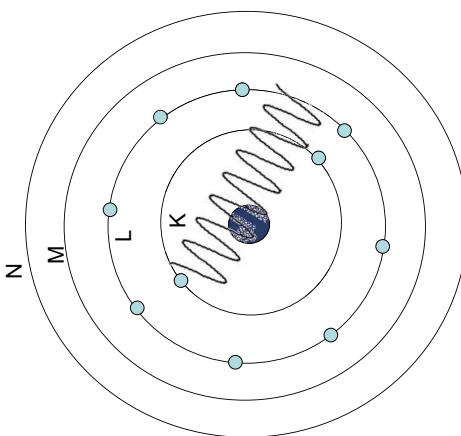
Energy

- Photon energy given by difference in energy levels
- Intensity of line depends on electron density in shells and quantum mechanics selection rules (including e.g. energy difference between shells)



## Lines $\rightarrow$ Characteristic radiation

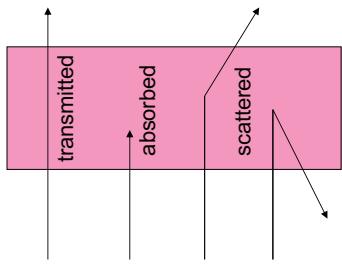
- The bombarding electron ionises the target atom (e.g. the K shell)
  - an  $e^-$  from a higher shell drops down to fill the vacancy



## Processes

- Absorption
- Scatter

### ATTENUATION



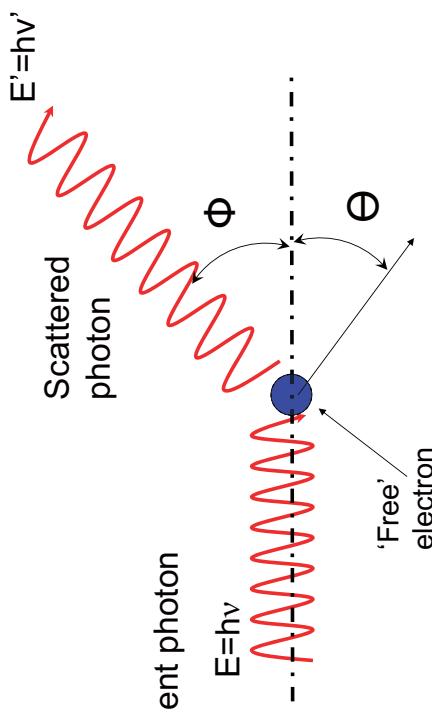
Attenuation is the removal of photons from the primary beam

## Compton scattering

- Incident **x-ray photon\*** scattered by a loosely bound electron (= considered free in the calculations)
- Inelastic: energy of the scattered x-ray <energy of incident x-ray
- Incoherent-scattering centres (electrons) scatter independently

\*NOTE: I tend to use "x-ray" or "photon" interchangeably

## Compton scattering



$$E^2 = p^2 c^2 + m_0^2 c^4$$

## Some equations

- Wavelength shift
- Scattered Photon energy
- Recoil electron kinetic energy
- Relation between scattering angles

$$\lambda' - \lambda = \frac{h}{m_0 c} [1 - \cos \varphi]$$

$$h\nu' = \frac{m_0 c^2}{(1 - \cos \varphi) + 1/\alpha}$$

$$T = h\nu - h\nu' = h\nu \cdot \frac{\alpha(1 - \cos \varphi)}{1 + \alpha(1 - \cos \varphi)}$$

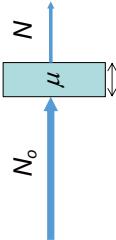
$\alpha = h\nu/m_0 c^2$  i.e. it is the initial x-ray energy expressed in "electron rest masses"

## Probability of Compton Scatter

- Attenuation coefficient  $\mu_{Compton} \propto \rho$

- Why do I express the probability with an attenuation coefficient?

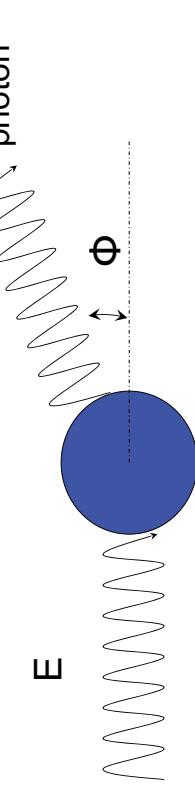
BEER'S LAW  $N = N_0 e^{-\mu t}$  where  $N$  is the number of photons transmitted through a layer of material with thickness  $t$  and attenuation coefficient  $\mu$  hit by  $N_0$  photons:



That " $\mu$ " is the combination of ALL processes that can remove photons from the initial beam i.e.  $\mu = \mu_{photoelectric} + \mu_{Compton} + \mu_{coherent} + \mu_{pair production}$

If beam collimated and small detector since coherent  $\rightarrow$  small-angle scattering

## Coherent Scattering



- Elastic scattering from bound atomic electrons (from the "electron cloud" of the atom)

- interaction is no longer with individual electrons but rather with the entire "electron cloud" – the whole atom takes up the recoil

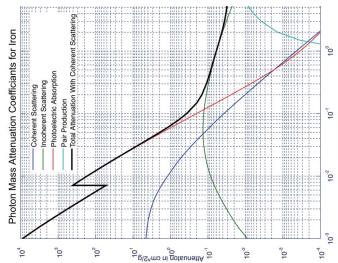
## Coherent scattering is confined to small angles

Al	$Z = 13$	$< 15^\circ - 0.1 \text{ MeV}$
		$< 2^\circ - 1.0 \text{ MeV}$
Pb	$Z = 82$	$< 30^\circ - 0.1 \text{ MeV}$
		$< 4^\circ - 1.0 \text{ MeV}$

- SMALL CONTRIBUTION to the total cross section, especially at high x-ray energy

## Compton or Coherent scatter ?

They coexist (see blue & green lines in graph on the left – but note the vertical scale is logarithmic); Compton "takes over" after a certain energy which depends on the material.



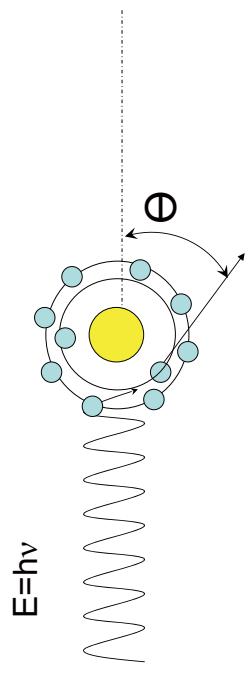
- Basically the probability depends on whether the electrons are seen as almost free or tightly bound, i.e. on the energy of the incoming x-ray compared to the binding energy of the electron (which depends on the material)

## Photoelectric Effect and Characteristic Radiation

- Photons incident on **bound** electrons can be totally absorbed as atom as a whole takes up recoil momentum
- **Photoelectric effect**
  - The excited electron is then emitted with energy  $T = h\nu - B_e$  where  $B_e$  is the binding energy of the electron
  - Effect dominates at low energies ( $<< 0.1 \text{ MeV}$ )

## Photoelectric effect

most interactions are with K-shell electrons



Photoelectron  $e^-$

## What happens when the ionized atom de-excites?

Either

- **Characteristic X-ray**

- Electron drops down from higher shell
- Energy of x-ray depends on relative shell energies

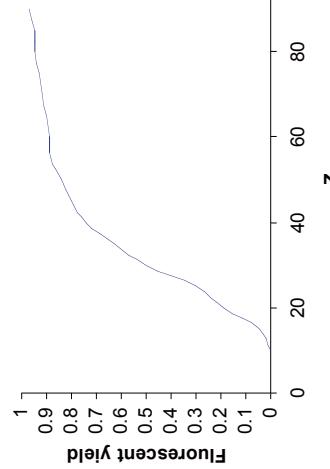
Or

- **Auger electron**

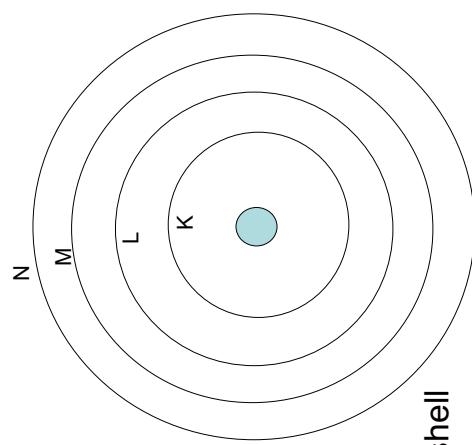
- Energy given to outer shell electron - emitted
- More likely for low atomic number materials

## Fluorescence yield

- Relative probability of characteristic x-ray production compared to auger electron emission



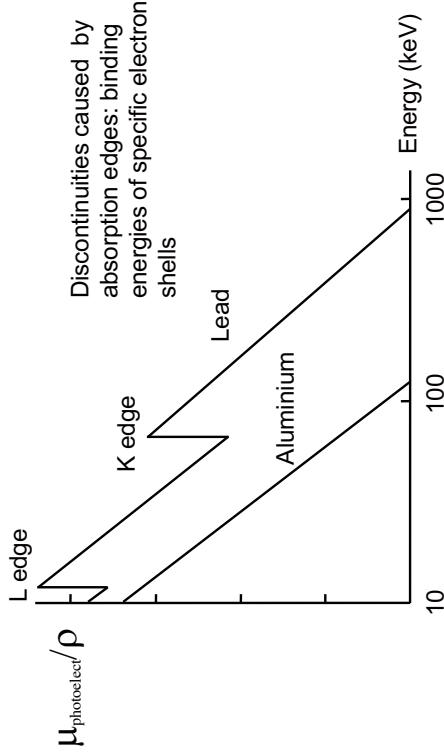
## Characteristic X-ray emission



- Element: W
  - K shell BE: 69.5
  - L<sub>III</sub> shell BE: 10.2
  - M<sub>III</sub> shell BE: 2.3
- If vacancy filled by L<sub>III</sub> shell electron  $h\nu = \dots \dots (K_{\beta})$

## UCL

photoelectric cross-section varies with  $\sim 1/E^3$  - hence it constantly decreases but there are exceptions at attenuation edges.

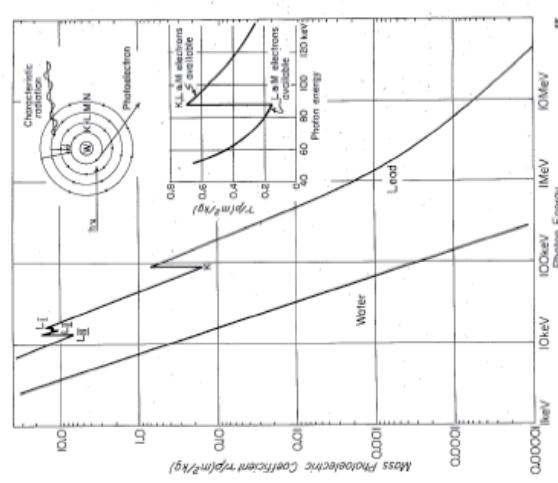


## Absorption Edges

- As the photon energy increases, photoelectric absorption decreases...

- So long as incident x-ray energy is less than binding energy of K-shell electron, x-rays can only kick out L and M shell electrons

- When the x-ray energy becomes greater than K shell binding energy, the attenuation coefficient for photoelectric absorption "jumps up" because the x-rays can now kick out **also K shell electrons** as well as L and M



## K-edges

- For low Z materials, E<sub>k</sub> low (<1keV) so K edge not significant

## Probability of Photoelectric absorption

- Attenuation coefficient

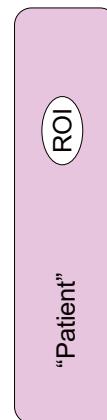
$$\mu_{photoelect} \propto \frac{Z^3 \rho}{E^3}$$

- **Photons interact** and are removed from beam

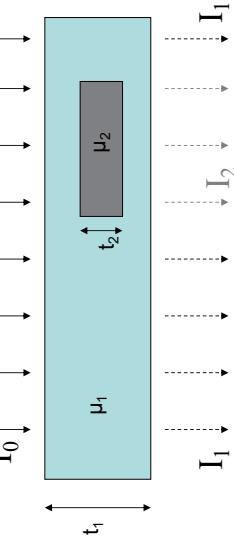
- **Attenuation** (absorption + scattering) depends on:
  - Z
  - Density
  - Thickness

- Leads to variation in detected intensity

**This is how we create an x-ray image**



$$\text{Contrast: } C = \frac{(I_1 - I_2)}{I_1}$$



With:

$$I_1 = I_0 \exp(-\mu_1 t_1)$$

$$I_2 = I_0 \exp[-\mu_1(t_1 - t_2)] \exp(-\mu_2 t_2)$$

Therefore:

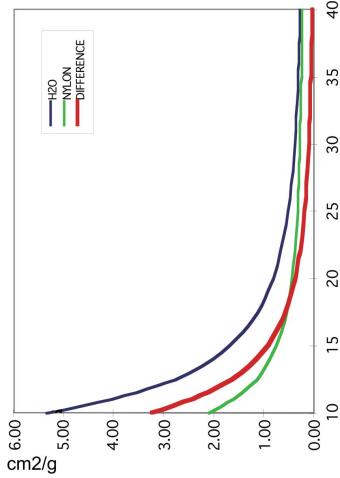
$$\begin{aligned} C &= \frac{(I_1 - I_2)}{I_1} = \frac{I_0 \exp(-\mu_1 t_1) - I_0 \exp[-\mu_1(t_1 - t_2)] \exp(-\mu_2 t_2)}{I_0 \exp(-\mu_1 t_1)} \\ &= \frac{I_0 \exp(-\mu_1 t_1) - I_0 \exp(-\mu_1 t_1) \exp(\mu_1 t_2) \exp(-\mu_2 t_2)}{I_0 \exp(-\mu_1 t_1)} = \end{aligned}$$

$$= \frac{I_0 \exp(-\mu_1 t_1) - I_0 \exp(-\mu_1 t_1) \exp[(\mu_1 - \mu_2)t_2]}{I_0 \exp(-\mu_1 t_1)} = 1 - \exp[(\mu_1 - \mu_2)t_2]$$

C does not depend on I, only on  $\mu$ 's and  $t$ 's -> SUBJECT characteristics (sometimes called "subject" contrast).

C increases with detail thickness (quite obviously) and with the difference between the attenuation coefficients of detail & background:

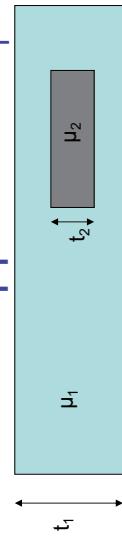
**HOW DOES THIS BEHAVE WITH X-RAY ENERGY?**



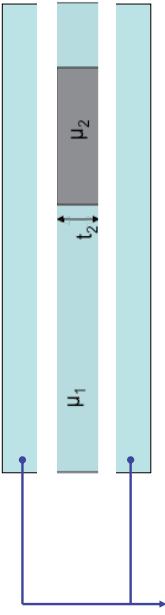
Away from absorption edges, attenuation coefficients decrease with increasing x-ray energy. Therefore, generally speaking the contrast DECREASES with increasing energy.

$$C = 1 - \exp[(\mu_1 - \mu_2)t_2]$$

What happened to  $t_1$ ?



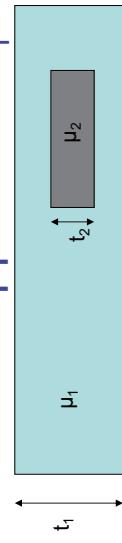
look at it this way:



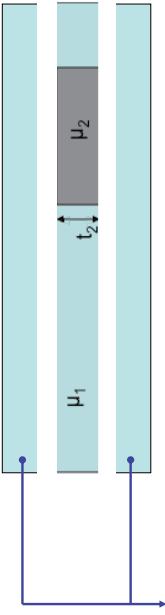
These are two uniform absorbers -> they only change I!

$$C = 1 - \exp[(\mu_1 - \mu_2)t_2]$$

What happened to  $t_1$ ?



look at it this way:



These are two uniform absorbers -> they only change I!

So the Contrast tells you how much a given detail, in percentage, stands out of the surrounding background

It depends on the detail ( $t, \mu$ ) and on the x-ray energy (through  $\mu$ ), but NOT ON THE AMOUNT OF X-RAYS you've used

-> IT DOES NOT TELL YOU how well you'll see it!  
e.g. if you shoot 2 x-rays in total, you'll hardly see anything even if your detail has C=90%!

### Here's where the SNR (or the CNR) becomes important:

(e.g. Rose criterion: a detail is visible if  $SNR \geq 5$ )

THE NOISE IN YOUR IMAGE determines how likely you are to see a detail with a given contrast.

NOISE is normally driven by the amount of x-rays you use (plus quality of your detector and other practical factors)

**SNR:** two “versions” found in the literature:

- 1) (most common) signal VS background noise;
- 2) Signal VS uncertainty on the signal itself.

$$\text{NOTE THAT: } SNR = \frac{N_1 - N_2}{\sqrt{N_1}} = \sqrt{N_1} \frac{N_1 - N_2}{N_1} = \sqrt{N_1} C$$

**SO HERE'S HOW WELL YOU SEE SOMETHING:** it depends on **C** ( $\rightarrow$  object, x-ray energy), and it gets better with the **SQUARE ROOT** of the number of x-rays

$$SNR = \sqrt{N_1} \{1 - \exp[-(\mu_1 - \mu_2)t_1]\} = \sqrt{N_0 \exp(-\mu_1 t_1)} \{1 - \exp[-(\mu_1 - \mu_2)t_2]\}$$

Where  $N_0$  is the number of photons (per unit area) hitting the sample.

**NOTE THAT  $t_1$  now plays a role:** the thicker the sample, the more the beam is attenuated Therefore less photons reach the detector  $\rightarrow$  higher noise  $\rightarrow$  lower SNR

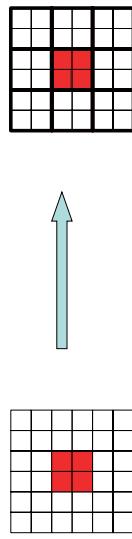
THE DETAILS I'VE GIVEN YOU ARE SIMPLIFIED AND ARE VALID FOR 1 PIXEL ONLY; the extension is straightforward and it involves multiplying x (# pixels involved)<sup>1/2</sup>

THESE DETAILS have the same C and the same number of photons was clearly used. So if  $SNR = \sqrt{N} * C$ , how comes I do not see them anymore below a certain size?

i.e. if a detail covers m pixels, then

$$SNR = \sqrt{m} \sqrt{N_1 C}$$

The explanation is extremely intuitive: imagine **binning** your pixels (e.g. 2x2 in the simple case the detail covers 4 pixels)



Now the detail covers 1 pixel, which receives 4 times as many counts i.e.  $4N_1$  counts in total:  $SNR = \sqrt{4N_1} C = \sqrt{4} \sqrt{N_1} C$

## Effect of scatter on contrast:

- WITHOUT scatter:
- WITH scatter:

$$C = \frac{I_1 - I_2}{I_1}$$

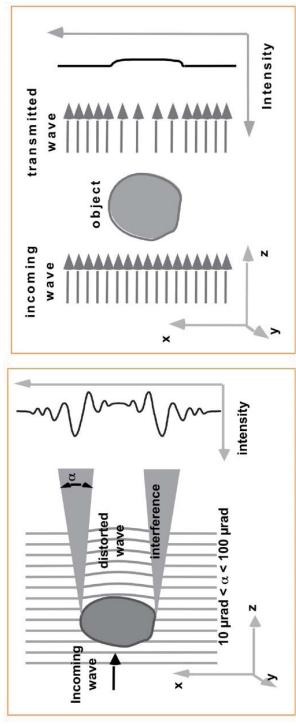
- A. Remove scatter
- B. Increase inherent contrast
  - **Contrast agent**
- C. Reduce kV
  - **Photoelectric effect  $\propto Z^3 E^{-3}$**
- D. Remove effects of overlying tissues
- E. USE PHASE CONTRAST!**

## Ways to improve contrast

- A. Remove scatter
- B. Increase inherent contrast
  - **Contrast agent**
- C. Reduce kV
  - **Photoelectric effect  $\propto Z^3 E^{-3}$**
- D. Remove effects of overlying tissues
- E. USE PHASE CONTRAST!**

$$C' = \frac{(I_1 + S) - (I_2 + S)}{I_1 + S} = \frac{I_1 - I_2}{I_1 + S} < C$$

## Phase Contrast Imaging vs. Conventional Radiology



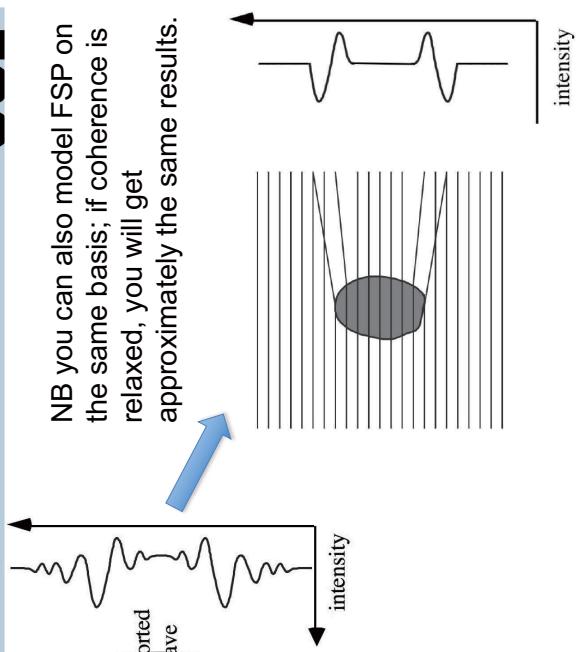
Refractive index:  $n = 1 - \delta + i\beta; \delta \gg \beta \rightarrow$   
 $\text{phase contrast } (\Delta I/I_0 \sim 4\pi\delta\Delta z/\lambda) \gg \text{absorption contrast } (\Delta I/I_0 \sim 4\pi\beta\Delta z/\lambda)$

**Two possible approaches:**

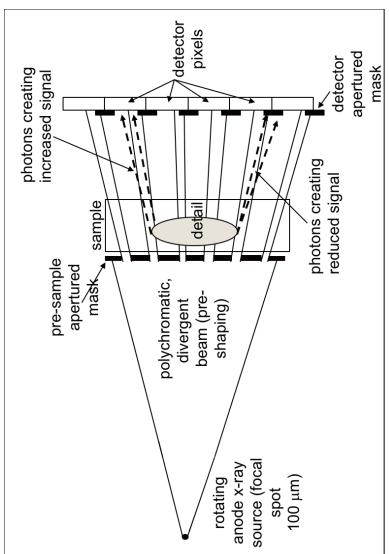
- detect interference patterns
- detect angular deviations



NB you can also model FSP on the same basis; if coherence is relaxed, you will get approximately the same results.



Which can be extended to full FoV imaging using large area masks  
(see e.g. invited talk by Massimi and talks by Endrizzi later in the conference)

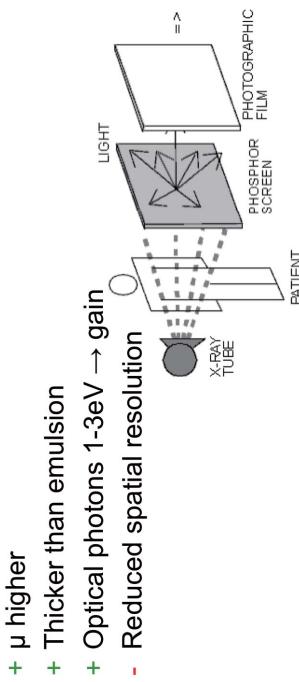


There are of course many other ways to exploit phase effects,  
even more based on interferometric effects – **Prof Franz Pfeiffer**  
will tell you all about that in the lecture following this one.

Before I leave you to Franz, a few historic milestones:

### Film-Screen

- Use fluorescent screen



The stopping power of the plain film is only 1-3% of the one provided by a modern intensifier screen (Sabel and Aichinger, 1996).

### a few historic milestones

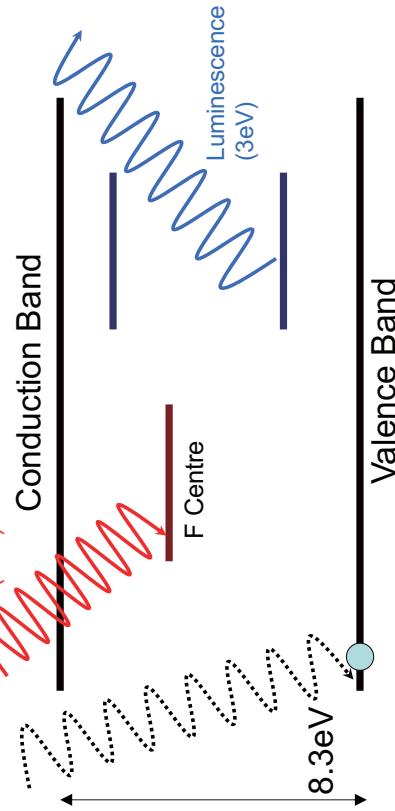
“A new system of computed radiography that is based on new concepts and the latest computer technologies has been developed. This system eliminates the drawbacks of conventional screen-film radiography. The basic principle of the system is the conversion of the x-ray energy pattern into digital signals utilizing scanning laser stimulated luminescence (SLSL)” (Sonoda et al., 1983)

Red laser light  
(2eV)

Conduction Band  
F Centre

Luminescence  
(3eV)

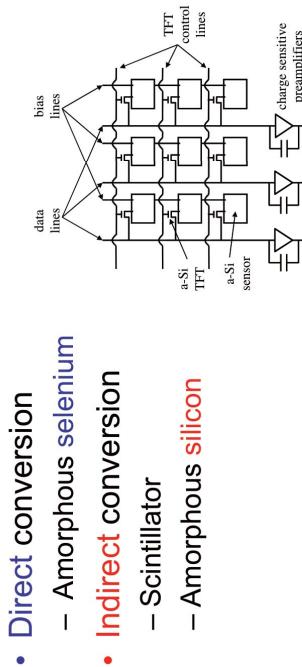
Valence Band



Computed Radiography:  
Photostimulable Phosphor  
(PSP) plate

## a few historic milestones

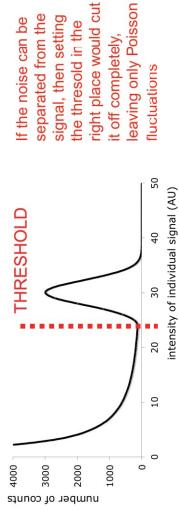
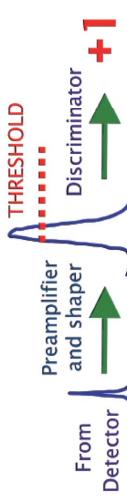
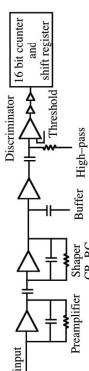
### Flat Panel Detectors



- Direct conversion
  - Amorphous selenium
- Indirect conversion
  - Scintillator
  - Amorphous silicon

## a few historic milestones

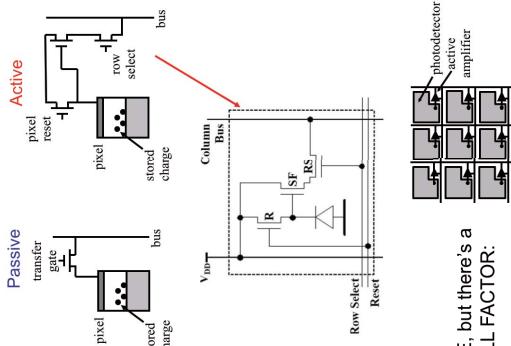
### Single-photon counting readout scheme



## a few historic milestones

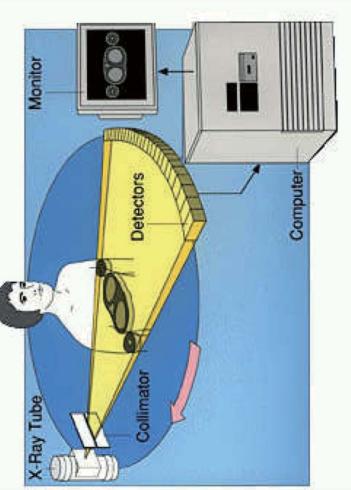
### CMOS sensors

- Reset transistor 'R' clears the pixel of integrated charge
  - Source Follower transistor 'SF' amplifies/buffers the signal (**ACTIVE** pixel)
  - Row Select transistor 'RS' selects the row for readout.
- ACTIVE** → reduces NOISE, but there's a price to pay in terms of FILL FACTOR:



## a few historic milestones

### Computed Tomography

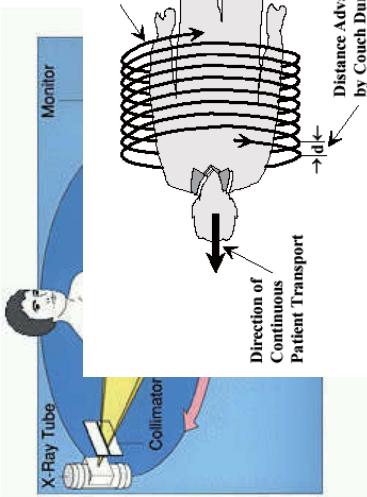


## a few historic milestones

### Computed Tomography

a few historic milestones

## Computed Tomography



... all details in Prof Marco Stampaponi's lecture later today

## Thanks for listening

**QUESTIONS??**

## **Tutorial 2**

**(14:15 – 14:45)**

# **Historical view of neutron radiography**

**Dmitry A. Pushin**

*University of Waterloo,*

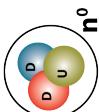
*Canada*

## Acknowledgements – NIST Neutron Imaging Team



L2-3

## The Neutron

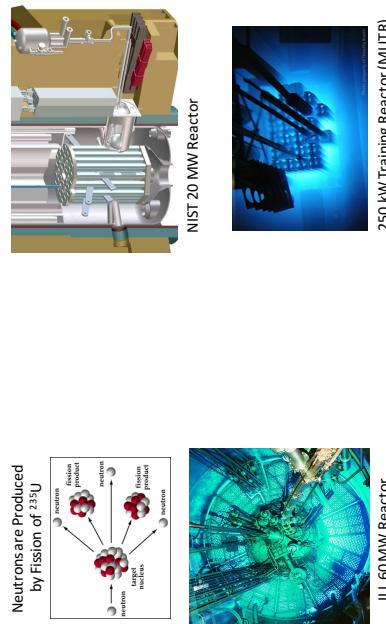


- Discovered 1932 by James Chadwick
- A fundamental building block of atomic nucleus
- Free neutron lifetime  $\sim 15$  min ( $880.2 \pm 1.0$  s)
- Neutron mass =  $1.001378419$  proton mass
- Produced from fission (nuclear reactor) or scattering of high energy proton beams (spallation source)
- Electrically neutral but has magnetic moment
- Thermal neutron unique penetrating abilities

nobelprize.org  
1935.

L2-4

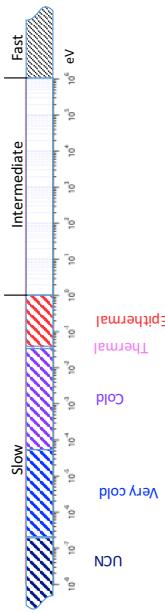
## Neutron production



250 kW Training Reactor (MUTR)

L2-6

## Neutron Spectrum



### A thermal neutron has:

- Energy of 20 meV
- Wavelength of 2 Å
- Speed of 2000 m/s

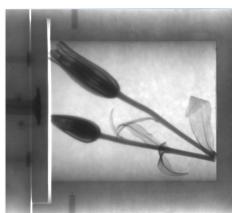


© Daniel Hussey, NIST

L2-7

## Imaging with Neutrons

The fine details of the water concentration in these lilies are clear to neutrons even in a lead cask



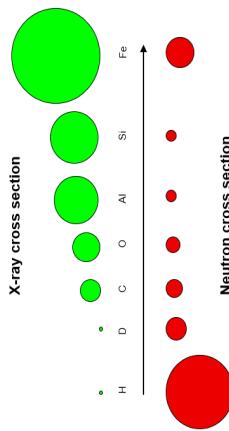
Neutron radiography



Ordinary photography

## Great things about neutrons

- Neutrons penetrate many materials well yet remain extremely sensitive to liquid water, hydrocarbons, and lithium
- This allows one to study a wide range of transport related issues like:
  - Liquid water in fuel cells
  - Lithium in batteries
  - Multiphase flowing geological rock cores



### Neutron cross section



Neutron image

- Metal parts: transparent
- Plastic parts: opaque

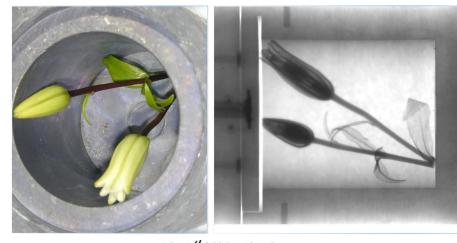


PSI

L2-8



DCComics

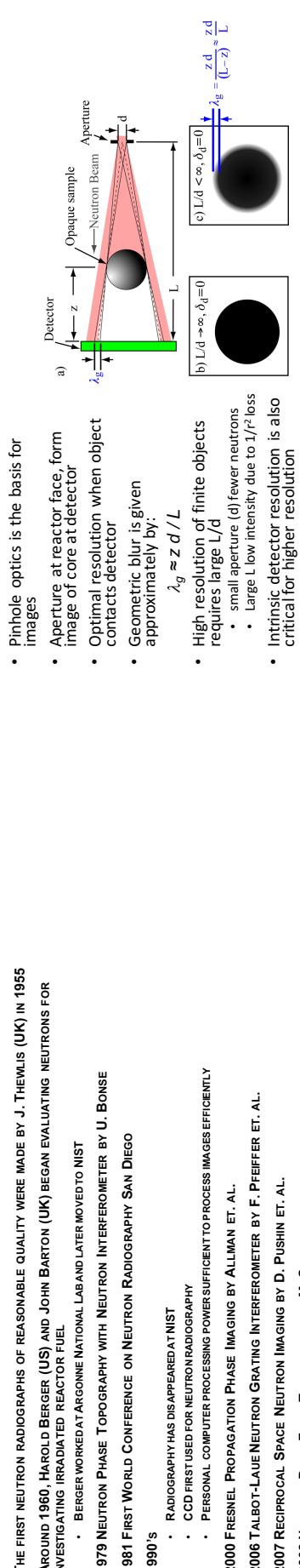


Daniel Hussey, NIST

## Brief Historical Perspective

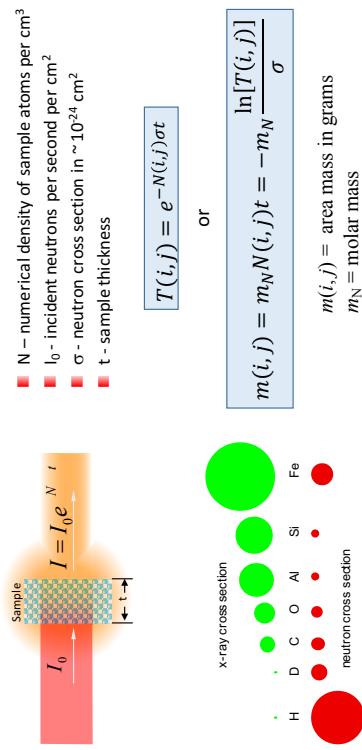
- THE FIRST DEMONSTRATION OF NEUTRON RADIOPHOTOGRAPHY WAS MADE BY HARTMUT KALLMANN AND E. KUHN IN THE LATE 1930S
- THE FIRST NEUTRON RADIOPHOTOGRAPHS OF REASONABLE QUALITY WERE MADE BY J. THEWLIS (UK) IN 1955
- AROUND 1960, HAROLD BERGER (US) AND JOHN BARTON (UK) BEGAN EVALUATING NEUTRONS FOR INVESTIGATING IRRADIATED REACTOR FUEL
  - BERGER WORKED AT ARGONNE NATIONAL LAB AND LATER MOVED TO NIST
- 1979 NEUTRON PHASE TOMOGRAPHY WITH NEUTRON INTERFEROMETER BY U. BONSE
- 1981 FIRST WORLD CONFERENCE ON NEUTRON RADIOPHOTOGRAPHY SAN DIEGO
- 1990's
  - RADIOPHOTOGRAPHY HAS DISAPPEARED AT NIST
  - CCD FIRST USED FOR NEUTRON RADIOPHOTOGRAPHY IN 1990
  - PERSONAL COMPUTER PROCESSING POWER SUFFICIENT TO PROCESS IMAGES EFFICIENTLY
- 2000 FRESNEL PROPAGATION PHASE IMAGING BY ALLMAN ET. AL.
- 2006 TALBOT-LAUE NEUTRON GRATING INTERFEROMETER BY F. PFEIFFER ET. AL.
- 2007 RECIPROCAL SPACE NEUTRON IMAGING BY D. PUSHIN ET. AL.
- 2008 NEUTRON DARK-FIELD TOMOGRAPHY BY M. STROBL ET. AL.
- 2017 PHASE-GRATING MOIRÉ NEUTRON INTERFEROMETER BY D. PUSHIN ET. AL.
- 2019 XNP(G2019 SENDAI, JAPAN

## Neutron Imaging Geometry



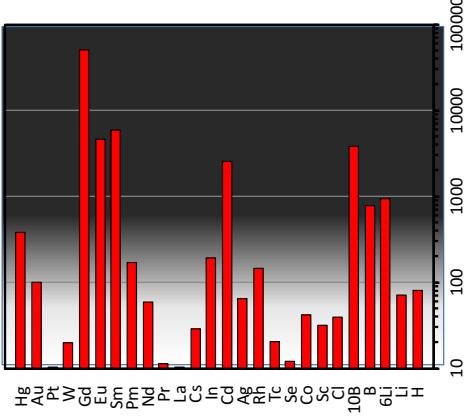
- Pinhole optics is the basis for images
- Aperture at reactor face, form image of core at detector
- Optimal resolution when object contacts detector
- Geometric blur is given approximately by:
$$\lambda_g \approx z d / L$$
- High resolution of finite objects requires large  $L/d$ 
  - small aperture ( $d$ ) fewer neutrons
  - Large  $L$  low intensity due to  $1/r^2$  loss
  - Intrinsic detector resolution is also critical for higher resolution

## Quantification



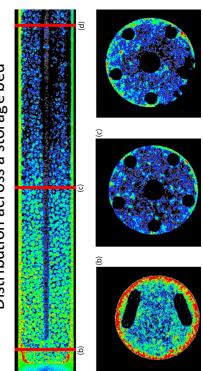
## Cross Sections

- Values below 10 have low contrast
- Between 10 - 100 contrast is good for high resolution
- Values above 100 are difficult to penetrate
- Greater than 300 they make excellent beam stops

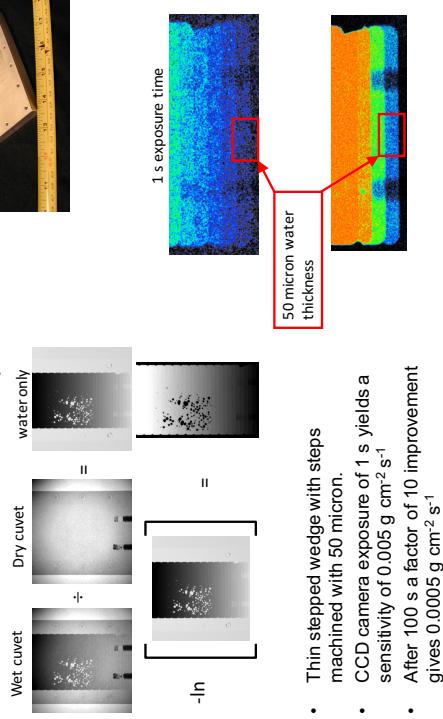


## Contrast Agents

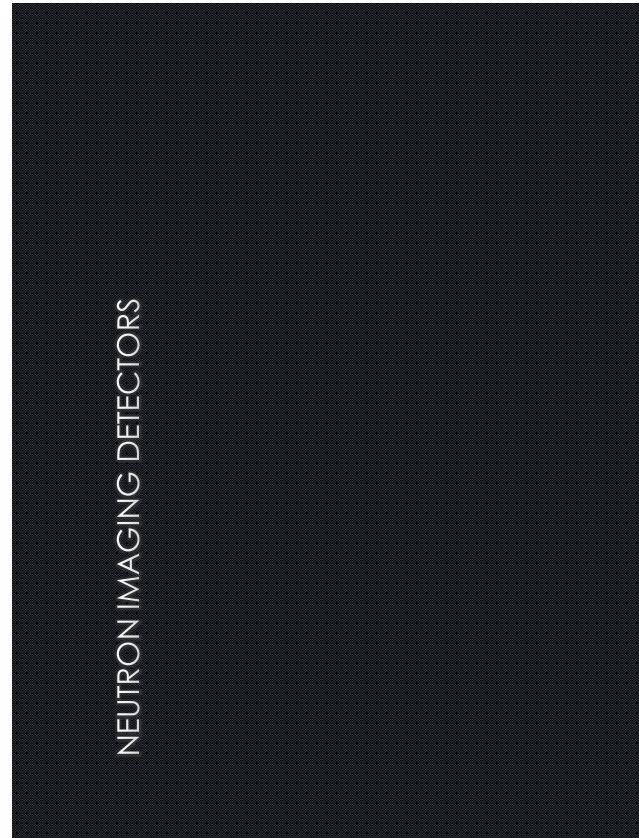
- Used to turn contrast on or off
- Deuterium and Hydrogen**
  - Replacement of hydrogen with deuterium is frequently used to turn off the hydrogen signal
  - Thick hydrogen samples can be imaged better in some cases by replacing the hydrogen with deuterium
- Gadolinium has an enormous cross section
- $\text{Gd}(\text{NO}_3)_3$  salts can be used to image cracks



## Water Sensitivity



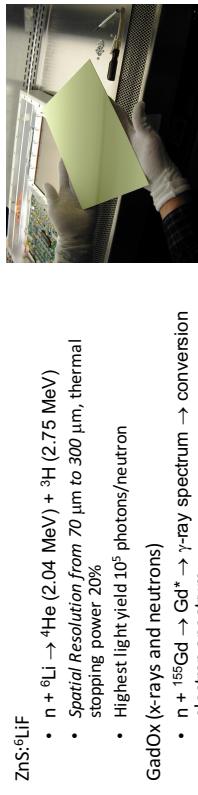
## NEUTRON IMAGING DETECTORS



## Nuclear Reactions for Neutron Imaging

- $n + {}^6\text{Li} \rightarrow {}^4\text{He} (2.04 \text{ MeV}) + {}^3\text{H} (2.75 \text{ MeV})$
- $n + {}^{10}\text{B} \rightarrow {}^7\text{Li}^* + {}^4\text{He} \rightarrow {}^7\text{Li} (0.84 \text{ MeV}) + {}^4\text{He} (1.47 \text{ MeV}) + {}^2\text{H} (93\%)$
- $n + {}^{155}\text{Gd} \rightarrow \text{Gd}^* \rightarrow \gamma\text{-ray spectrum} \rightarrow \text{conversion electron spectrum}$
- $n + {}^{157}\text{Gd} \rightarrow \text{Gd}^* \rightarrow \gamma\text{-ray spectrum} \rightarrow \text{conversion electron spectrum}$
- ${}^3\text{H}$  range in ZnS > 30 mm (SRIM calculation) but as much as 120

## Neutron Scintillators



$\text{ZnS:}^6\text{LiF}$

- $\text{n} + {}^6\text{Li} \rightarrow {}^4\text{He}$  (2.04 MeV) +  ${}^3\text{H}$  (2.75 MeV)
- Spatial Resolution from 70  $\mu\text{m}$  to 300  $\mu\text{m}$ , thermal stopping power 20%
- Highest light yield  $10^5$  photons/neutron

GadOx (X-rays and neutrons)

- $\text{n} + {}^{155}\text{Gd} \rightarrow \text{Gd}^*$   $\rightarrow \gamma$ -ray spectrum  $\rightarrow$  conversion electron spectrum
- $\text{n} + {}^{157}\text{Gd} \rightarrow \text{Gd}^*$   $\rightarrow \gamma$ -ray spectrum  $\rightarrow$  conversion electron spectrum
- Resolution ~20-60  $\mu\text{m}$ , thermal stopping power up to 80%
- Low light yield ( $10^3$  photons/neutron) since conversion electrons are < 100 keV
- Other Gd type scintillators (GGG) resolution of 7  $\mu\text{m}$  reported

L2-19

## Microchannel Plate Detectors



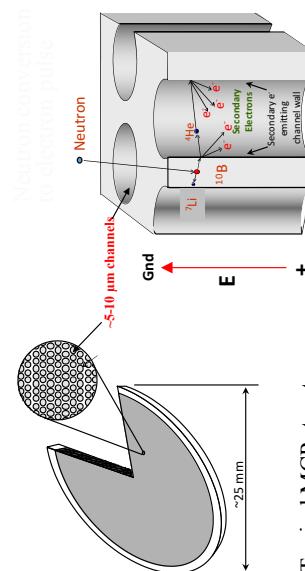
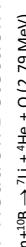
### Microchannel plate detectors

- 1984, R. Schrack, NIMA
- 1990 Boron Doped MCPs (Fraser, et al, NIMA, 377,p119)
- 1996 ND&M (Dietze, et al, NIMA,377,p320)
  - Counting detector SNR
  - Incorporates centroiding to get 50  $\mu\text{m}$  resolution
  - Count rate very limited
  - Extremely innovative detector developed in Munich!
  - Led to rebirth of Neutron Radiography at NIST!
  - 2006 Boron/Gd Doped MCPs with Cross delay line anode detectors
  - 2009 Boron/Gd Doped MCPs with Cross strip detectors (1-2 MHz max count rates) (Tremesin, et al, NIMA, 604, p140 (2009))

## Advanced High Resolution Neutron Imaging Detector

L2-20

### Borated MCP Neutron Detection Mechanism



Typical MCP structure



40mm XS anode neutron detector showing the front of the detector on the 6" conflat flange, and the HV connections.

• Berkley Space Sciences Laboratory  
• Benson Sciences, LLC  
• NOVA Scientific

## Detectors: Light Imagers

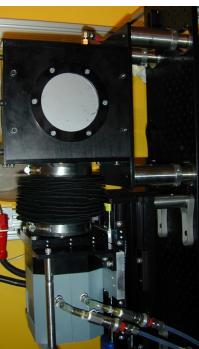
### Amorphous Silicon

- Estermann, et al, NIMA, 542, p253 (2005)
- Fixed pixel pitch of 127  $\mu\text{m}$ , 25x20cm FOV
- Up to 30Hz frame rate (2x2 binning)
- Amorphous silicon sensor is mostly rad hard
- Non-rad hard readout electronics are folded out of the beam
- LiF:



L2-23

### NIST Camera Box



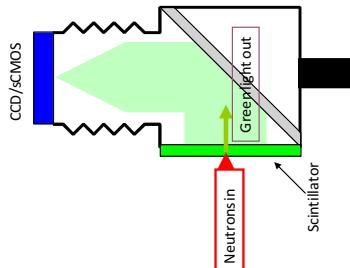
- Lens/Camera is soft coupled by a flexible bellows for light tightness  
Lens adjusted by hand or mechanical control  
Fine focus by moving camera on a translation stage  
Lens coupled enables flexibility  
CCD has slow readout that limits time resolution  
Andor Neo sCMOS,  
• 2560 x 2160,  
• 6.5  $\mu\text{m}$  pixels,  
• 30 fps burst mode 100 fps with on board 4 Gb memory
  - 1 e read noise
  - FOVs:
    - 1.66 cm x 1.40 cm
    - To 26 cm x 26 cm (beam size)

## Neutron CCD/sCMOS Imaging Device

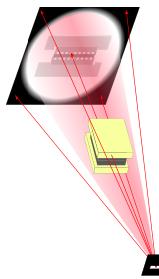
First method used by many to capture digital radiographs

### Most versatile

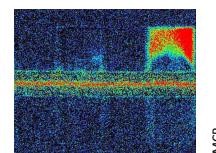
- Can use standard Nikon lenses
  - Any light emitting converter
  - MCP intensified and gated cameras for dynamic imaging
- Images are high quality except for those distorted by the lens  
Light collection efficiency is low due to distance and lens  
Current generations low noise allow single photon counting  
Readout Time/Frame Rate
- CCD 3 s – 5 s or more
  - EMCCD 10 Hz
  - sCMOS 100 Hz and more



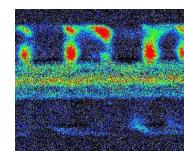
L2-24



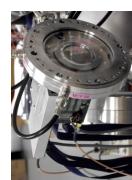
### Fuel Cell Water Profile



CCD/sCMOS  
Spatial Resolution: 13  $\mu\text{m}$   
Field of View: 3.5 cm x 3.5 cm  
Frame Rate: 10 s – 20 min

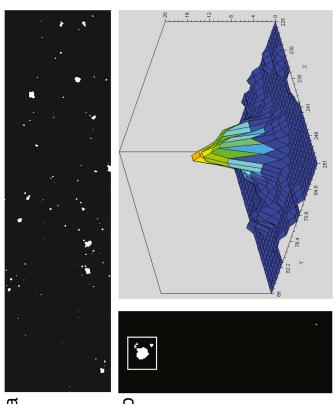


CCD/sCMOS  
Spatial Resolution: 20  $\mu\text{m}$   
Field of View: 1 cm x 1 cm  
Frame Rate: 100 frame/s



## Another Potential Path to High Resolution: Light Centroiding

- Light from scintillator blooms out
- Size of the light bloom results in blurring in the image
- Spatial resolution is  $25 \mu\text{m}$  due to blurring
- Image intensifier improves signal
- New sCMOS cameras allow very high frame rates (100 fps)
- Individual neutron strikes can be captured
- Centroiding the light clouds could get to sub  $5 \mu\text{m}$  resolution
- Modern field-programmable gate array (FPGA) could allow efficient centroiding

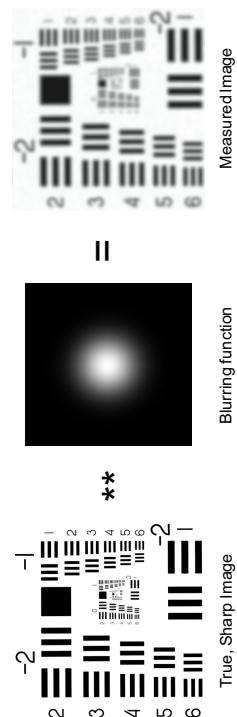


D. S. Hussey, J. M. Lalivanna, E. Baltic, D. L. Jacobson, Nucl. Inst. and Meth. A, **866** (2017) 9–12

L2-27

## Spatial Resolution

- Resolution described by point spread function (PSF) which introduces cross-talk between all the pixels
- The cross-talk, besides blurring out detail, also introduces an effective background which changes the observed attenuation
- This is seen in the “Measured Image” where black areas are now grey
- Deconvolution algorithms can be used to correct this systematic effect



L2-28

## Spatial Resolution

- 1951 USAF TARGET
  - LIMITING RESOLUTION
    - 10 % CONTRAST (MTF 10 %)
    - HERE 28.5 LINE PAIRS PER MILLIMETER FOR LINE PAIR WIDTHS OF 17.54 MM.
    - SPATIAL RESOLUTION IS  $\sim 18 \text{ MM}$
- 

## Setting up the Image for Radiography or Tomography

- Lots of room for sample setup
- 6 meters from aperture to sample position.
- Aluminum flight tube evacuated.
- Short sections can be made into a shorter tube for closer positions.
- Closest position is 1 meter.



L2-26

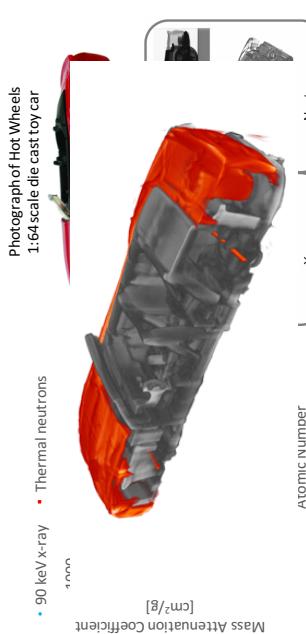
L2-29

Why combine neutrons and X-rays? Awesome complementarity!



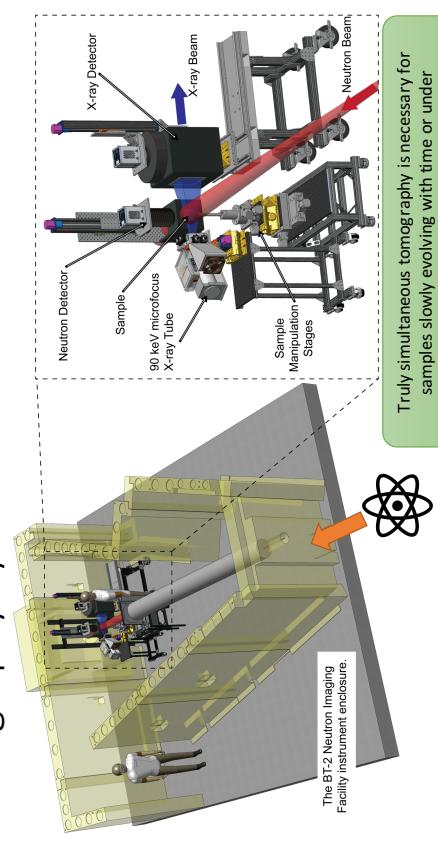
L2-30

Why combine neutrons and X-rays? Awesome complementarity!



L2-31

## The NIST Simultaneous Neutron and X-ray Tomography System



J.M. LaMantia et al., "Neutron and X-ray Tomography (NeXT) System for Simultaneous Dual Modality Tomography", Rev. Sci. Inst., 88, 113702 (2017).

L2-32

## Identification of Organic and Mineral Distributions in Shale

- Aim: Understand distribution of shale constituents to improve understanding of hydraulic fracturing
- Initial well characterized open literature samples

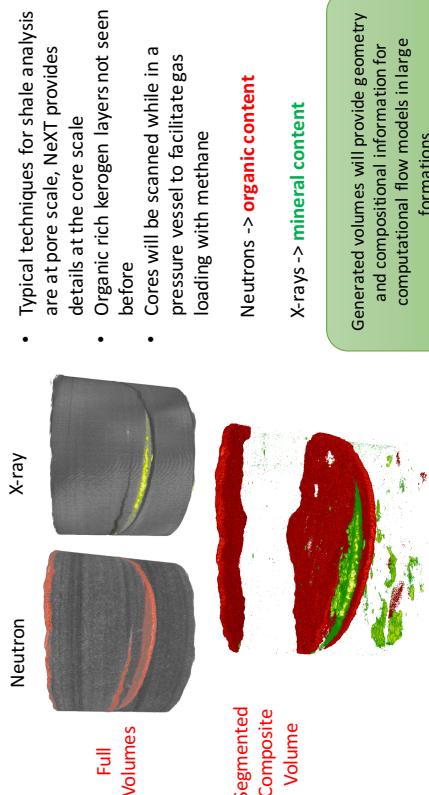
Neutrons -> **organic content**

X-rays -> **mineral content**

Hydrocarbons, dense minerals, and fractures all identified for improved computational modeling.

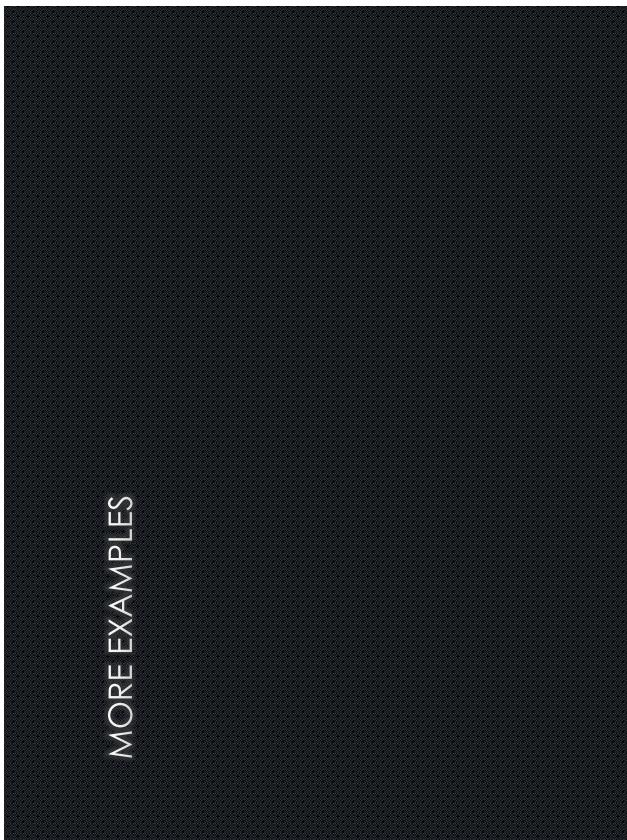
W.S. Chang et al., "Simultaneous Neutron and X-Ray Imaging of 3D Structure of Organic Matter and Fracture in Shales", PETROPHYSICS, VOL. 59, NO. 2 (APRIL 2018), PAGES 153–161.

## Extended Analysis to Cores from Production Wells

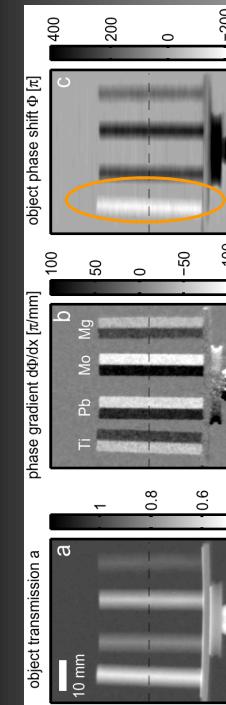


W.S. Chiang et al., "Simultaneous Neutron and X-Ray Imaging of 3D Structure of Organic Matter and Fracture in Shales", PETROPHYSICS, VOL. 59, NO. 2 (APRIL 2018), PAGES 153-161.

## MORE EXAMPLES



## NEUTRON PHASE CONTRAST RADIOGRAPHY

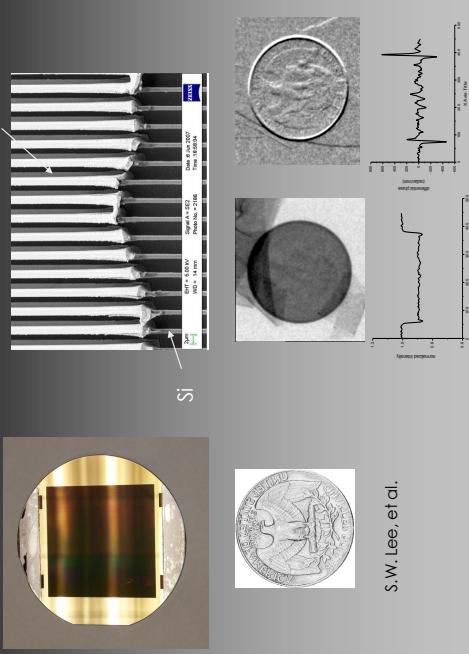


*total exposure time ~ 100 sec,  
spatial resolution ~ 250 micron*



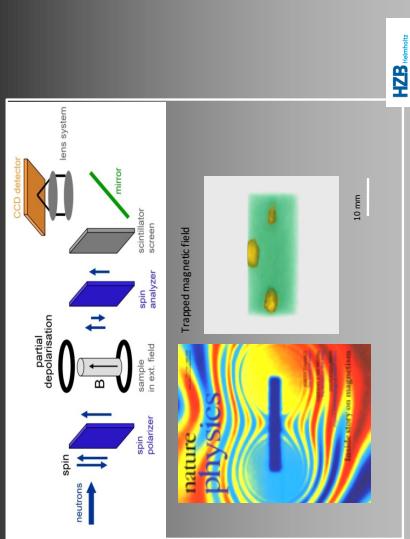
F. Pfeiffer, C. Grünzweig, O. Bunk,  
G. Frei, E. Lehmann and C. David  
*PRL 96*, 215505 (2006).

## Grafting Phase Imaging

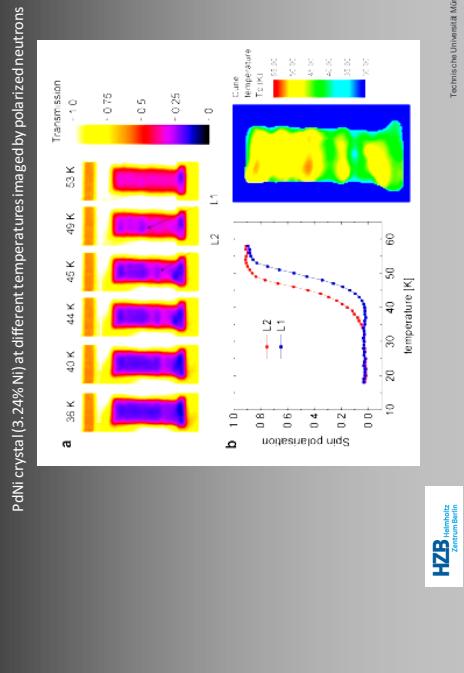


S.W. Lee, et al.

## IMAGING WITH POLARIZED NEUTRONS

N. Kardjiev et al. *Nature Physics* 4, 398, 2008

## Phase transitions in magnetic systems

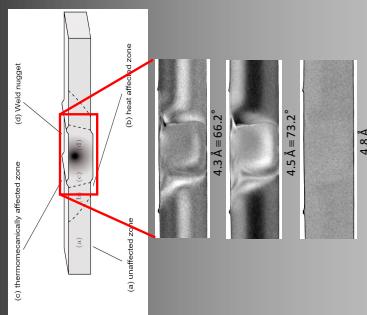


TUM

HZB  
Helmholtz-Zentrum Berlin  
Zentrum für Materialien und  
Brennstoffe

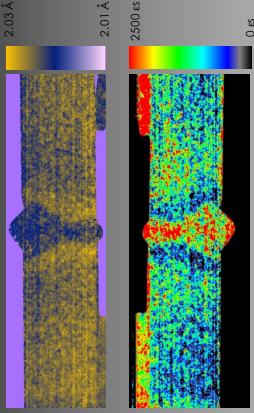
## ENERGY SELECTIVE IMAGING

- Bragg Edge of Al is at  $7\text{\AA}$
- Wavelength dependent attenuation was measured from  $2.7\text{\AA}$  to  $6.0\text{\AA}$
- Low attenuation of Al leads to long exposure times of 45 min to give sufficient contrast
- Texture: preferred orientation of crystallites wrt. the incoming beam leads to dark areas at certain wavelengths
- Each wavelength corresponds to one reflection angle

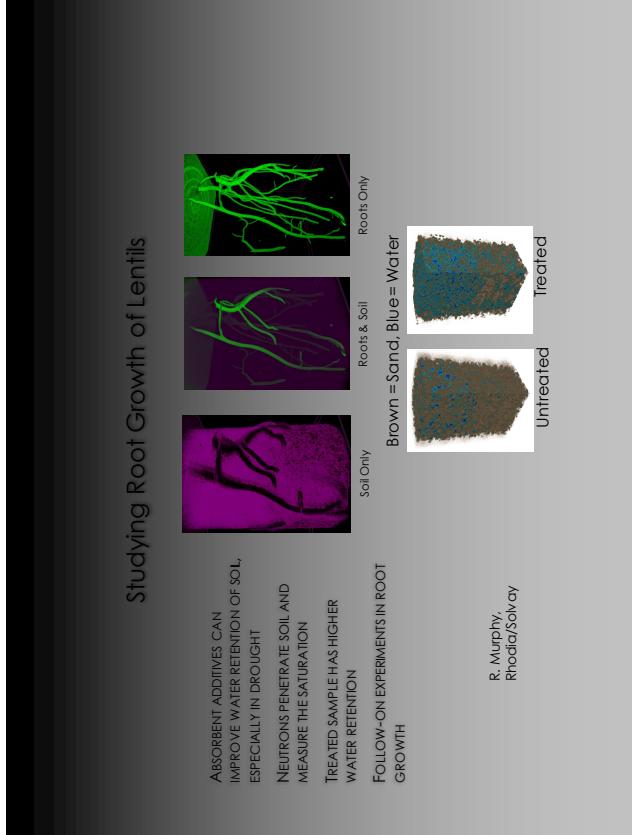
Brockhaus Institute  
Helmholtz-Zentrum Berlin

"Bragg Edge" is increase in transmission when  $\lambda > 2d_{\text{hkl}}$   
Acquire many images over narrow  $\lambda$  band  
Compressive strain map constructed from Bragg-edge image (chemical and mechanical) Here, image spatial resolution is  $50\text{ \mu m}$ , sample is  $1\text{ cm} \times 2\text{ cm} \times 6\text{ cm}$

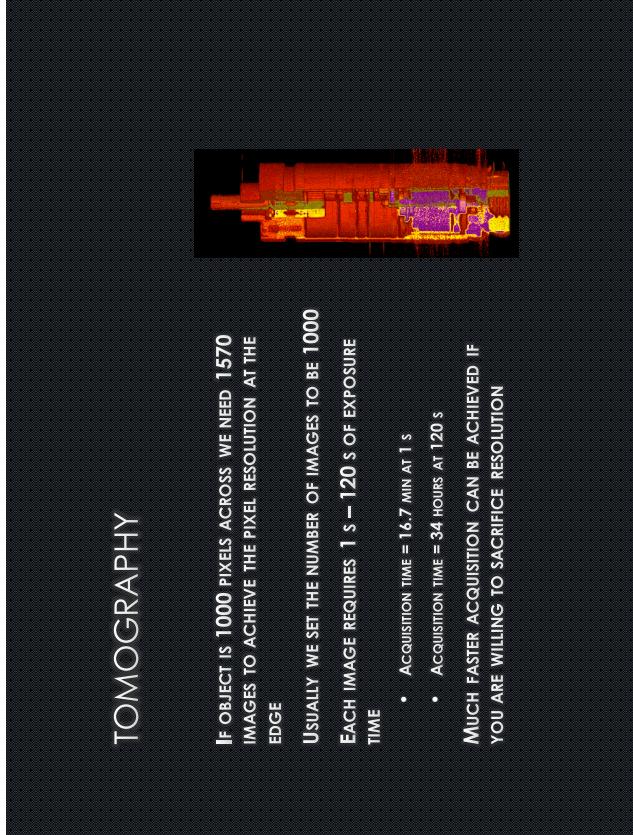
## Imaging of Laser Weld



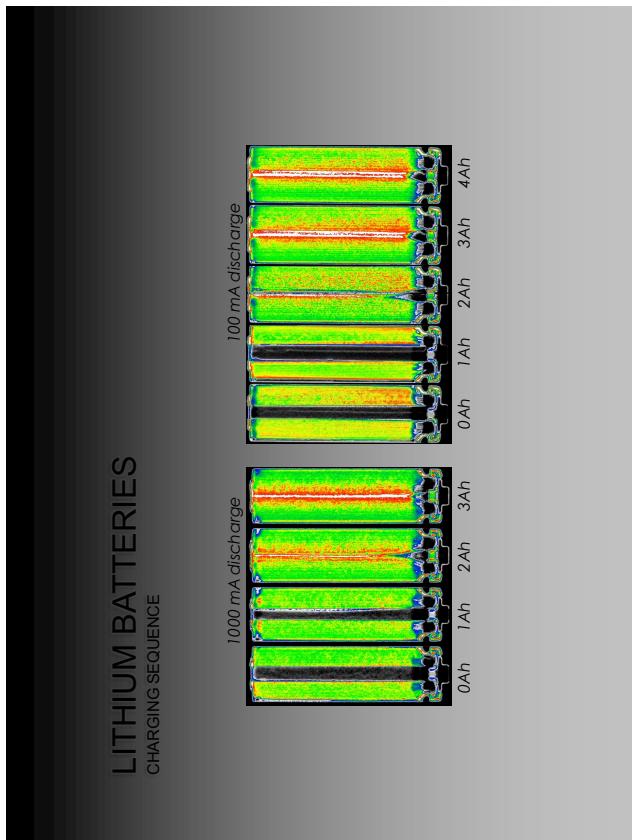
"Bragg Edge" is increase in transmission when  $\lambda > 2d_{\text{hkl}}$   
Acquire many images over narrow  $\lambda$  band  
Compressive strain map constructed from Bragg-edge image (chemical and mechanical) Here, image spatial resolution is  $50\text{ \mu m}$ , sample is  $1\text{ cm} \times 2\text{ cm} \times 6\text{ cm}$



L2-43

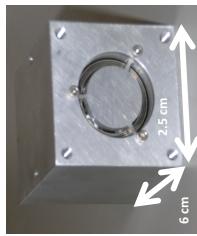
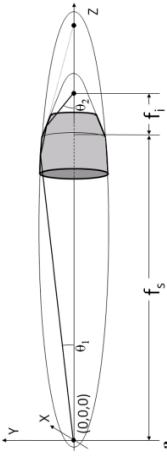


L2-44



### Neutron Microscope

Ellipsoid – Hyperboloid for Image Magnification



- Prototype lens**
- 4 nested Ni mirrors
  - nesting increases flux collection

- Observed Performance:**
- 75 μm spatial resolution
  - 1 cm FOV & 4x magnification
  - 5 mm depth of focus
  - 5x gain in intensity to pinhole

Liu et al., Appl. Phys. Lett. 102, 183508 (2013)

## CONCLUSION

### RADIOGRAPHY AND TOMOGRAPHY WITH NEUTRONS

- GOOD FOR TWO PHASE FLOW WHEN X-RAYS CAN'T PENETRATE METAL OR ROCK
- UNIQUE CONTRAST FOR CERTAIN ELEMENTS ESPECIALLY HYDROGEN
- ISOTOPIC CONTRAST AS WELL ALLOWS CONTRAST TO BE VARIED

### MULTIMODAL IMAGING WITH X-RAYS AND NEUTRONS

- OVERCOMES REGISTRATION OF X-RAY AND NEUTRON TOMOGRAPHY
- PRODUCES IN SITU COMPLETE PICTURE FOR TWO PHASE FLOW PROBLEMS
- ALLOWS 2-D HISTOGRAM OF X-RAY/NEUTRON ATTENUATION COEFFICIENT TO BETTER SEGMENT PHASES

### FUTURE: ENERGY SELECTIVE STRESS/STRAIN IMAGING WITH HIGH SPATIAL RESOLUTION

- IMPACT FOR UNDERSTANDING STRESS/STRAIN IN ADDITIVE MANUFACTURING METHODS

### FUTURE: GRATING METHODS

- DARK FIELD PAIR CORRELATION FUNCTION MEASUREMENTS HAVE POTENTIAL TO CONNECT THE NANOSCALE TO MACROSCALE IMAGING
- OPENS NEW POSSIBILITIES IN STUDYING POROUS MEDIA

### FUTURE: NEUTRON MICROSCOPY

- COULD ACHIEVE 1 MM RESOLUTION WITH [20 MIN EXPOSURES — QUICK FOR NEUTRONS AND 100X FASTER THAN CURRENTLY ACHIEVABLE]

THANK YOU!!



## **Tutorial 3**

**(15:05 – 15:50)**

# **Introduction to phase imaging principles & potential applications**

**Franz Pfeiffer**

*Technische Universität München,*

*Germany*



## Introduction to Phase Imaging Principles & Potential Applications

Prof. Dr. rer. nat. Franz Pfeiffer

Munich School of Bioengineering  
Faculty of Physics & Medicine  
Technical University Munich

Sendai, October 2019



## Basic Physics

Wave propagation, phase shift, complex index of refraction



## X-rays as Waves & Phase shift in vacuum

$$\Psi(\vec{r}, t) = \Psi_0 e^{i(\vec{k} \cdot \vec{r} - \omega t)}$$

$$\vec{k} = (0, 0, k = \frac{2\pi}{\lambda})$$

$$\Psi_v(\vec{r}, t) = \Psi_0 e^{i(\vec{k} \cdot \vec{r} - \omega t)} = \Psi_0 e^{i(kz - \omega t)}$$

$$\Psi_m(z, t) = \Psi_0 e^{i(nkz - \omega t)} = \Psi_0 e^{-i\omega t} e^{(1-\delta)ikz} e^{-\beta kz}$$

$$= \Psi_v(z, t) \cdot \underbrace{e^{-i\delta kz}}_{[\text{phase-shift}]} \cdot \underbrace{e^{-\beta kz}}_{[\text{attenuation}]}$$



## X-rays as Waves & Phase shift in a medium

$$\Psi(\vec{r}, t) = \Psi_0 e^{i(\vec{k} \cdot \vec{r} - \omega t)}$$

$$n = \underbrace{1 - \delta}_{[\text{elastic}]} + \underbrace{i\beta}_{[\text{inelastic}]}$$

$$\Delta\Phi$$

$$\Psi_m(z, t) = \Psi_0 e^{i(nkz - \omega t)} = \Psi_0 e^{-i\omega t} e^{(1-\delta)ikz} e^{-\beta kz}$$

$$\Psi_v(z, t) \cdot \underbrace{e^{-i\delta kz}}_{[\text{phase-shift}]} \cdot \underbrace{e^{-\beta kz}}_{[\text{attenuation}]}$$

L3-6



## X-rays as Waves & Phase shift

transmission & phase shift

$$T(d) = \frac{I_m(d)}{I_v(0)} = \frac{|\Psi_m(d, t)|^2}{|\Psi_v(0, t)|^2} = e^{-2k\beta d} \\ = e^{-\mu d} ; \quad \Delta\Phi = \delta kd$$

$$T(x, y) = e^{-2k \int \beta(x, y, z) dz}$$

$$\Delta\Phi(x, y) = k \int \delta(x, y, z) dz$$

$$\delta = \frac{r_0}{2\pi} \lambda^2 \rho_e = \frac{2\pi r_0 \hbar^2 c^2}{E^2} \rho_e .$$

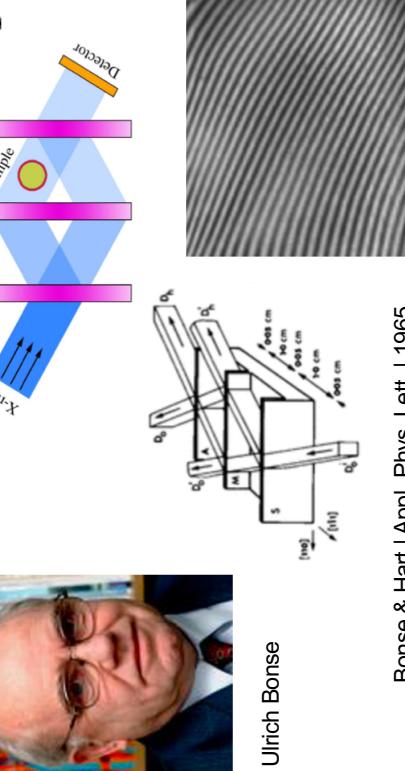
L3-7



## The 1960s

Crystal Interferometer Phase Contrast

Ulrich Bonse

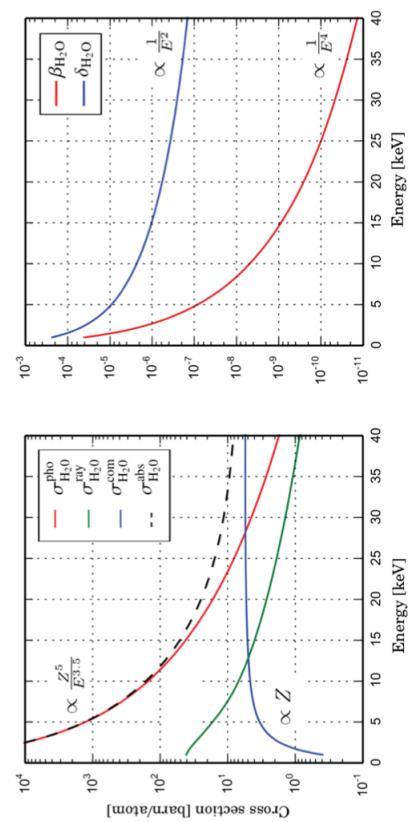


L3-6



## X-rays as Waves & Phase shift

cross sections & refractive index values for water



L3-8



## Crystal Interferometry

with perfect single-crystal silicon interferometers



Bonse & Hart | Appl. Phys. Lett. | 1965

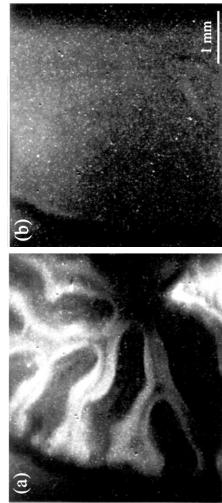
L3-9

L3-10



## Crystal Interferometry

with perfect single-crystal silicon interferometers



Momose et al  
Medical Physics | 1995



Momose et al  
Nature Medicine | 1996



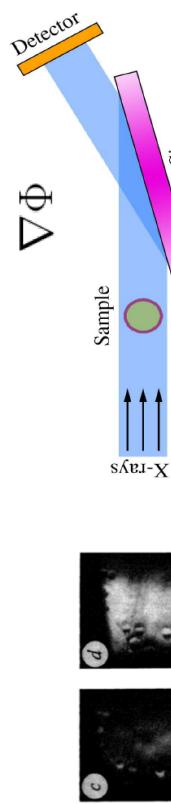
## The 1990s

Analyzer- and Propagation-Based Phase Contrast



## Analyzer-Based Phase-Contrast Imaging (ABI)

a.k.a. Diffraction-Enhanced Imaging (DEI)



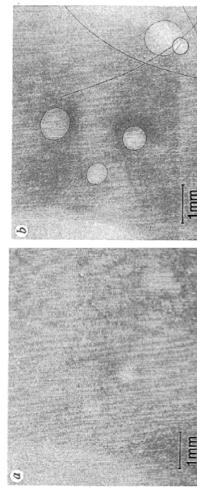
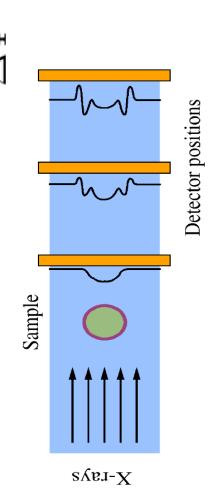
Davis et al | Nature | 1995  
Ingal & Beliaevskaya | J. Physics D | 1995

Wilkins et al | Nature | 1996



## Propagation-Based Phase-Contrast Imaging

uses Fresnel nearfield diffraction



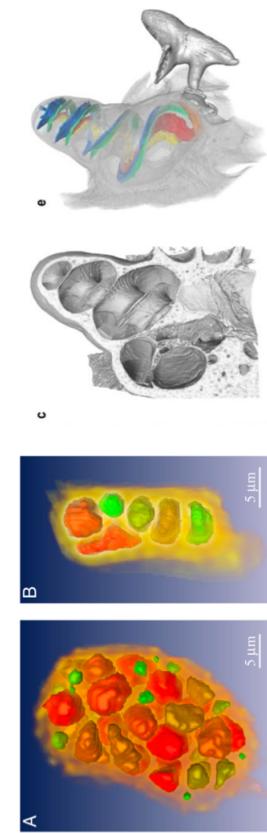
Snigirev et al | RSI | 1995  
Wilkins et al | Nature | 1996

L3-13

### Propagation-Based Phase-Contrast Imaging

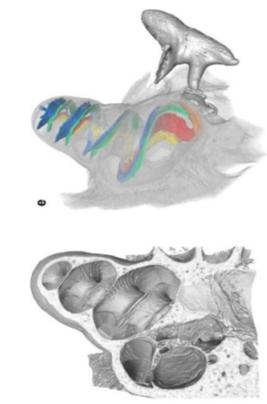
de facto standard @ synchrotron sources

Big synchrotrons (ESRF)



Cloetens et al | PNAS | 2007

Compact synchrotrons (MuCLS)



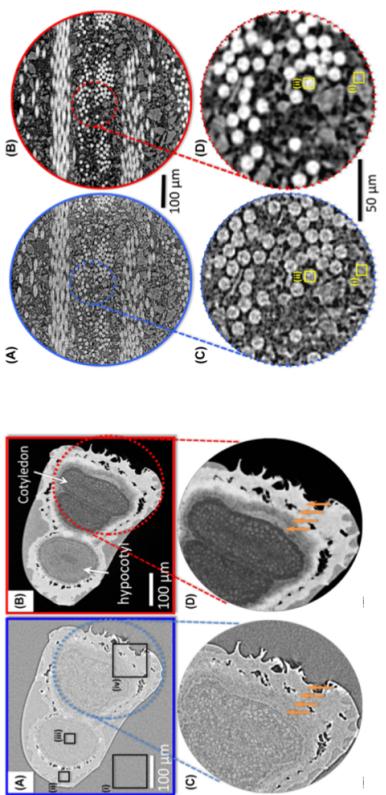
Toppervien et al | Sci Rep | 2018

L3-14

### Propagation-Based Phase-Contrast Imaging

works also with high-resolution microfocus lab sources

Microfocus lab sources (Zeiss Xradia Versa 520)



Biddola et al | Journal of Microscopy | 2017

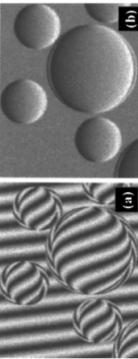
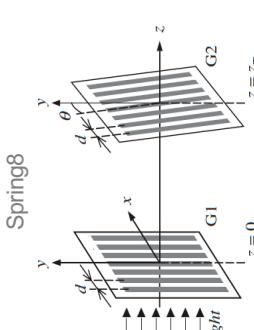
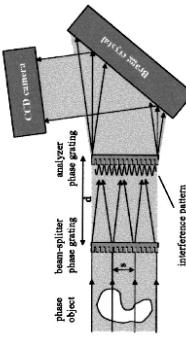
L3-15

L3-16

### Grating-Based X-Ray Phase Contrast

pioneering works at synchrotron sources

$\nabla \Phi$



David et al | Appl Phys Lett | 2002



Momose et al | JAP | 2003

L3-15

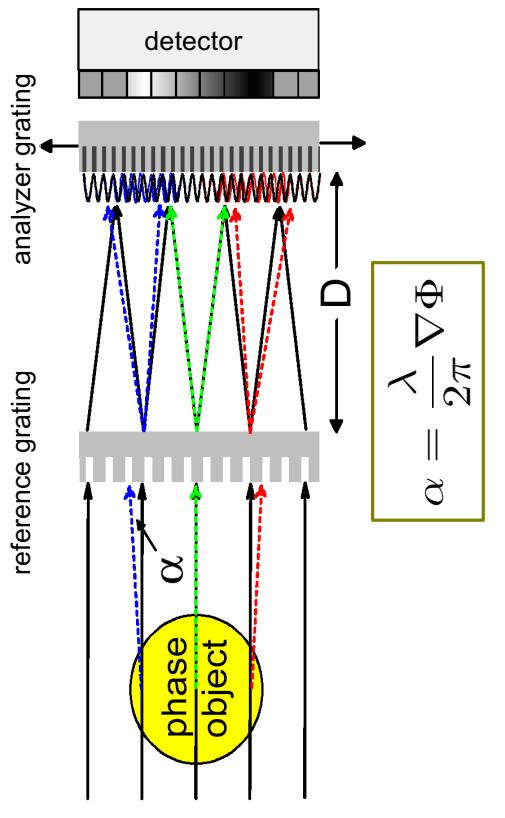


Early 2000s – Teenage Years

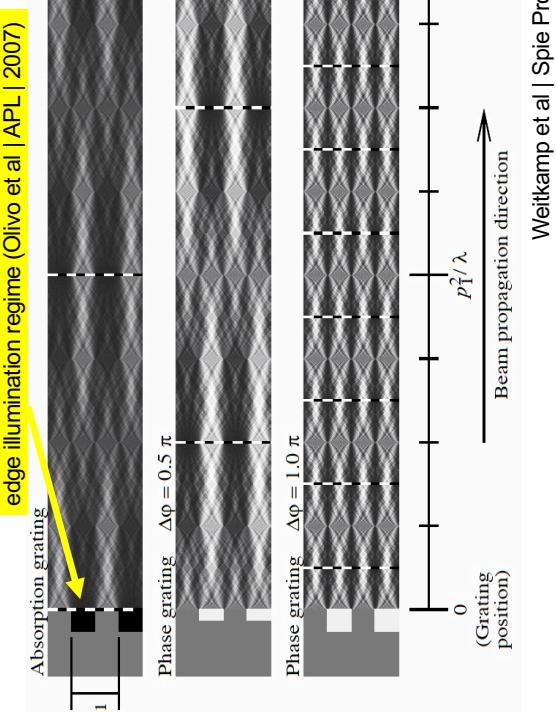
Grating-Based Phase Contrast @ Synchrotron Sources

## Grating-Based X-Ray Phase Contrast

measures refraction of X-ray waves in the object

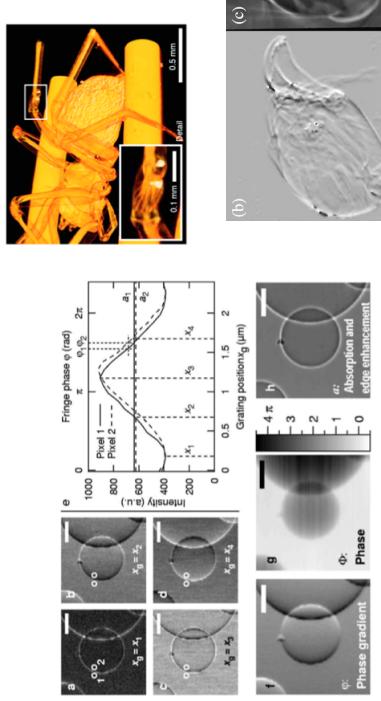


## Talbot Effect



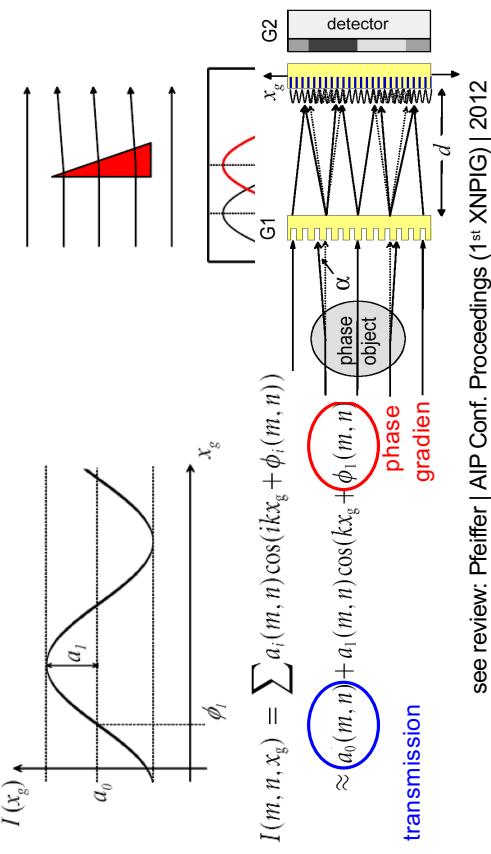
## Grating-Based X-Ray Phase Contrast CT

phase-stepping data processing and quantitative CT



## Quantitative Signal Extraction

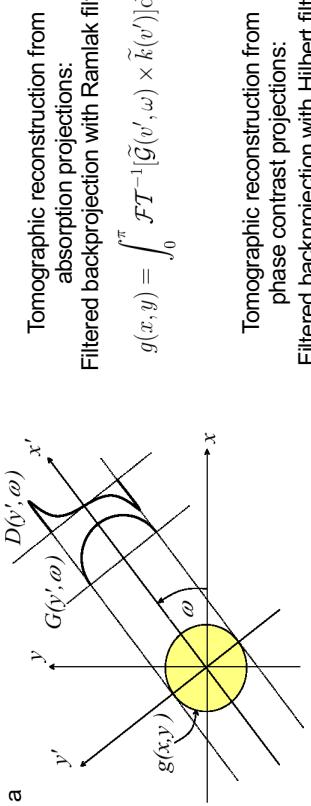
attenuation and differential phase contrast



L3-21

## Quantitative CT reconstruction

incorporating the integration into the filter kernel



Tomographic reconstruction from phase contrast projections:

$$g(x, y) = \int_0^\pi \mathcal{F}^{-1}[\tilde{\mathcal{D}}(v', \omega) \times \tilde{h}(v')] d\omega$$

Pfeiffer et al | Phys. Rev. Lett. | 2007

L3-22

## Review paper on Grating-Based Imaging



## AIP | Conference Proceedings

**Milestones and basic principles of grating-based x-ray and neutron phase-contrast imaging**

Franz Pfeiffer

Citation: AIP Conf. Proc. 1466, 2 (2012); doi: 10.1063/1.4742261

View online: <http://dx.doi.org/10.1063/1.4742261>

L3-23

## Late 2000s

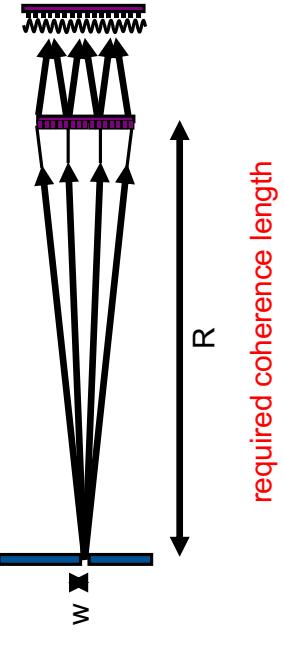
Translation to medical x-ray tubes & discovery of grating-based darkfield contrast

L3-24

## TUM

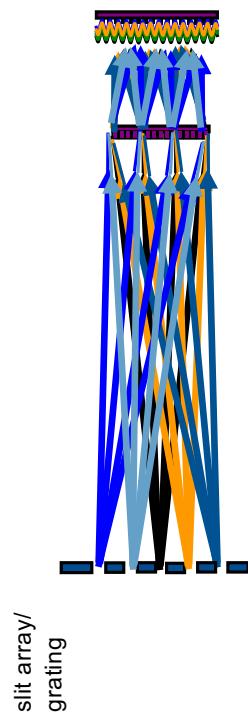
## From Synchrotrons to Medical X-ray Tubes

single slit





## From Synchrotrons to Medical X-ray Tubes



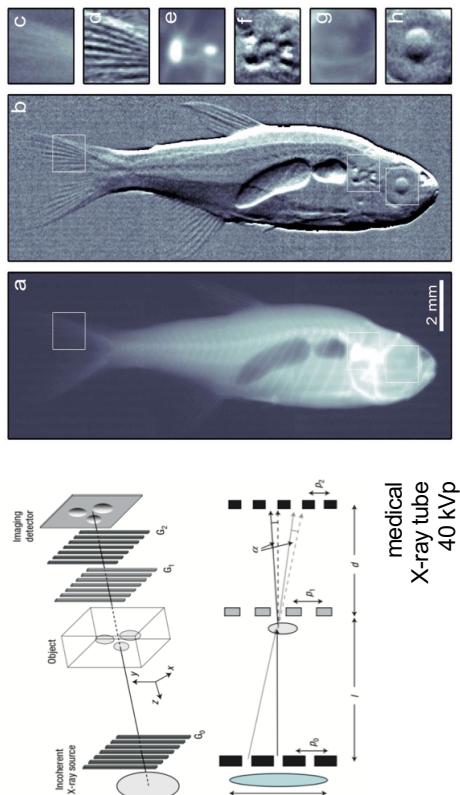
Decouples coherence from spatial resolution!

Pfeiffer et al. | Nature Physics | 2006



## Talbot-Lau Grating-Based X-Ray Phase Contrast

works also with medical X-ray tubes & incoherent sources



Pfeiffer et al. | Nature Physics | 2006



## Talbot-Lau Grating-Based X-Ray Phase Contrast

works also with medical X-ray tubes & incoherent sources

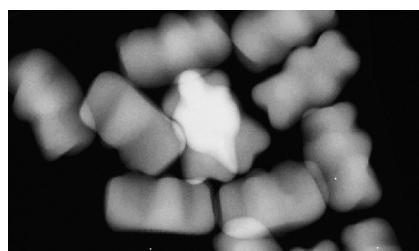
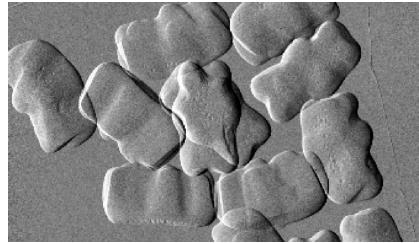


Pfeiffer et al. | Nature Physics | 2006



## X-Ray Phase Contrast

...more examples



phase contrast

Pfeiffer et al. | Nature Physics | 2006

medical  
X-ray tube  
40 kVp

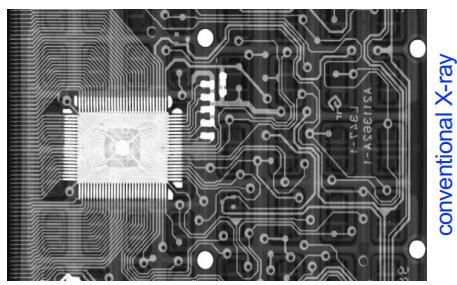
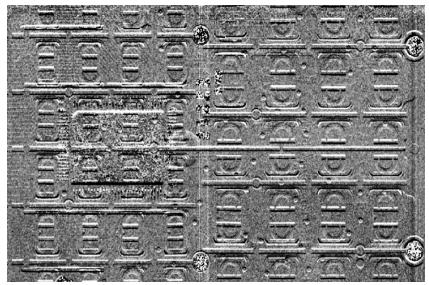
conventional X-ray

L3-30



## X-Ray Phase Contrast

...more examples



phase contrast

Pfeiffer et al. | Nature Physics | 2006

L3-29



## Discovery of Grating-Based Darkfield Imaging

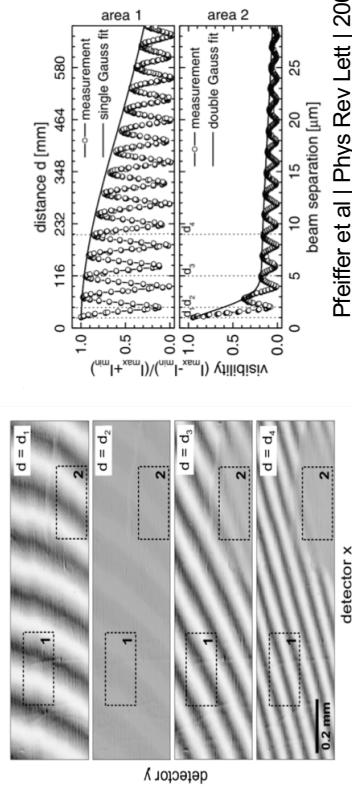
triggered by SR research on coherent diffraction

PRL 94, 164801 (2005)

week ending  
29 APRIL 2005

### Shearing Interferometer for Quantifying the Coherence of Hard X-Ray Beams

F. Pfeiffer, O. Bunk, C. Schulze-Briese, A. Diaz, T. Weitkamp, C. David, and J. F. van der Veen  
Paul Scherrer Institut, CH-5232 Villigen, Switzerland

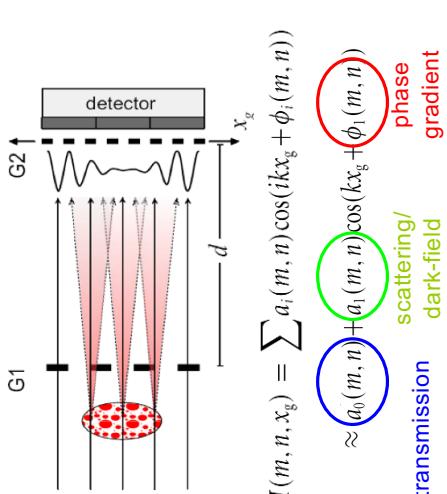


Pfeiffer et al. | Phys Rev Lett | 2005

L3-31



## Discovery of Grating-Based Darkfield Imaging



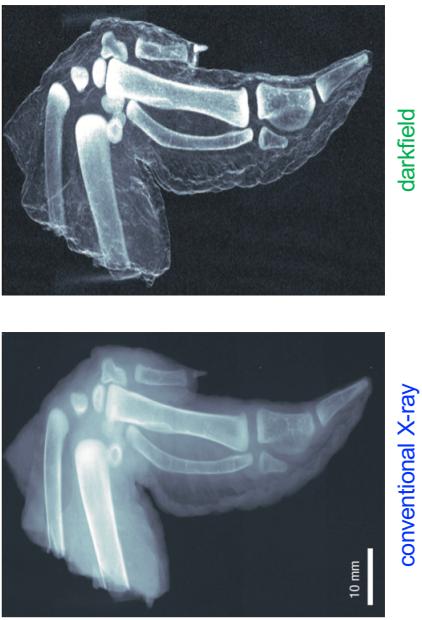
Pfeiffer et al. | Nature Materials | 2006

L3-32



## Darkfield Contrast

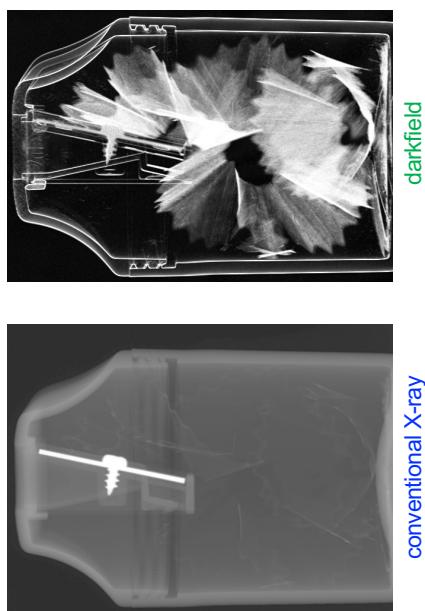
is sensitive to micro-structures in the object



Pfeiffer et al. | Nature Materials | 2008

## Darkfield Contrast

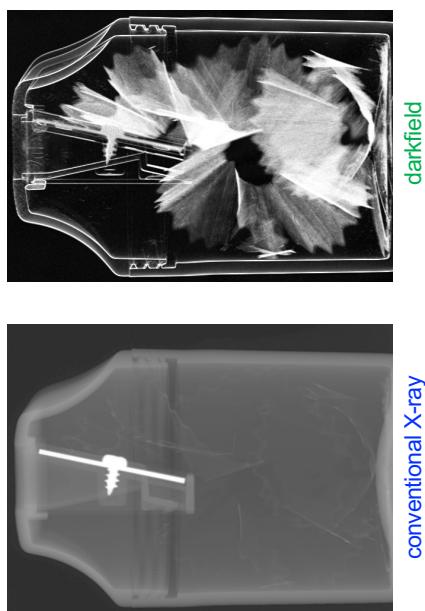
is sensitive to micro-structures in the object



Pfeiffer et al. | Nature Materials | 2008

## Darkfield Contrast

...is sensitive to micro-structures in the object

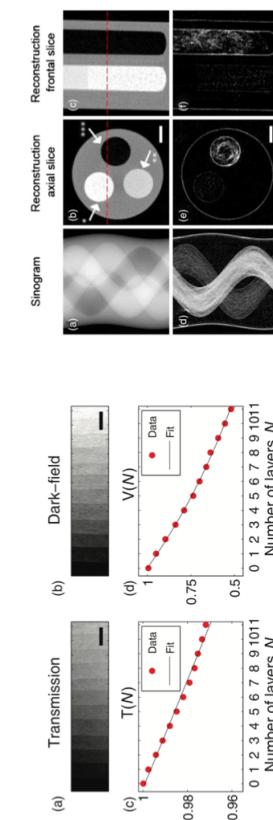


Pfeiffer et al. | Nature Materials | 2008

## Understanding the Darkfield-Signal

introduction of „linear diffusion coefficient“ / „darkfield extinction coefficient“

$$\epsilon \equiv \frac{\sigma^2}{\Delta z} \quad V(m, n) = \exp \left( \frac{-2\pi d^2}{p_z^2} \int \epsilon_{m, n}(z) dz \right)$$

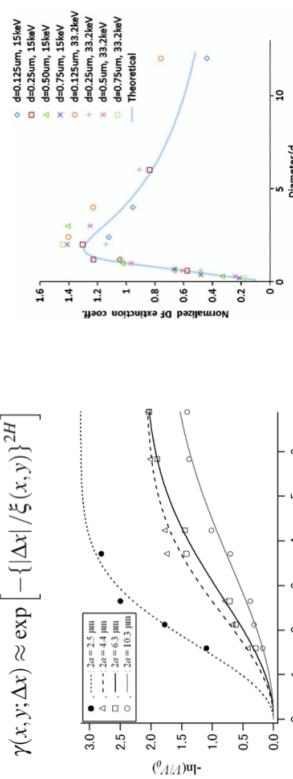


Bech et al. | Phys Med Biol | 2010

## Understanding the Darkfield-Signal

establishing relationship to correlation length

$$\frac{V}{V_0} \approx \frac{\exp[i\Delta\Phi_l(x, y; pd)]}{\exp[-\sigma^2(x, y)\{1 - \gamma(x, y; -pd)\}]}, \quad \mu_d = \frac{3\pi^2}{l^2} f/\lambda l^2 d \begin{cases} \frac{D - \sqrt{D^2 - 1}(1 + D^{-2})/2 + (D^{-1} - D^{-3}/4)}{D}, & \text{for } D > d; \\ \frac{\ln(D + \sqrt{D^2 - 1})/(D - \sqrt{D^2 - 1})}{D}, & \text{for } D \leq d; \end{cases}$$

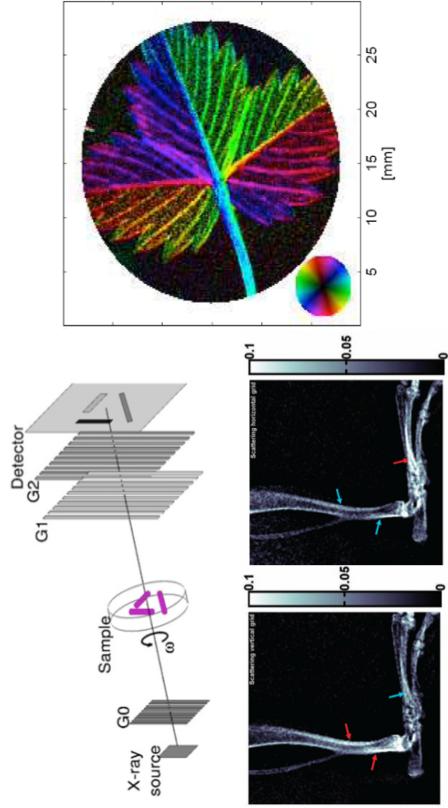


Yashiro et al. | Optics Express | 2010 & Lynch et al. | Optics Express | 2011



## Darkfield Vector Radiography

exploiting directional dependence

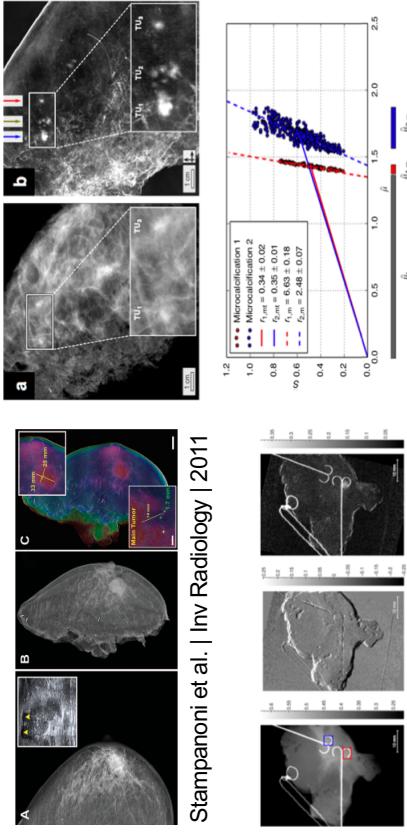


L3-39



## Ex-vivo tissue imaging

exploring the potential medical impact – mammography



L3-40



see talks in  
Session II

## Ex-vivo tissue imaging

exploring the potential medical impact – musculoskeletal imaging



L3-41



## Ex-vivo specimen imaging

assess potential medical applications

Early 2010s

Ex-vivo specimen imaging to assess potential medical applications

L3-41



## Ex-vivo tissue imaging

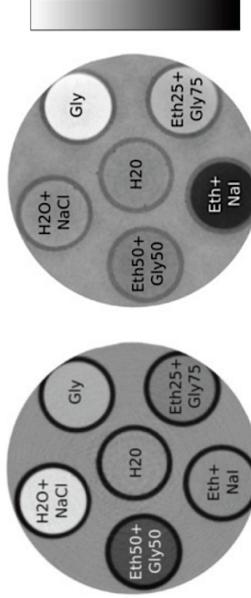
assess potential medical applications

## Quantitative phase CT

'conventional'  
**phase-contrast'**



Hounsfield Units

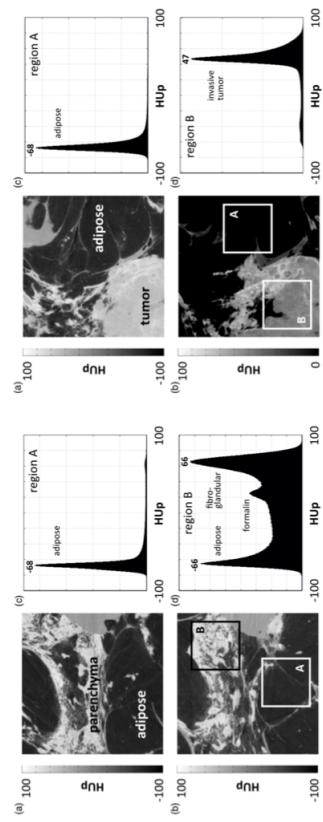


$$\frac{\mu - \mu_{water}}{\mu_{water} - \mu_{air}}$$

Tapfer et al | Med Phys | 2011 [see also before: Herzen et al | Opt Express | 2009]

## Ex-vivo tissue imaging

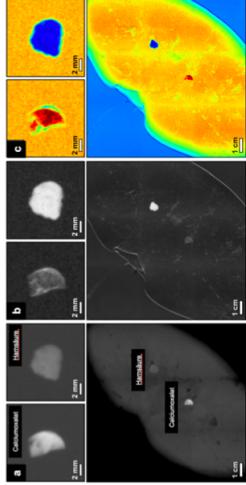
exploring the potential medical impact – **breast CT**



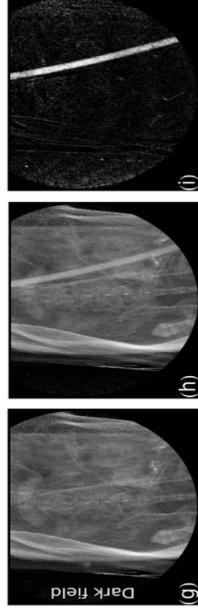
Willner et al | Phys Med Biol | 2013; Grandl et al | ZMP | 2013  
Grandl et al | PlosOne | 2014; Grandl et al | Eur Rad | 2015

## Ex-vivo tissue imaging

exploring the potential medical impact – **stone classification & CAs**



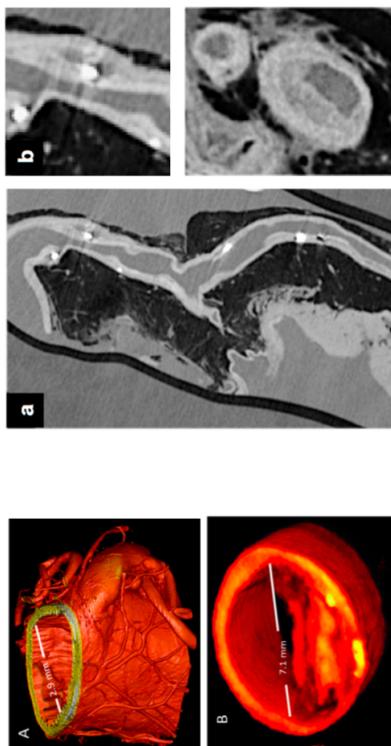
Scherer et al.  
Scientific Reports | 2015



Velroyen et al | 2015  
PlosOne | 2015

## Ex-vivo tissue imaging

exploring the potential medical impact – **cardiovascular CT**



Hettich et al | Radiology | 2014  
Hettich et al | Inv Radiology | 2015

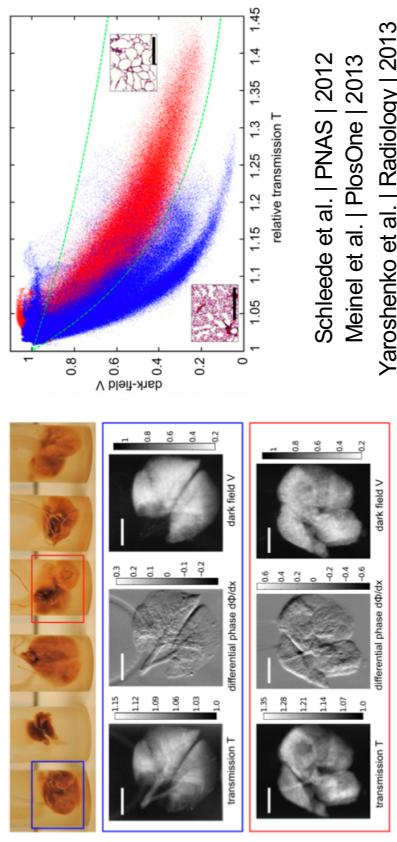
Saam et al.  
PlosOne | 2013

L3-46



## Ex-vivo tissue imaging

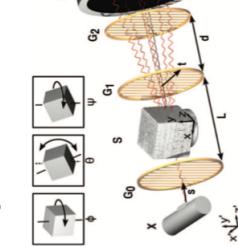
exploring the potential medical impact – lung diseases



L3-47

## Darkfield Tensor CT

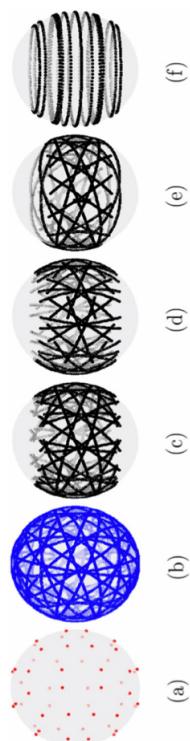
solving the 6D tensorial scattering reconstruction problem



$$D(x, y) = \exp \left[ - \int \sum_i (|\epsilon_i(x, y, z)| |t|)^2 \cdot (|\hat{s} \times \hat{\epsilon}_i| (\hat{\epsilon}_i, \hat{t}))^2 dz \right].$$

Malecki et al. | Eur Phys Lett | 2014  
Sharma et al. | Appl Phys Lett | 2016  
Sharma et al. | Scientific Reports | 2017

$$\dots$$

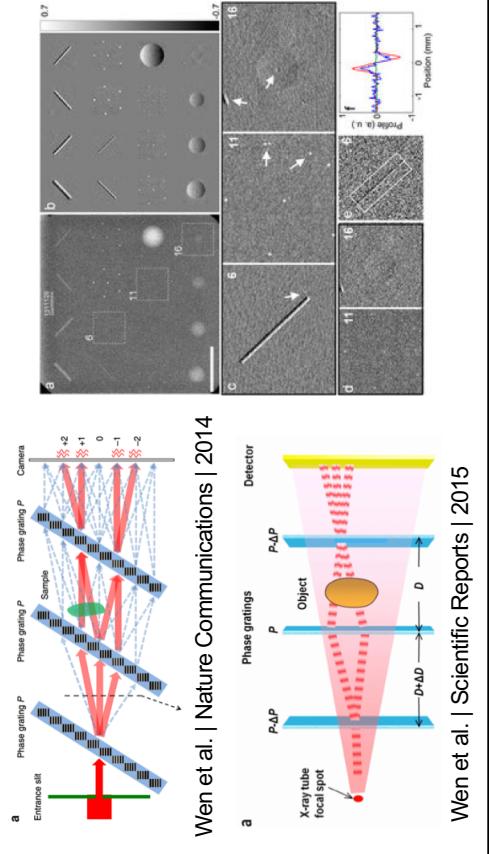


L3-46

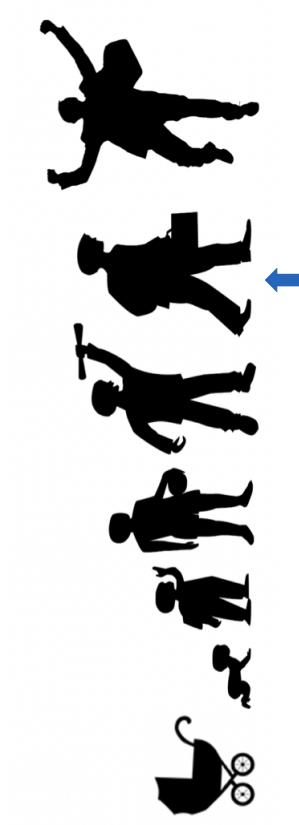


## High-sensitivity Farfield Interferometry

with submicron-period phase gratings



L3-48



## Late 2010s – Adulthood

Translation to Pre-Clinical Small-Animal Imaging & Research



## First Step: Mouse-CT

first phase-contrast small-animal CT

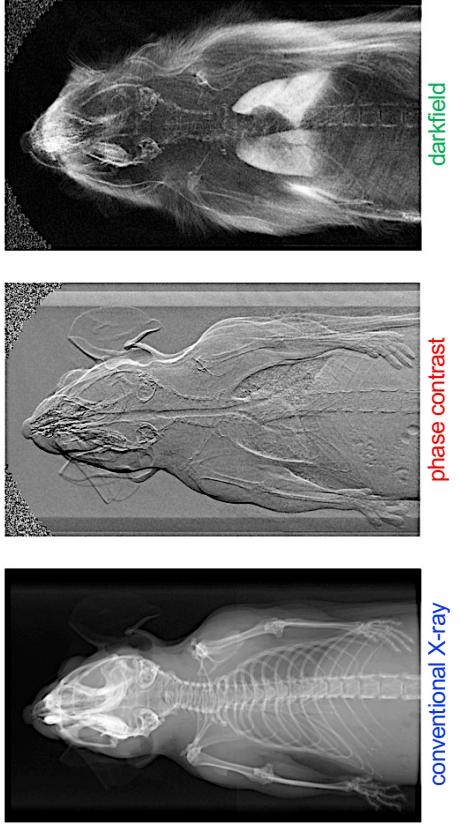


Tapfer et al | Med. Phys. | 2011; Tapfer et al | PNAS | 2012



## First Step: Mouse-CT

first phase-contrast small-animal CT

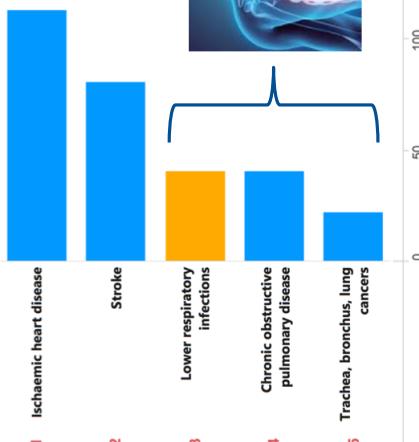


Bech et al | Nature Sci. Rep. | 2013



## Medical Relevance

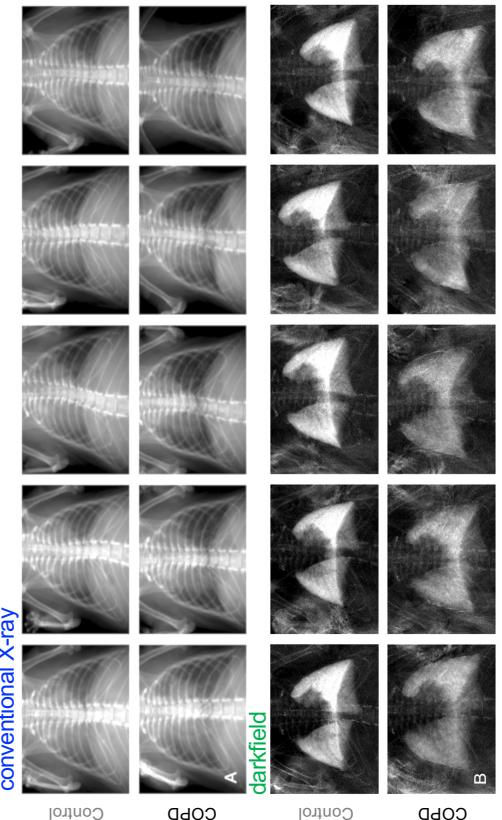
for lung diseases



L3-54



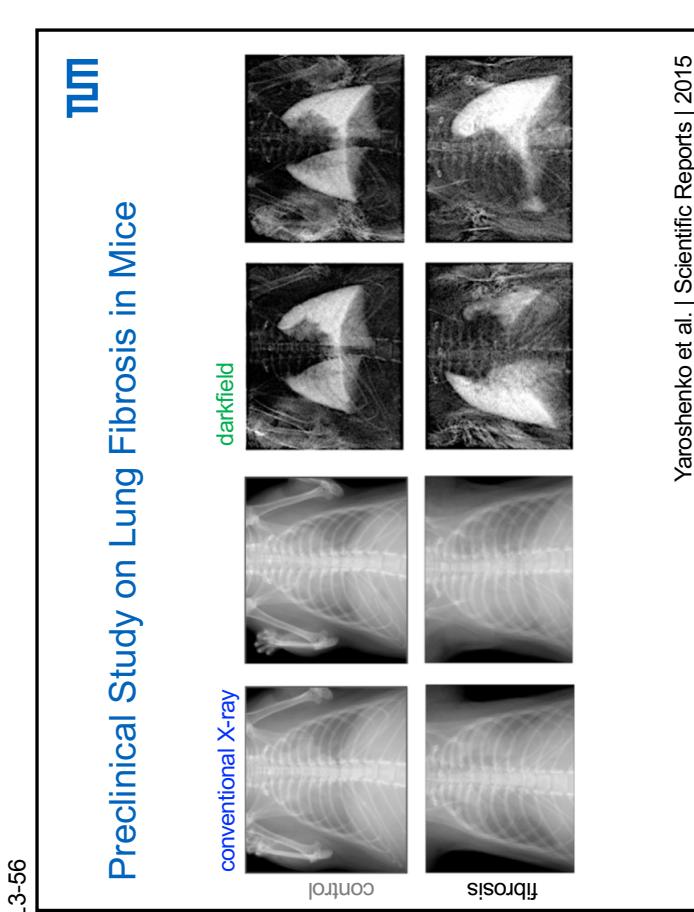
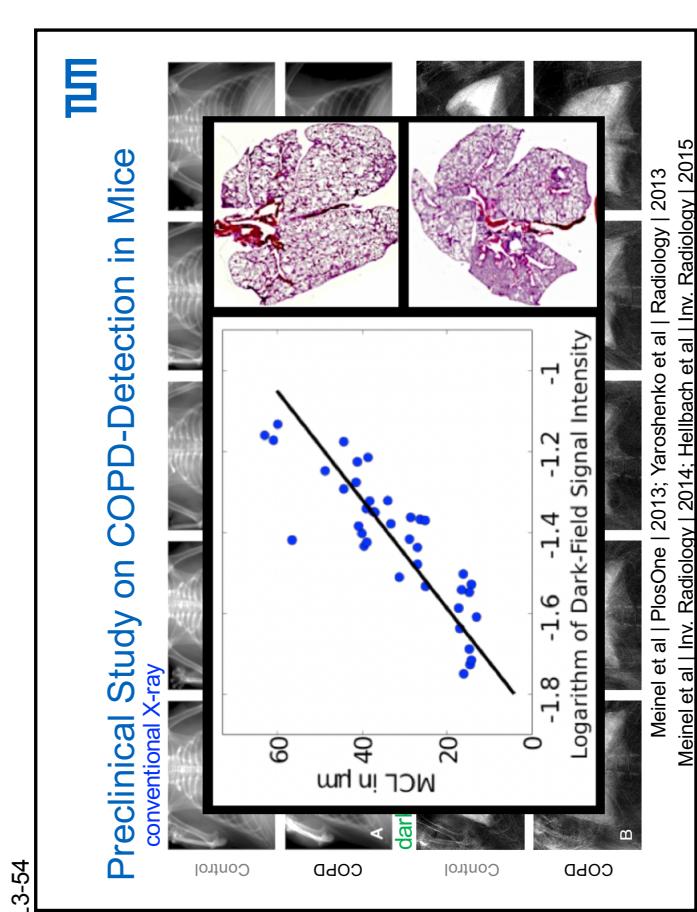
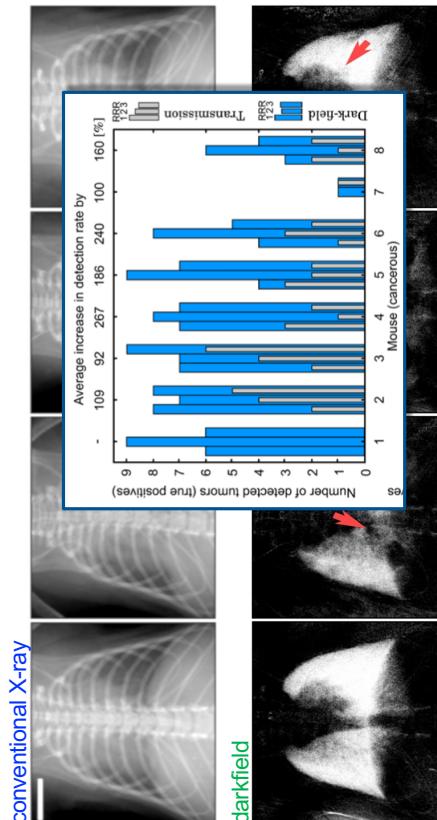
### Preclinical Study on COPD-Detection in Mice



L3-55



### Preclinical Study on Lung Cancer in Mice



L3-57



## First In-Vivo Multi-Contrast X-Ray CT



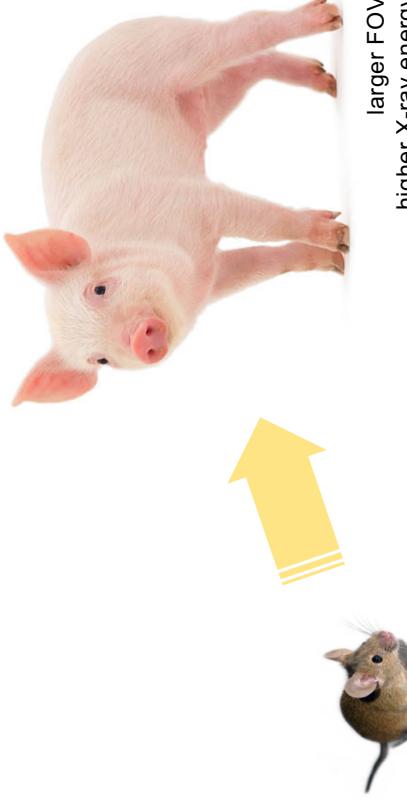
[www.youtube.com/watch?v=WeiADQ0h3B4](http://www.youtube.com/watch?v=WeiADQ0h3B4)

Velroyen et al. | EBiomedicine | 2015

L3-58



## Next Step: Darkfield "Pig-Scanner"



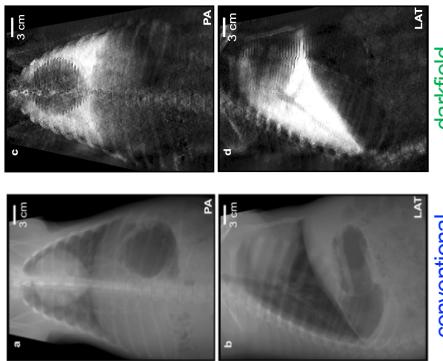
larger FOV  
higher X-ray energy

L3-59



## Darkfield Pig-Scanner

worldwide first in-vivo large-animal proof-of-principle



med. X-ray generator 70 kVp  
10 sec scan time  
dose 80  $\mu$ Sv

darkfield

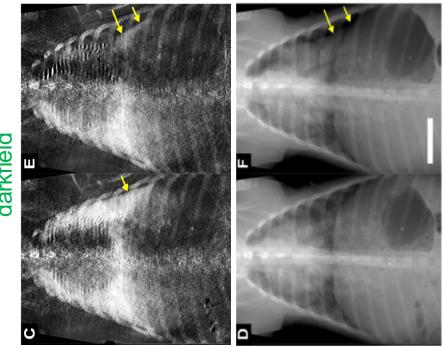
Gromann et al. | Scientific Reports | 2017

L3-60



## Darkfield Pig-Scanner

improved pneumothorax detection demonstrated



med. X-ray generator 70 kVp  
10 sec scan time  
dose 80  $\mu$ Sv

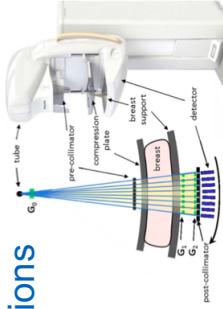
conventional

Hellbach et al. | Scientific Reports | 2018

L3-62



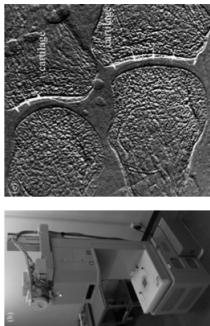
## Work Toward Patient Applications



Koehler et al. | J Med Phys | 2015



Li et al. | Proc SPIE | 2018



Tanaka et al. | ZMP | 2013



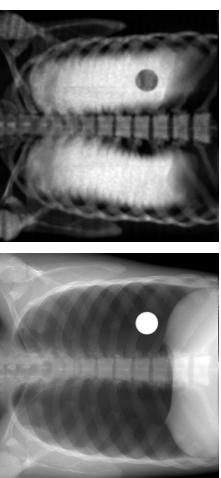
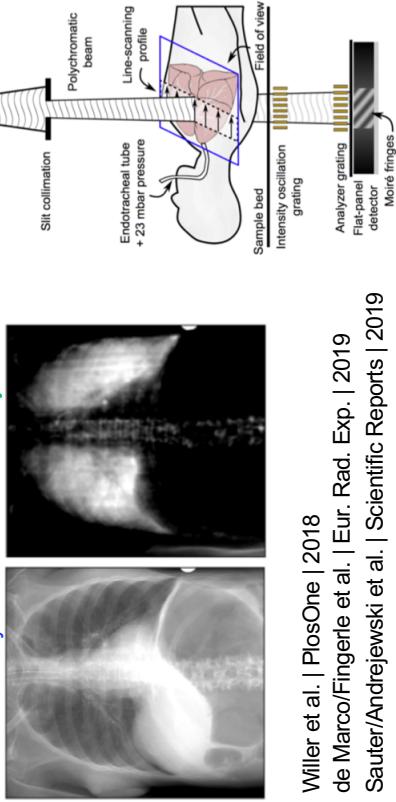
Hauke et al. | J Med Phys | 2018

L3-63



## First Darkfield Chest X-ray Prototype for Humans

extensive phantom studies

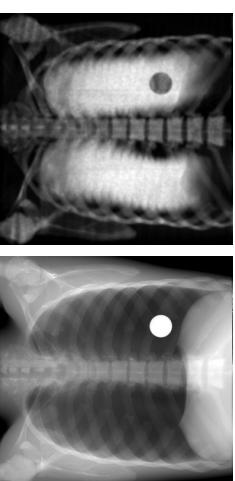
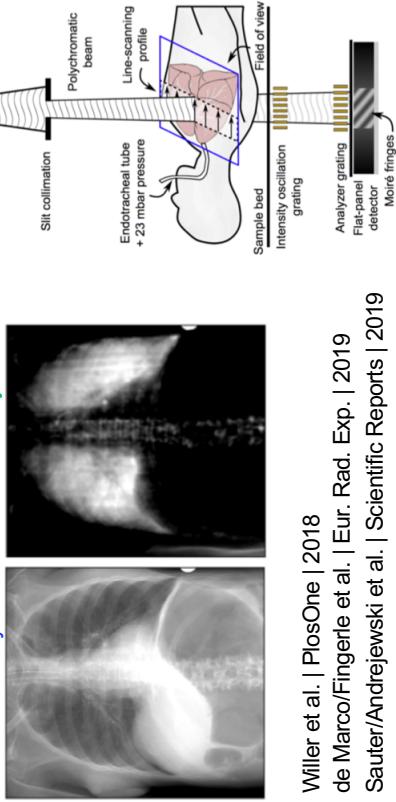
conventional  
chest X-raydarkfield  
chest X-ray

Willer et al. | PlosOne | 2018  
de Marco/Fingerle et al. | Eur. Rad. Exp. | 2019  
Sauter/Andrzejewski et al. | Scientific Reports | 2019

L3-64

## First Darkfield Chest X-ray Prototype for Humans

worldwide first ex-vivo darkfield human chest x-rays

conventional  
chest X-raydarkfield  
chest X-ray

Willer et al. | PlosOne | 2018  
de Marco/Fingerle et al. | Eur. Rad. Exp. | 2019  
Sauter/Andrzejewski et al. | Scientific Reports | 2019



See talks in  
Session I & IX  
...from prototype in Munich will be presented at this conference (tomorrow)

## First Results with Patients

...from prototype in Munich



COPD study > 500 Patienten

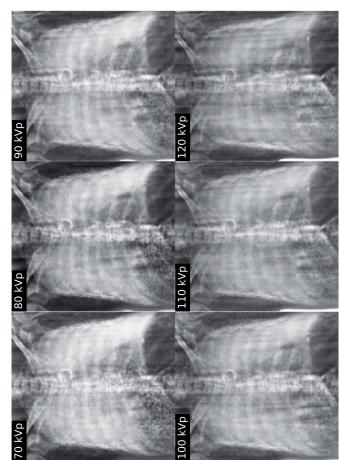


Bundesamt für Strahlenschutz

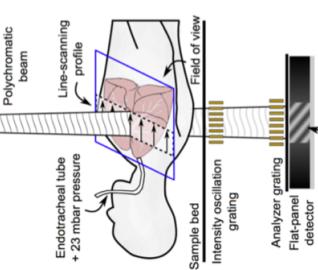


## First Darkfield Chest X-ray Prototype for Humans

Worldwide first ex-vivo darkfield human chest x-rays



Willer et al. | PlosOne | 2018  
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Sauter/Andrijewski et al. | Scientific Reports | 2019



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[www.e17.ph.tum.de](http://www.e17.ph.tum.de)



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Joachim Schulz, Tobias Schröter



Deutsche Forschungsgemeinschaft  
DFG



## **Tutorial 4**

**(15:50 – 16:20)**

# **Introduction to tomographic image reconstruction**

**Marco Stampanoni**

*Paul Scherrer Institut / Eidgenössische Technische  
Hochschule Zürich,  
Switzerland*

## Introduction to Tomographic Image Reconstruction

Marco Stampanoni

Institute for Biomedical Engineering, University and ETH Zurich  
Swiss Light Source, Paul Scherrer Institut

L4-3

### Contrast definition

$$\text{Definition: } C = \frac{I_1 - I_2}{I_2}$$

$$\begin{aligned} I_1 &= P_1 + S_1 & P_1 &= Ne^{-\mu_1 x} \times e^{\mu_2(T-x)} \\ I_2 &= P_2 + S_2 & P_2 &= Ne^{-\mu_2 T} \end{aligned}$$

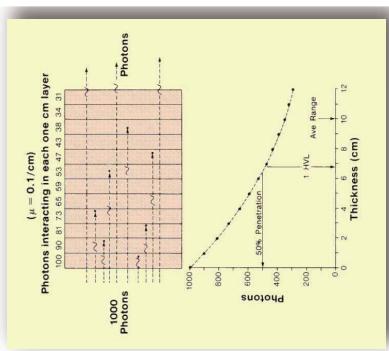
$$C = \frac{N(e^{-(\mu_1-\mu_2)x} e^{-\mu_2 T}) + S_1 - S_2}{Ne^{-\mu_2 T} + S_2}$$

Using  $e^{-x} \approx 1-x$  for small  $x$   
and assuming  $S_1 \approx S_2$  we can write:

$$C \approx \frac{(\mu_1 - \mu_2)x}{1+R} \quad \text{where } R \equiv \frac{S_2}{Ne^{-\mu_2 T}}$$

- Contrast maximized by increasing attenuation coefficient difference
- Small scatter contributes to higher contrast

## Beer-Lambert's law



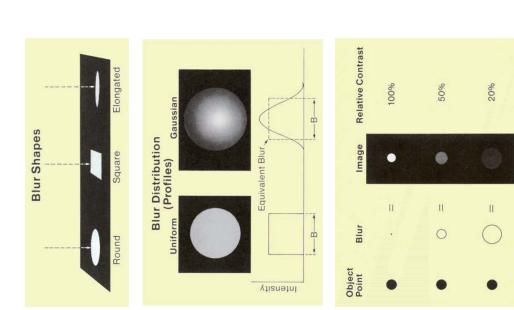
$$I = \int_0^{E_{\max}} I_0(E) \cdot e^{-\int_{-\infty}^E \mu(E, x) dx} dE$$

- "Photons do not have the same energy"
- "Some of the photons travel a relatively short distance before interacting, whereas others pass through or penetrate the object"

## Blur vs contrast

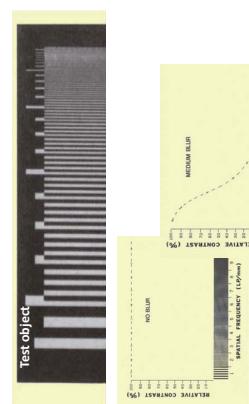
- Blurring is present in all imaging processes
- In an ideal situation, each small point within an object would be represented by a small, well-defined point within the image. In reality, the "image" of each object point is spread, or blurred, within the image.
- Blur has little effect on the visibility of large objects but it reduces the contrast and visibility of small objects.
- Relationship between spatial resolution and contrast!!!

L4-4



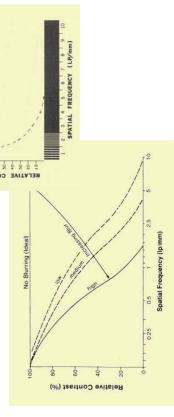
## Contrast Transfer Curves

- The resolving ability, or resolution, of an imaging system is relatively easy to measure and is often used to evaluate system blur.



- The common practice is to describe the line width and separation distance in terms of line pairs (lp) per unit distance (millimeters or centimeters). One line pair consists of one lead strip and one adjacent separation space.

- The number of line pairs per millimeter is actually an expression of spatial frequency. As the lines get smaller and closer together, the spatial frequency (line pairs per millimeter) increases.
- A typical test pattern contains areas with different spatial frequencies.



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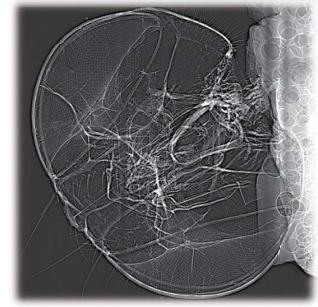
## Computed Tomography



## Tomoscopy

(gated tomography, kHz time resolution)

## Radiography



→ Computed tomography!

## Computed tomography: from 2D to 3D



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## 2D - 3D - 4D

## Computed tomography: from 2D to 3D



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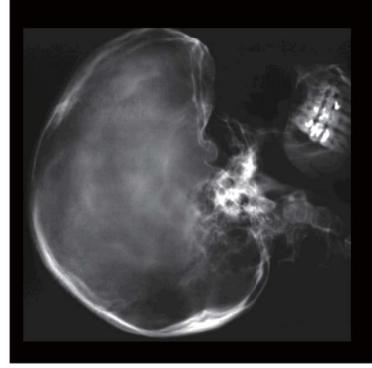
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## Slicing Imaging – Why ?

- Tomography means imaging by sections or slices.

(From the Greek word tomos, meaning "a section" or "a cutting")



Radiographic projection

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## Beer-Lambert law

- Homogeneous object, monochromatic radiation

$$I = \int_0^{E_{max}} I_0(E) \cdot e^{-\int_0^E \mu(E') dE'} dE$$

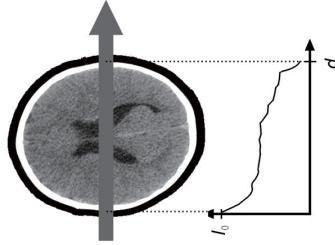
object dependence  
energy dependence

$$I = I_0 \cdot e^{-\mu d}$$

$$P = \ln \frac{I_0}{I} = \mu d$$

$$\mu = \frac{P}{d} = \frac{1}{d} \ln \frac{I_0}{I}$$

$\mu$  = linear attenuation coefficient  
 $\mu = (\tau + \sigma + \kappa)$



## Beer-Lambert law

- Inhomogeneous object, polychromatic radiation

$$I = \int_0^{E_{max}} I_0(E) \cdot e^{-\int_0^E \mu(E') dE'} dE$$

object dependence  
energy dependence

$$I = \int_0^{E_{max}} I_0(E) \cdot e^{-\int_0^E \mu(E') dE'} dE$$

$$\mu(z) = ?$$

$$P = \ln \frac{I_0}{I} = \int_0^d \mu(z) dz$$

Radon Transform, i.e. integral of a function over a (straight) line...

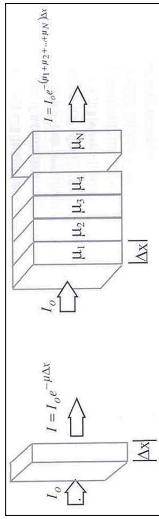
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**Beer-Lambert law**

- Arbitrary Object:



- It holds:  $I = I_0 e^{-\mu_1 \Delta x} e^{-\mu_2 \Delta x} e^{-\mu_3 \Delta x} \dots e^{-\mu_N \Delta x} = I_0 e^{-\sum_{n=1}^N \mu_n \Delta x}$  ?
- Define the projection measurement:  $p = \ln \left( \frac{I_0}{I} \right) = \sum_{n=1}^N \mu_n \Delta x = \int_L \mu(x) dx$

The question is:

Given the (1D) measured projections, corresponding to the line integrals of the attenuation coefficient, how do we reconstruct its (2D) distribution?

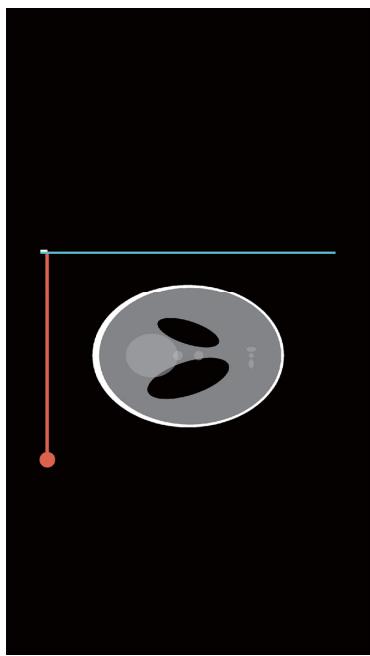
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L4-14

ETH Zürich

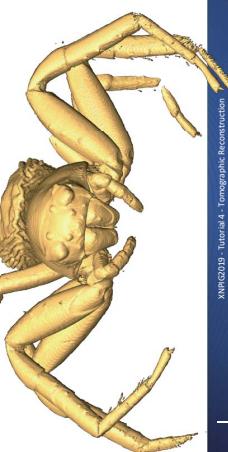
**Projection data: demonstration**

<https://youtu.be/TbLaQo3gEE>

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L4-15

ETH Zürich

**Computed tomography: from 2D to 3D**

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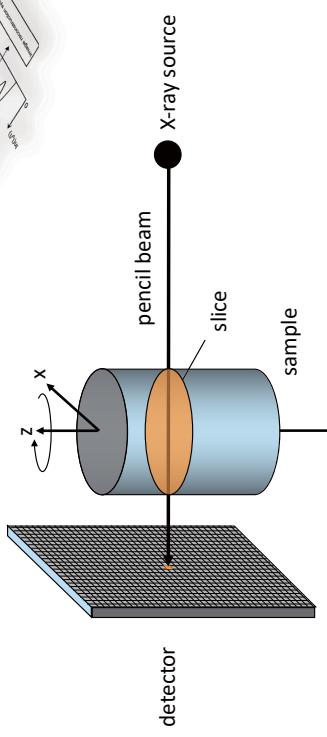
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L4-16

ETH Zürich

**Acquisition schemes: point detector**

- Simplest beam geometry
- Integrating one detector pixel at a time



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L4-16

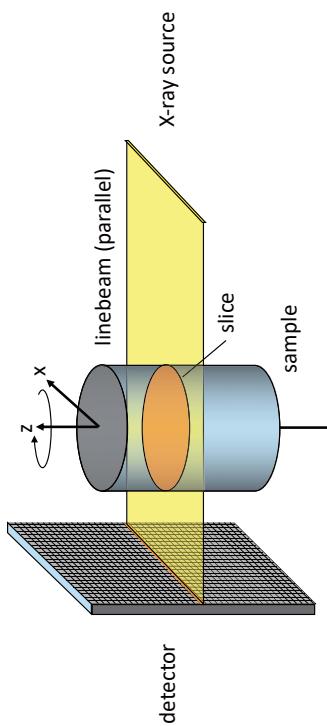
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## Acquisition schemes: line geometry

- Integrating a row of detector pixels at a time ( $\rightarrow$  faster scans)



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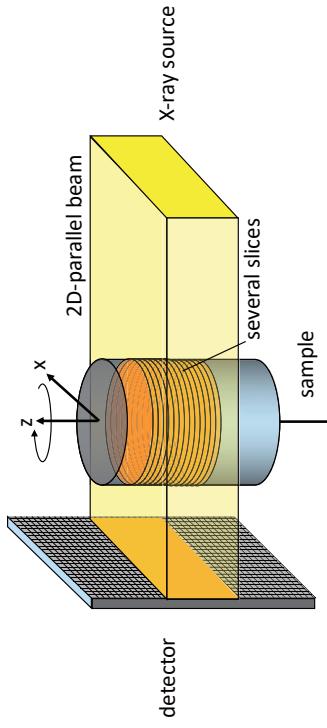
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## Acquisition schemes: parallel beam geometry

- Integrating a 2D array of pixels at a time, very fast
- Simple reconstruction algorithm



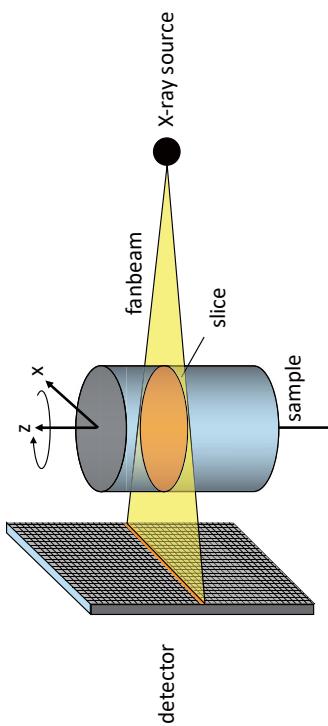
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## Acquisition schemes: fan-beam geometry

- Integrating a row of pixels at a time
- Magnification effect by fan geometry



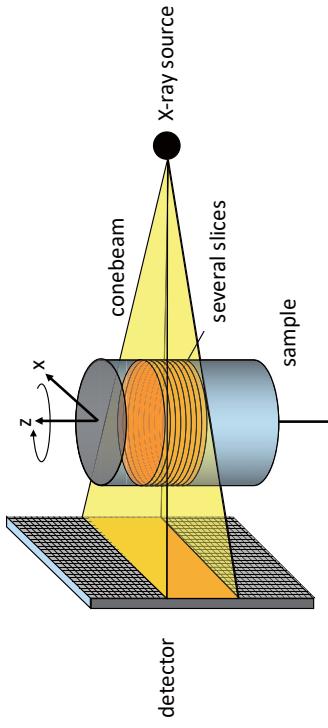
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## Acquisition schemes: cone-beam geometry

- Integrating a 2D array of pixels at a time
- Magnification effect by cone geometry
- Reconstruction is non-trivial, since beam travels through different slices



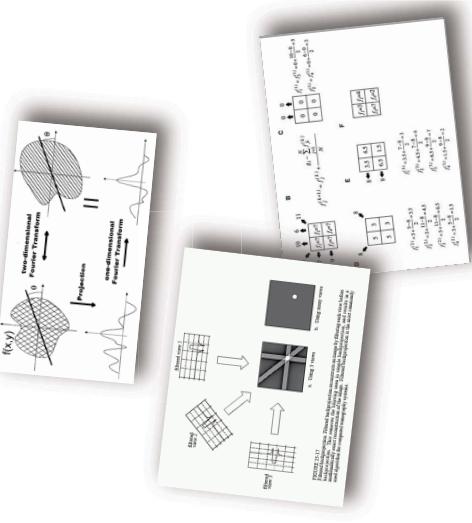
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## Tomographic reconstruction algorithms

- Fundamental Tools:
  - Radon Transform
  - Fourier Slice Theorem



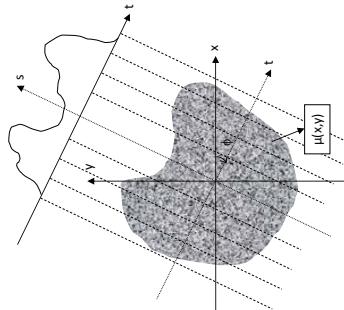
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## Radon transform

- The Radon transform in 2D is the integral of a function over straight lines and therefore represents the projections data as obtained in a tomographic scan



$$R(t, \phi) = \int \mu(x, y) dl$$

$$R(t, \phi) = P_\phi(t) := -\ln\left(\frac{I_\phi(t)}{I_0}\right)$$

$$R(t, \phi) = \int_{-\infty}^{+\infty} \mu(x, y) \delta(x \cos \phi + y \sin \phi - t) dx dy$$

Wanted!

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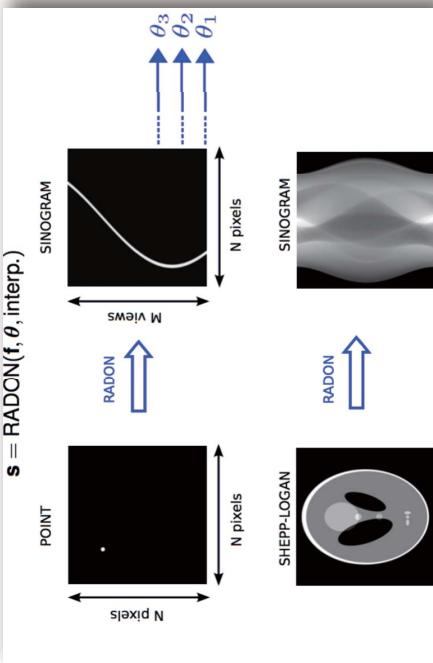
## Direct inversion (historic)

- Brute force approach
  - N equations with N unknowns
  - Need more than  $N^2$  equations to ensure linear independence
- 
- Sir Godfrey Hounsfield (in the late 60s)
  - Reconstructed the first human head
  - Solved 280000 equations simultaneously
  - Nobel Prize in 1979 together with A. Cormack

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## Radon Transform aka "sinogram"

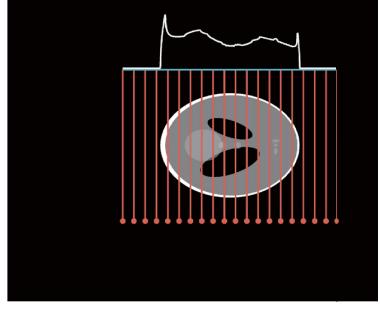


The Radon transform is often called a sinogram because the Radon transform of a Dirac delta function corresponds to the graph of a sine wave

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## Sinogram formation: demonstration



<https://youtu.be/5Vyc1TzmNl8>

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L4-26

## Radon transform

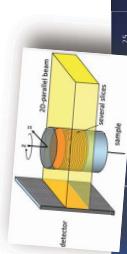
- The Radon transform was introduced by Johann Radon, who also provided a formula for the inverse transform
- The inverse of the Radon transform can be used to reconstruct the original density from the projection data, and thus it forms the mathematical underpinning for tomographic reconstruction
- Radon found the solution to the tomographic problem already in 1917
  - but assumed an infinite number of projections and continuous projection functions
  - while we only have a finite number of projections and a finite number of detector points



$$R(t, \phi) = \int_{-\infty}^{+\infty} \mu(x, y) \delta(x \cos \phi + y \sin \phi - t) dx dy$$

Wanted !

L4-27

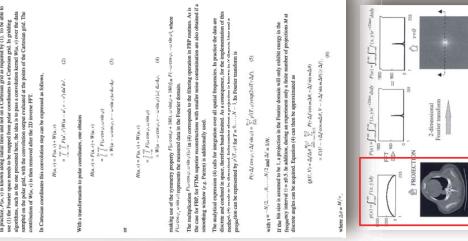
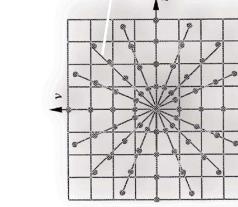


L4-28

L4-28

## Direct Fourier Method

- Algorithm:
  - 1D FFT of the projections
  - Filtering
  - Resampling
  - 2D inverse FFT
- Resampling issues:
  - Interpolation
  - Limited accuracy
  - (Re-)Bridging
- Most accurate Fourier reconstruction method
- Mapping by convolution with FFT of  $w(x, y)$
- Gridrec
- W(x): 1D Prolate Spheroidal Wave Functions (PSWF) of zeroth order
- $W(x, y)$ : maximally concentrated in square region of interest
- $\text{FFT}(w(x, y))$ : concentrated as much as possible around 0
- PSWF: calculated using rapidly converging expansion in terms of Legendre polynomials
- PSWF and FFT (PSWF) can be efficiently computed and stored at run time



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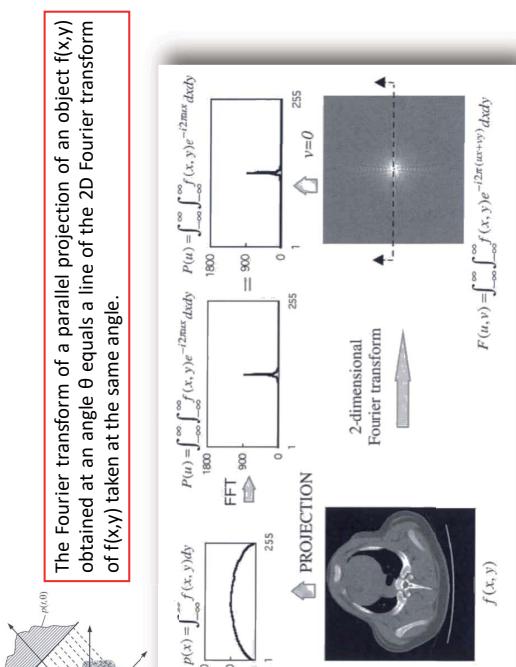
L4-29

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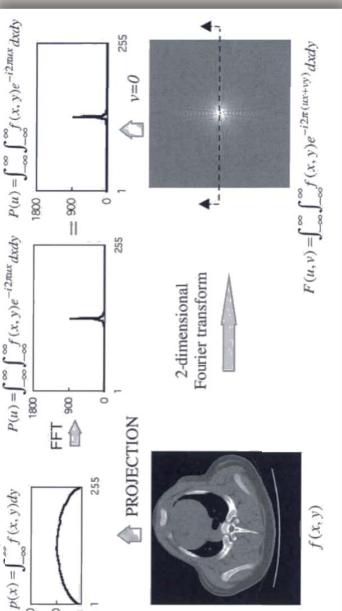
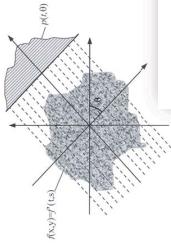
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L4-29

## Fourier Slice Theorem



The Fourier transform of a parallel projection of an object  $f(x, y)$  obtained at an angle  $\theta$  equals a line of the 2D Fourier transform of  $f(x, y)$  taken at the same angle.



$f(x, y)$

$F(u, v) = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} f(x, y) e^{-j2\pi u x} e^{-j2\pi v y} dx dy$

L4-30

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## Filtered backprojection (mathematical background)

$$-\ln \left( \frac{I_\phi(r)}{I_0} \right) := P_\phi(r) = R(t, \phi) = \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} \mu(x, y) \delta(x \cos \phi + y \sin \phi - t) dx dy$$

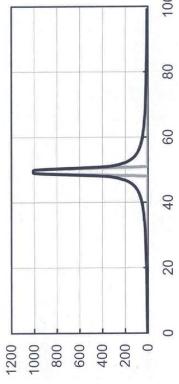
$$\text{Image function: } \mu(x, y) = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \tilde{M}(u, v) e^{j2\pi(u \cos \theta + v \sin \theta)} du dv$$

Coordinate transform:  
(cartesian to polar)

$$\mu(x, y) = \int_0^{2\pi} \int_0^{\infty} \tilde{M}(\omega \cos \theta, \omega \sin \theta) e^{j2\pi(\omega \cos \theta + y \sin \theta)} d\theta d\omega$$

with  $\begin{cases} u = \omega \cos \theta \\ v = \omega \sin \theta \end{cases}$  and  $g = \begin{pmatrix} \frac{\partial u}{\partial \omega} & \frac{\partial u}{\partial \theta} \\ \frac{\partial v}{\partial \omega} & \frac{\partial v}{\partial \theta} \end{pmatrix} = \begin{pmatrix} \cos \theta & -\omega \sin \theta \\ \sin \theta & \omega \cos \theta \end{pmatrix}$

$\Rightarrow$  Concept of backprojection!



$$\text{Fourier Slice Theorem: } \hat{P}(\omega, \theta) = \int_0^{2\pi} \hat{P}(\omega, \theta) e^{j2\pi(\omega \cos \theta + y \sin \theta)} d\omega$$

$$\hat{P}(\omega, \theta + \pi) = \hat{P}(-\omega, \theta)$$

$$\mu(x, y) = \int d\theta \int_{-\infty}^{\infty} \hat{P}(\omega, \theta) |\omega| e^{j2\pi\omega t} d\omega$$

Symmetry properties:

Image function:

## Reconstruction using backprojection (only)

- If no a priori information is known, the intensity of the object is assumed to be uniform along the beam path.
- The projection intensity is evenly distributed among all pixels along the ray path



Backprojection of a point ...

## Image reconstruction

$f(x, y) = \int_0^{\pi} d\theta \int_{-\infty}^{\infty} P(\theta, \omega) |\omega| e^{j2\pi\omega x} d\omega$

with filtering



0 projections



1 projection



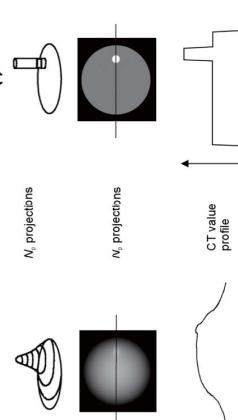
3 projections



$N_p$  projections



CT value profile



## Filtered backprojection

- Image characteristic can be influenced by the choice of a convolution kernel, whereby increasing spatial resolution or edge enhancement also means increasing image noise!

original profile

convolution kernel

standard

smoothing

edge enhancing

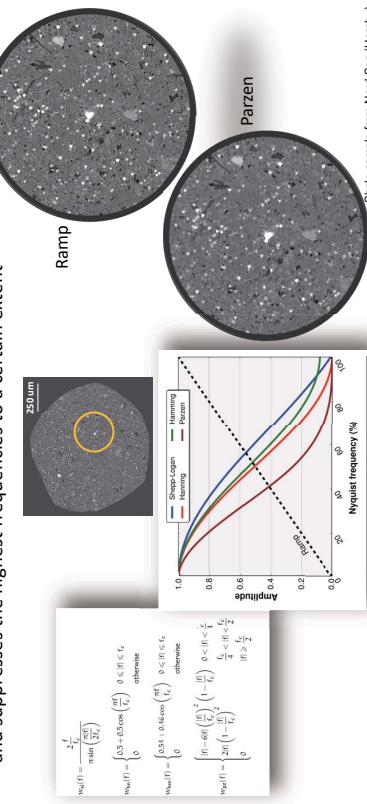
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=

=

## Filtered backprojection: a few hints

- Due to the high-pass nature of the ramp filter, the filtering step enhances the noise affecting the projections. As a matter of fact, the "pure" ramp filter should be employed only with almost noiseless data.
- In general, the ramp filter is multiplied with a window, that considers low frequencies and suppresses the highest frequencies to a certain extent



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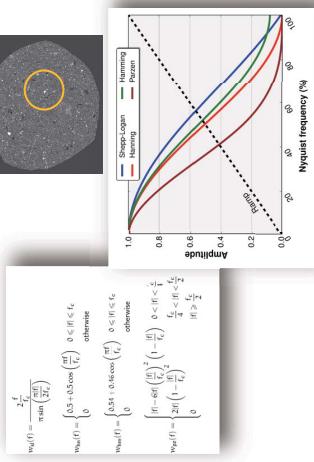
## FBP at work: demonstration



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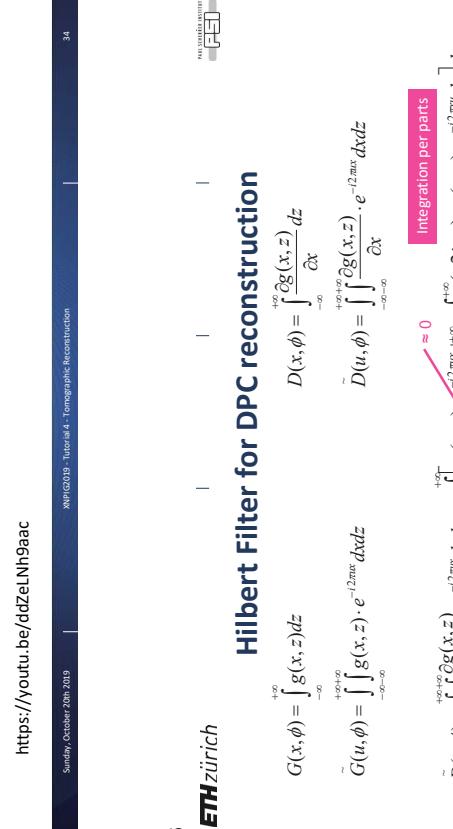
## Optimal sampling for FBP



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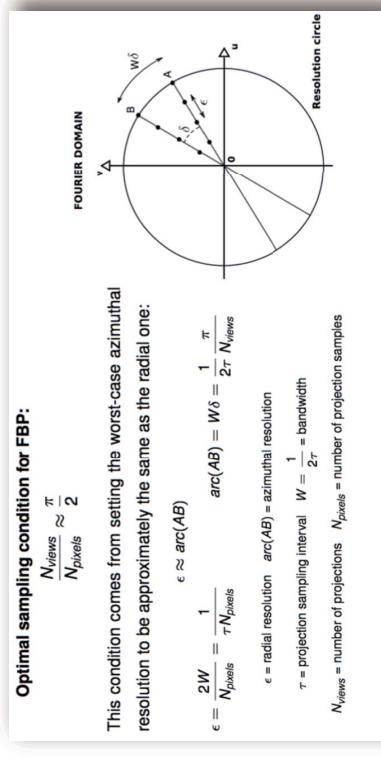
## Hilbert Filter for DPC reconstruction



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## Refractive tomography



This condition comes from setting the worst-case azimuthal resolution to be approximately the same as the radial one:

$$\epsilon = \frac{2W}{N_{\text{pixels}}} = \frac{1}{\tau N_{\text{pixels}}} \quad \text{arc}(AB) = W\delta = \frac{1}{2\pi} \frac{\pi}{N_{\text{views}}}$$

$\epsilon$  = radial resolution    $\text{arc}(AB)$  = azimuthal resolution

$\tau$  = projection sampling interval    $W = \frac{1}{2\pi}$  = bandwidth

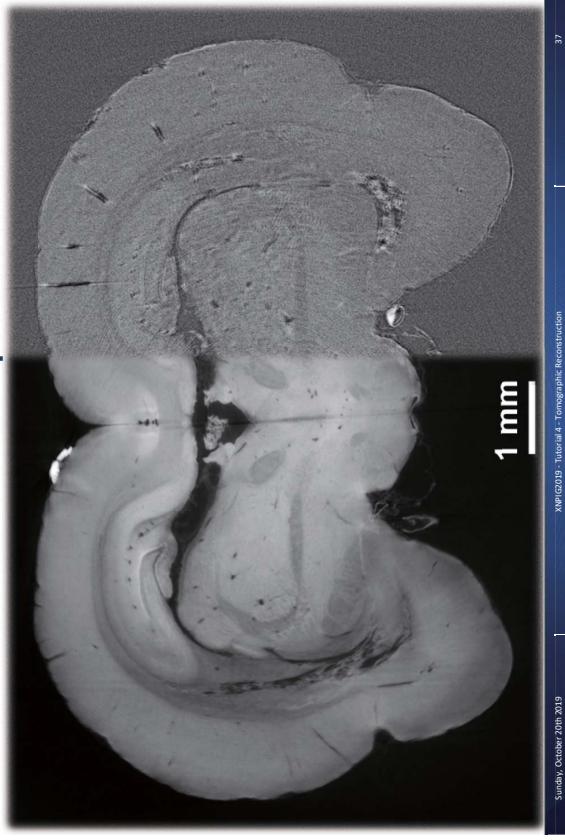
$N_{\text{views}}$  = number of projections    $N_{\text{pixels}}$  = number of projection samples

$$\delta(x, y) = \int_0^{\pi} d\theta \int_{-\infty}^{\infty} \tilde{D}(\omega, \theta) \frac{1}{2\pi} \frac{|\omega|}{\omega} e^{i2\pi \omega \theta} d\omega$$

Refraction of a beam transmitted through a phase object is directly proportional to the local gradient of the phase of the wave front!

Pfeiffer et al., PRJ 2007  
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## Phase vs absorption CT



## TAKE HOME MESSAGE - Algebraic Methods

Pro: Simple and fast

- Req: Need large number of projections  
(same order as detector pixels)
- Cons: Cannot include a-priori information  
(not suitable for under-sampled datasets)

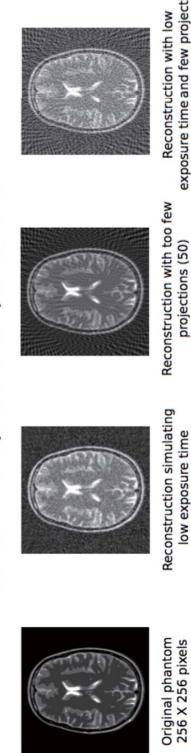
## Limitations of FBP: underconstrained tomograms

In many tomographic applications the following constraints are encountered:

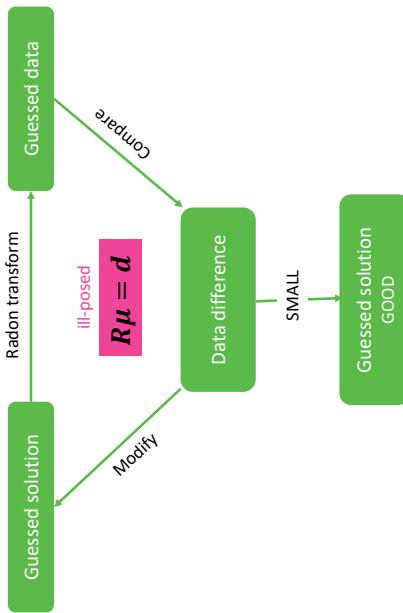
- short acquisition times for fast evolving samples
- dose limit tolerated by the sample
- projections that cannot be acquired homogeneously in  $[0, 180]$



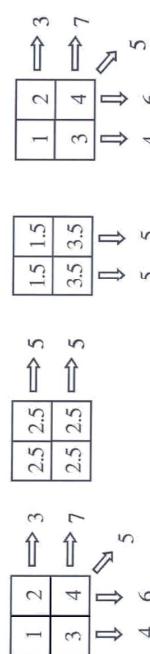
These circumstances lead to **underconstrained tomograms** that cannot be accurately reconstructed by means of FBP



## Iterative algorithms



## Iterative algorithms: Algebraic Reconstruction Technique (ART)



- Consider a four-block object and assign a specific attenuation value to each block (projection measurements are given).
- Assume, "a priori", an homogenous object. As initial estimate use the average of the projection samples (horizontal and vertical) which is  $10/4 = 2.5$ .
- Calculate the line integrals of our estimated distribution along the paths used for the original projection measurement. This gives a sum of 5 along all directions.
- "Fix the rows": Compare the calculated projections against the measured values of 3 and 7: the top row is overestimated by 2 (5-3) and the bottom row is underestimated by 2 (5-7). Since, again, we have no "a priori" knowledge of the object, we assume again that the difference between the measured and calculated projections needs to be split evenly among all pixels along each ray path. Therefore we decrease the value of each block in the top row by 1 and increase the bottom row by 1.
- "Fix the columns": The calculated projections in the horizontal direction are now consistent with the measure projections. We repeat the same process for projections in the vertical directions and reach the conclusion that each element in the first column must be decreased by 0.5 and each element in the second column must be increased by 0.5.
- The calculated projections in all directions are now consistent with the measured projections (including the diagonal direction) and the reconstruction process stops.

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## Iterative algorithms (algebraic)

ill-posed

$$R\mu = d$$

Optimization problem

$$\text{Cost function} \quad \underset{\mu}{\operatorname{argmin}} f(\mu, d) + g(\mu)$$

Regularization term  
Fidelity term

- The fidelity term serves to enforce the consistency between the synthesized forward projections and the measured raw data projections throughout the iterative process.

- If one were to perform iterative reconstruction with just the data fidelity term alone, the iteration might not converge to a low-noise solution. Therefore, the regularization term is employed, usually to reduce noise while preserving spatial resolution. This is accomplished by penalizing large differences in neighboring voxels. The mathematical approach used for regularization can vary significantly.

Optimization problem

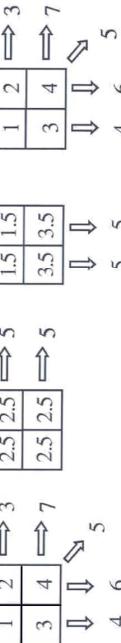
$$\underset{\mu}{\operatorname{argmin}} f(\mu, d) + g(\mu)$$

Optimization problem  
 $\underset{\mu}{\operatorname{argmin}} f(\mu, d) + g(\mu)$

$N$  – expected photon counts  
 $i$  – each pixel in each view

## Iterative algorithms

For DPC...  
 $f(\mu, d) = \frac{1}{2} \left\| R \frac{\partial \delta}{\partial \mu} - d \right\|_2^2$



- Algebraic methods (ART,...)
- $f(\mu, d) = \frac{1}{2} \|R\mu - d\|_2^2$
- $g(\mu) = \lambda \|\mu\|_2^2$
- Tikhonov small norm
- Lasso for sparse data
- Total Variation (TV) piecewise constant, edge preserving...

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## Iterative algorithms - statistical

ill-posed

$$\bar{N}_i = N_0^i \cdot e^{-[R\mu]_i}$$

Optimization problem

$$\text{Cost function} \quad \underset{\mu}{\operatorname{argmin}} f(\mu, d) + g(\mu)$$

Regularization term  
Fidelity term

- The fidelity term serves to enforce the consistency between the synthesized forward projections and the measured raw data projections throughout the iterative process.

- If one were to perform iterative reconstruction with just the data fidelity term alone, the iteration might not converge to a low-noise solution. Therefore, the regularization term is employed, usually to reduce noise while preserving spatial resolution. This is accomplished by penalizing large differences in neighboring voxels. The mathematical approach used for regularization can vary significantly.

Optimization problem

$$\underset{\mu}{\operatorname{argmin}} f(\mu, d) + g(\mu)$$

Optimization problem  
 $\underset{\mu}{\operatorname{argmin}} f(\mu, d) + g(\mu)$

$N$  – expected photon counts  
 $i$  – each pixel in each view

Optimization problem  
 $\underset{\mu}{\operatorname{argmin}} f(\mu, d) + g(\mu)$

Cost function  
 $f(\mu, d) = \frac{1}{2} \|R\mu - d\|_2^2$

$g(\mu) = \lambda \|\mu\|_1$

$g(\mu) = \lambda \|\nabla \mu\|_1$

Tikhonov

small norm

Lasso

for sparse data

Total Variation (TV)

piecewise constant, edge preserving...

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Sunday, October 20th 2019 XN@2019 - Tutorial 4 - Tomographic Reconstruction

Sunday, October 20th 2019 XN@2019 - Tutorial 4 - Tomographic Reconstruction

Sunday, October 20th 2019 XN@2019 - Tutorial 4 - Tomographic Reconstruction

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Sunday, October 20th 2019 XN@2019 - Tutorial 4 - Tomographic Reconstruction

## TAKE HOME MESSAGE - Iterative Methods

- Pros:

  - Can include *a-priori* information
  - Flexible – can model almost anything
  - Suitable for under-sampled datasets
  - ...

- Cons:

  - Computational intensive
  - Highly dataset specific
  - ...
  - Needs to tune (lots of) parameters
  - ...

## References – Computed tomography

- A. C. Kak, M. Slaney, Principle of Computerized Tomographic Imaging”, SIAM Classics in Applied Mathematics 33, New York, 2001, ISBN 0-89871-494-X
- F. Natterer, “The Mathematics of Computerized Tomography”, SIAM Classics in Applied Mathematics 32, Philadelphia 2001, ISBN 0-89871-493-1
- W. A. Kalender, “Computed Tomography – Fundamentals, System Technology, Image Quality, Applications”, 2nd revised edition, 2005, Publicis Corporate Publishing, ISBN 3-89578-216-5
- J. Hsieh, Computed Tomography: Principles, Design, Artifacts and Recent Advances, SPIE Press Monograph, ISBN 0-8194-4425-1



## **Tutorial 5**

**(16:40 – 17:10)**

**Fabrication technology of gratings**

**Christian David**

*Paul Scherrer Institut,*

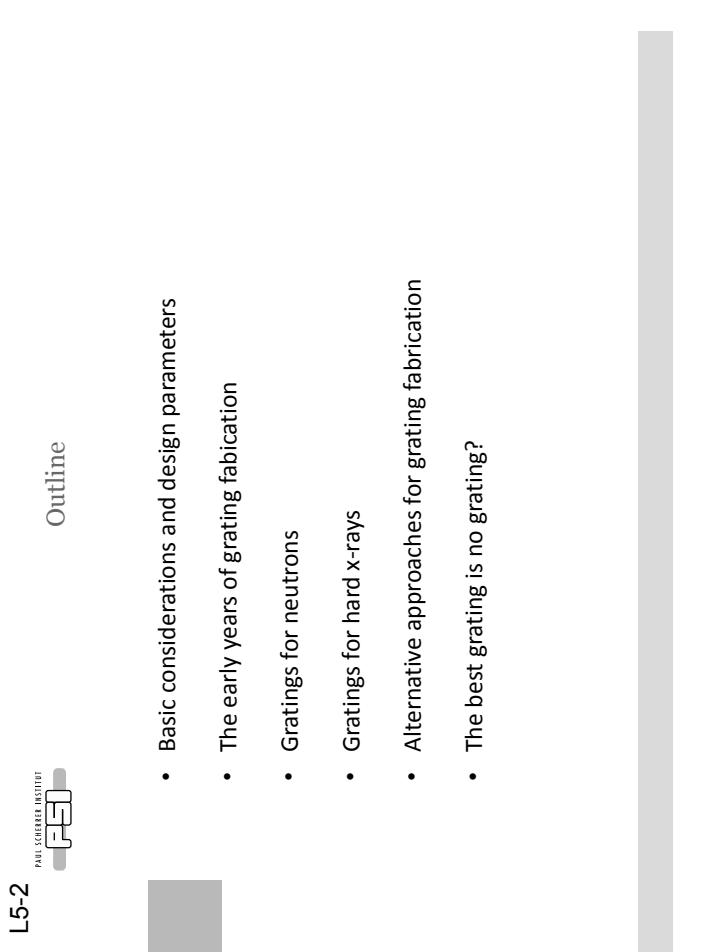
*Switzerland*



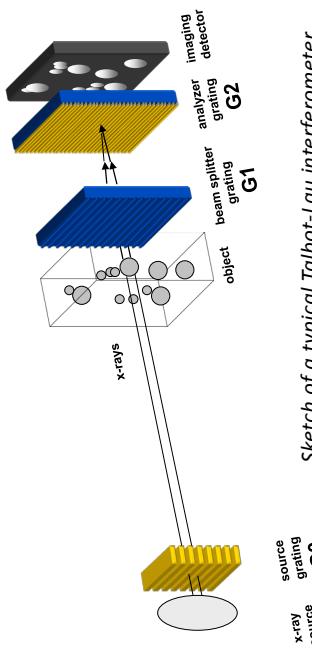
Christian David, Paul Scherrer Institut, Switzerland

## Fabrication technology of gratings

- Basic considerations and design parameters
  - The early years of grating fabrication
  - Gratings for neutrons
  - Gratings for hard x-rays
  - Alternative approaches for grating fabrication
  - The best grating is no grating?



Basic considerations and design parameters



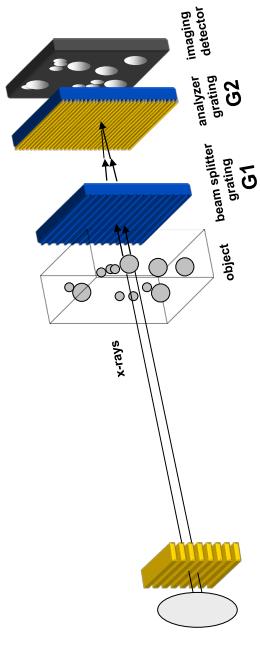
Sketch of a typical Talbot-Lau interferometer

**Purpose of the gratings:** detect small changes in the propagation of x-rays by:

- refraction due to differences in phase shift => **phase contrast imaging**
- small-angle scattering => **dark-field imaging**

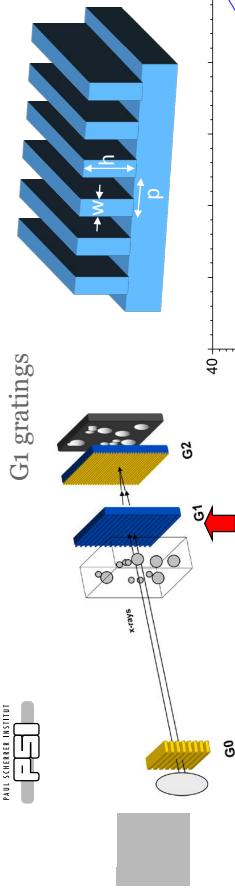
Angular sensitivity depends on grating periods => **micron pitches**

Basic considerations and design parameters



Sketch of a typical Talbot-Lau interferometer

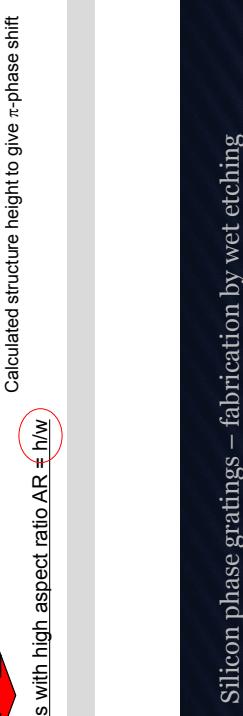
Grating	Interaction with x-rays	typ. materials	typ. pitch	size
G0	high absorption	Au, Ir, Pb, W, ...	p0: many $\mu\text{m}$	small
G1	$\pi$ -phase shifting (or $\pi/2$ )	Si, Ni	p1: few $\mu\text{m}$	field of view (FOV)
G2	high absorption	Au, Ir, Pb, W, ...	p2: few $\mu\text{m}$	larger than FOV



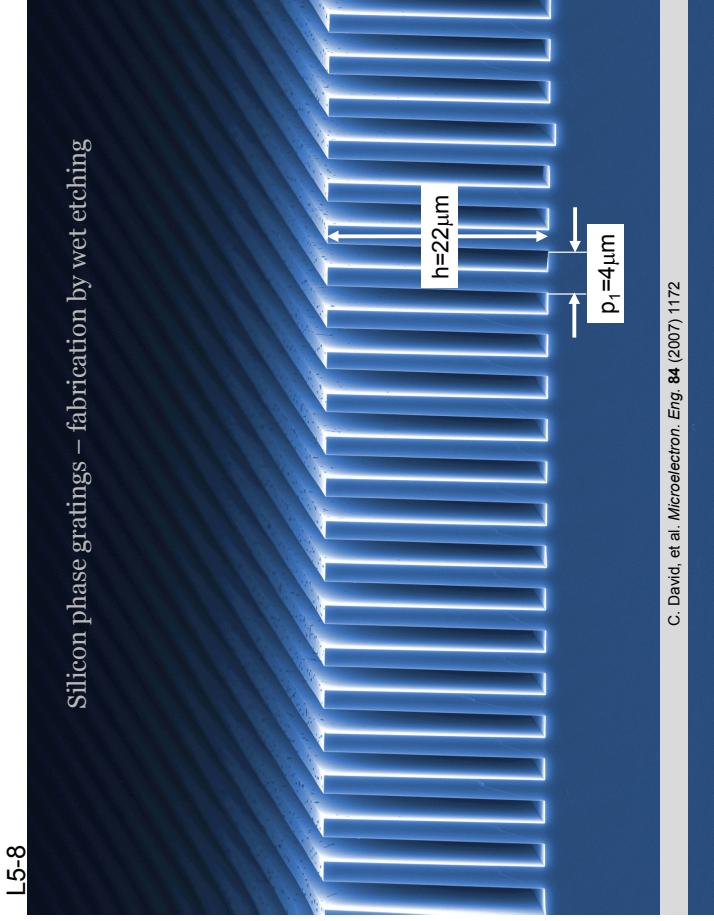
## Early years of grating fabrication (When photons were soft)

### Requirements:

- Size limits field of view
- Periods  $p$  of a few microns
- Low zero<sup>th</sup> order efficiency
- Low absorption
- Duty cycle DC =  $w/p = 0.5$
- Introduce phase shift of  $\pi$
- Grating lines with high aspect ratio  $AR = h/w$



Calculated structure height to give  $\pi$ -phase shift



C. David, et al. *Microelectron. Eng.* **84** (2007) 1172



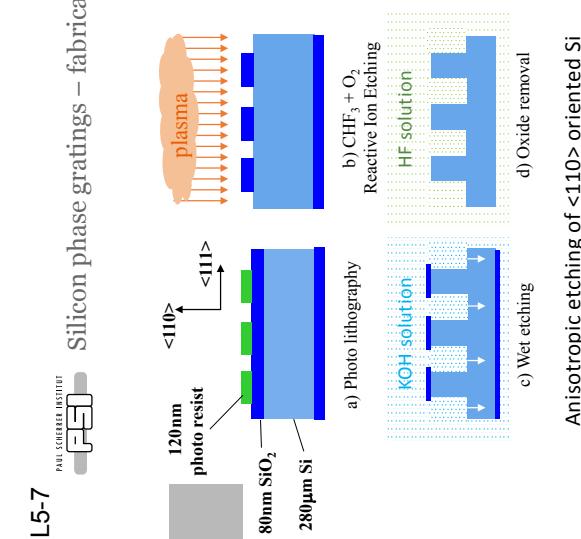
First silicon gratings for x-ray phase imaging,  $p = 1 \mu\text{m}$ ,  $h = 12 \mu\text{m}$

First x-ray phase images of latex spheres,  $E = 12.4 \text{ keV}$



First silicon gratings for x-ray phase imaging,  $p = 1 \mu\text{m}$ ,  $h = 12 \mu\text{m}$

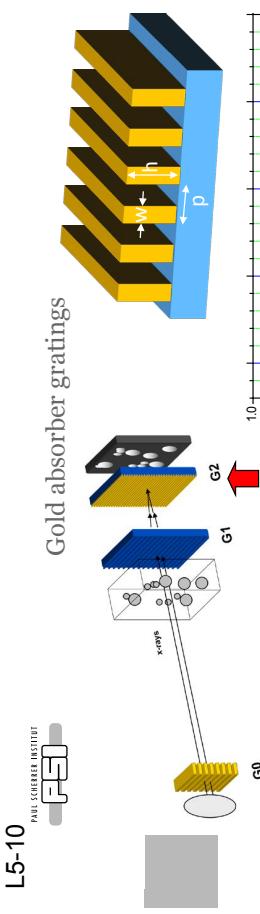
First x-ray phase images of latex spheres,  $E = 12.4 \text{ keV}$



Anisotropic etching of <110> oriented Si gives vertical side walls with <111> orientation

C. David, B. Nohammer, H.H. Solak, E. Ziegler, *Applied Physics Letters* **81** (2002) 3287

**Silicon phase gratings – fabrication by wet etching**



**Requirements:**

- Size limits field of view
- Periods 2x smaller than phase grating
- Duty cycle typ. DC = 0.5
- High absorption required

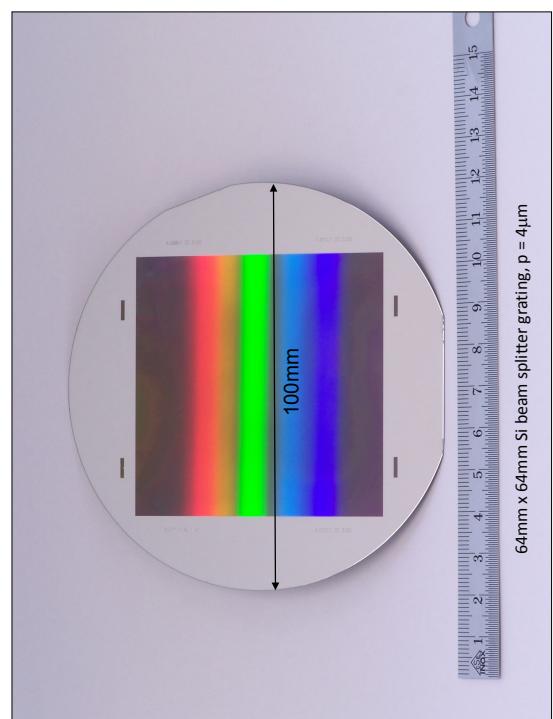
• Grating lines with very high aspect ratio AR =  $h/W$

C. David, et al. *Microelectron. Eng.* **84** (2007) 1172

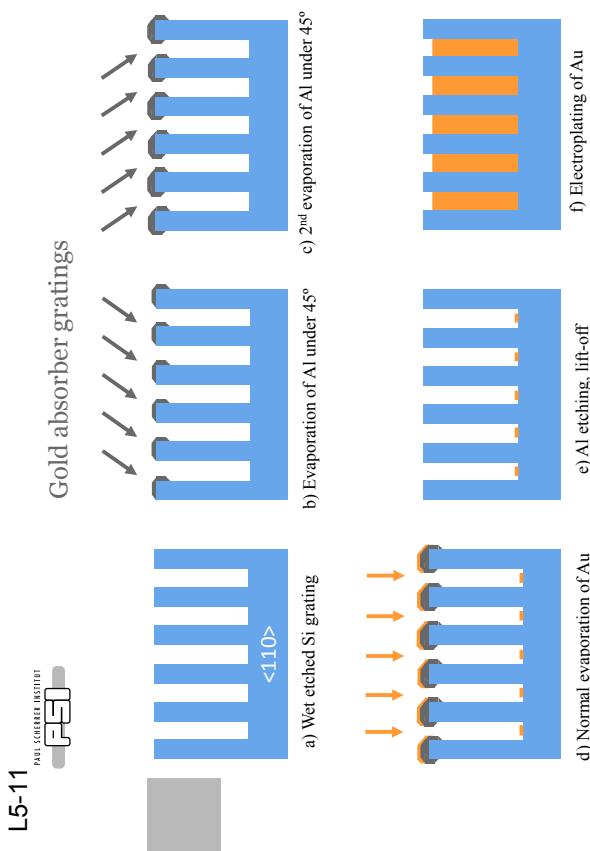


C. David, et al. *Microelectron. Eng.* **84** (2007) 1172

C. David, et al. *Microelectron. Eng.* **84** (2007) 1172

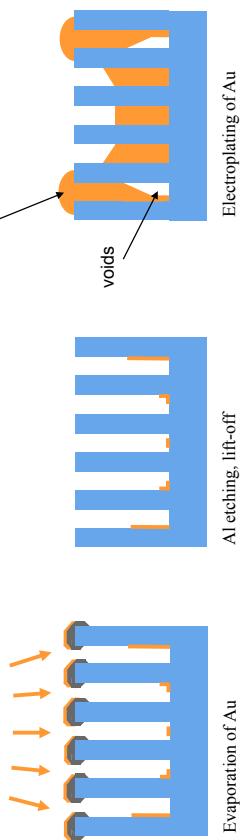


C. David, et al. *Microelectron. Eng.* **84** (2007) 1172



**Problem:**  
Aspect ratio (AR) is limited by precision  
of Au plating base deposition

$\Rightarrow$  limited by grating size to AR  $\sim 10$



#### Advantages:

- Frequency doubling
- Higher aspect ratios possible

- Disadvantages:**
- Control of DC of Si grating and plated thickness is crucial



L5-15  
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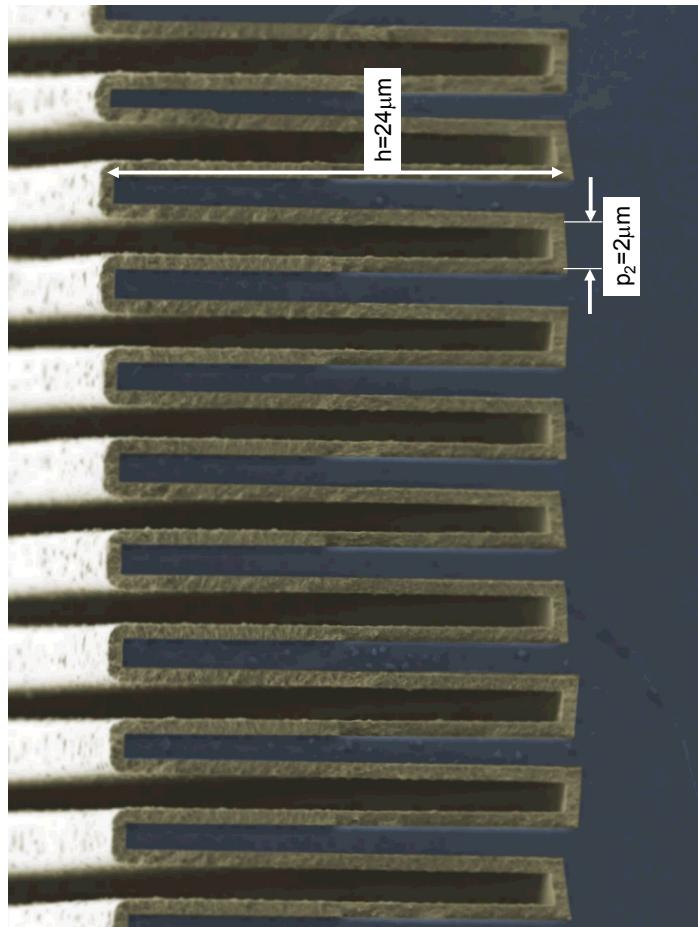
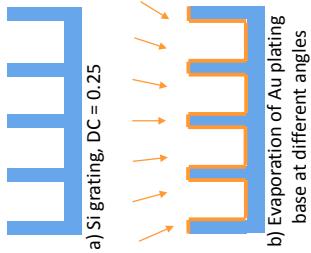
Gold absorber gratings – line doubling

#### Advantages:

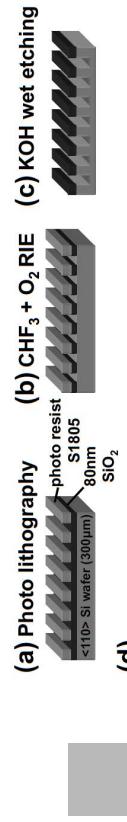
- Frequency doubling
- Higher aspect ratios possible

#### Disadvantages:

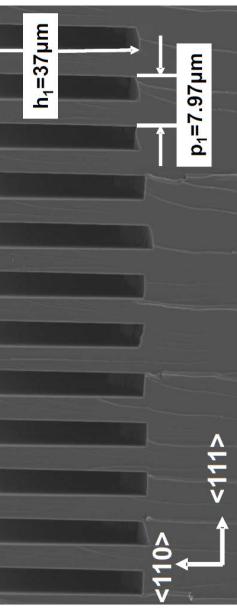
- Control of DC of Si grating and plated thickness is crucial



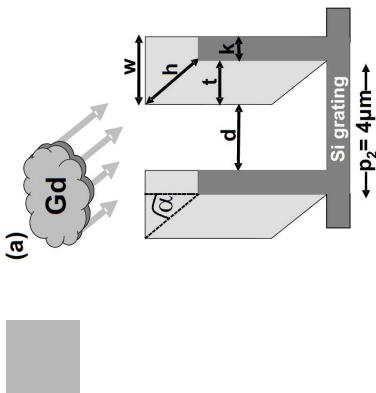
Gratings for neutrons



## Gratings for neutrons (easier than we thought)

At  $\lambda = 4.1 \text{ \AA}$ , the neutron  $\pi$ -shift length for Si is  $37 \mu\text{m}$ C. Grünzweig, F. Pfeiffer, O. Bunk, T. Donath, G. Kühne, G. Frei, M. Dierolf, C. David, *Rev. Sci. Instrum.* **79** (2008), 053703

Gratings for neutrons

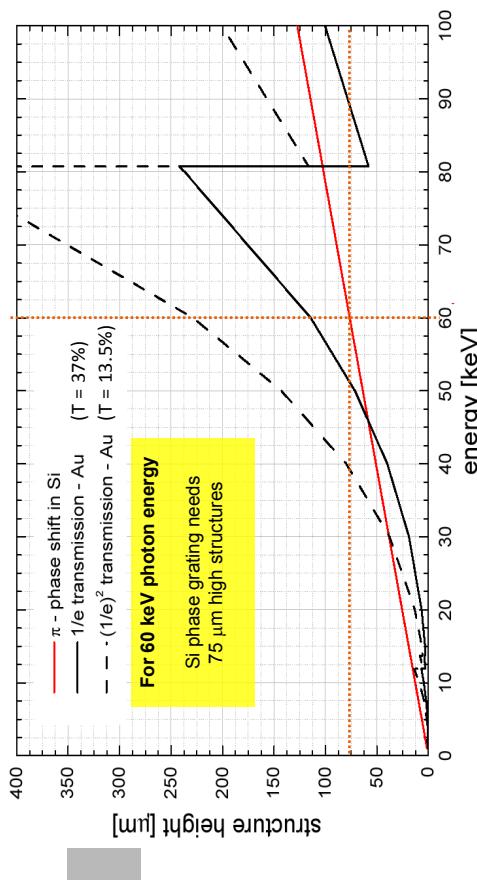
At  $\lambda = 4.1 \text{ \AA}$ , the neutron  $1/e$  length for Gd is  $3 \mu\text{m}$ 

For progress on neutron gratings see XNPIG session VII, Tuesday afternoon

C. Grünzweig, F. Pfeiffer, O. Bunk, T. Donath, G. Kühne, G. Frei, M. Dierolf, C. David, *Rev. Sci. Instrum.* **79** (2008) 053703

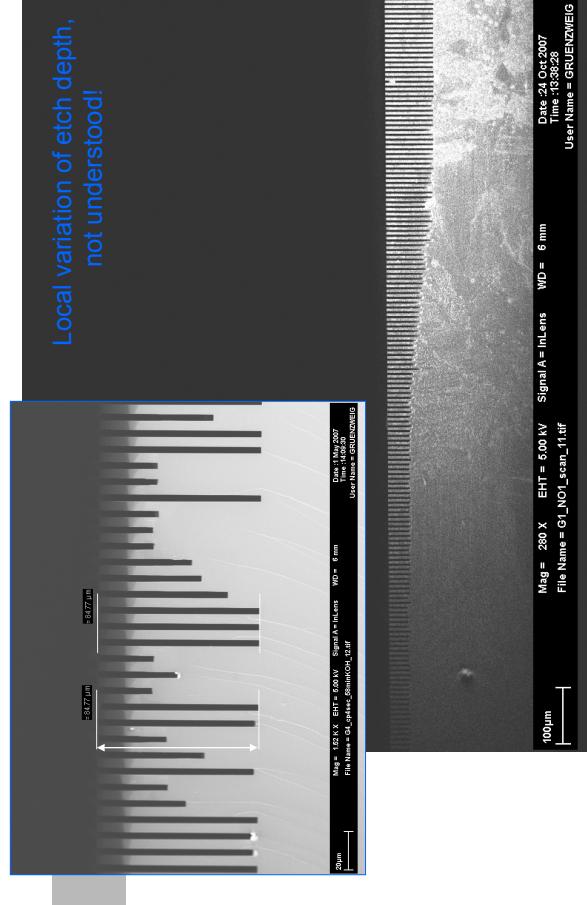
Gratings for hard x-rays  
(when things become much, much more difficult)

High photon energies require high structures



Structure heights for **phase gratings** and absorber gratings

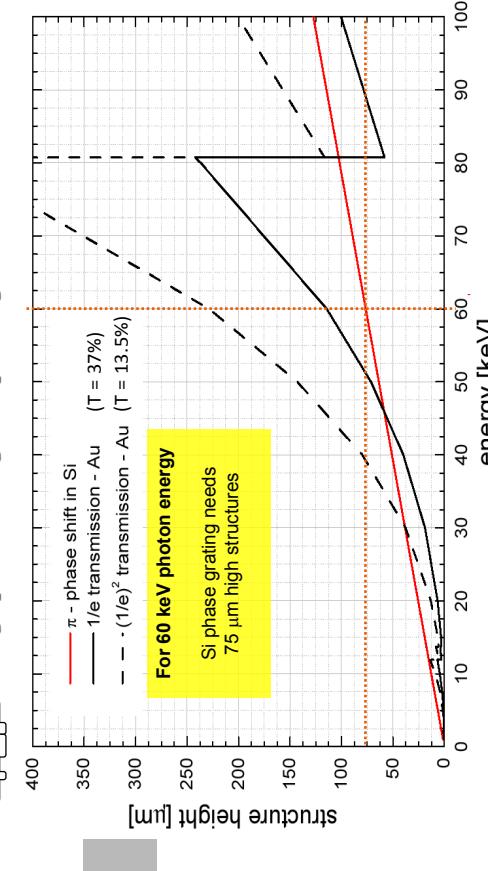
Courtesy F. Pfeiffer



Local variation of etch depth,  
not understood!

For 60 keV photon energy

Si phase grating needs  
75 μm high structures

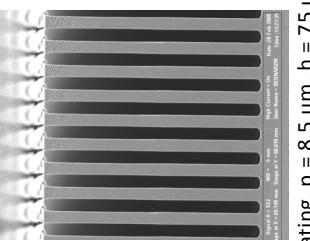


Structure heights for **phase gratings** and absorber gratings

Courtesy K. Jefimovs

Bosch plasma etching process

- 2 step plasma etching process
- Etching: SF<sub>6</sub>
- Passivation: C<sub>4</sub>F<sub>8</sub>
- variables: etching/passivation times, gas flows, temperature, pressure, RF/ICP power



Silicon phase grating,  $p = 8.5 \mu\text{m}$ ,  $h = 75 \mu\text{m}$ , AR = 17.5

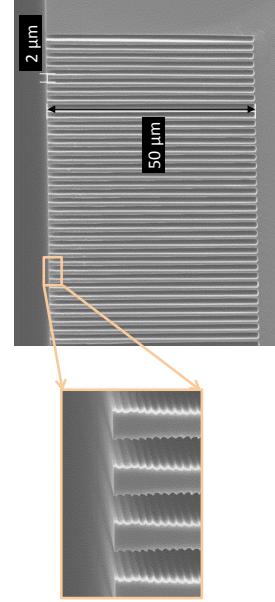
(by M. Bednarzik)

Courtesy of K. Jefimovs

T. Donath, Review of Scientific Instruments **80** (2009) p. 053701-4

Bosch plasma etching process

- 2 step plasma etching process
- Etching: SF<sub>6</sub>
- Passivation: C<sub>4</sub>F<sub>8</sub>
- variables: etching/passivation times, gas flows, temperature, pressure, RF/ICP power

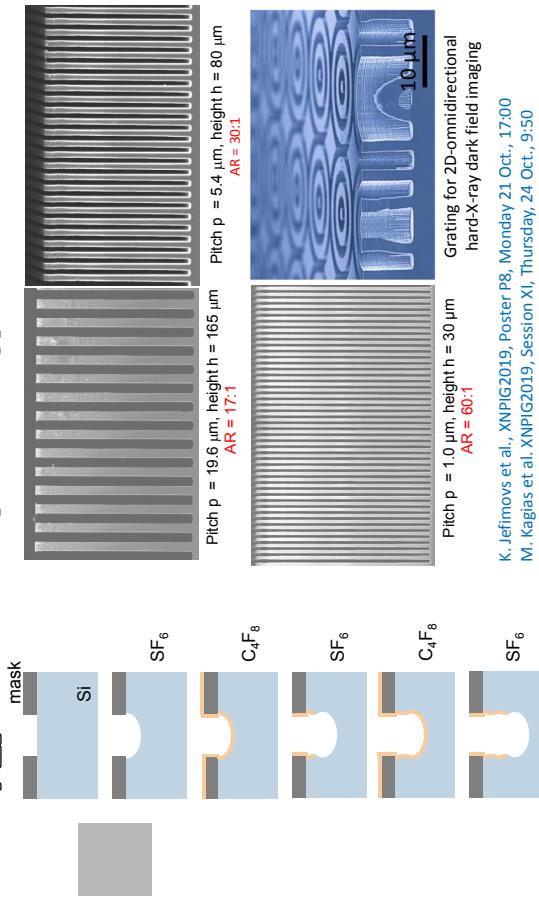


Silicon phase grating,  
 $p = 2 \mu\text{m}$ ,  $h = 50 \mu\text{m}$ , AR = 50  
(recent results by K. Jefimovs)

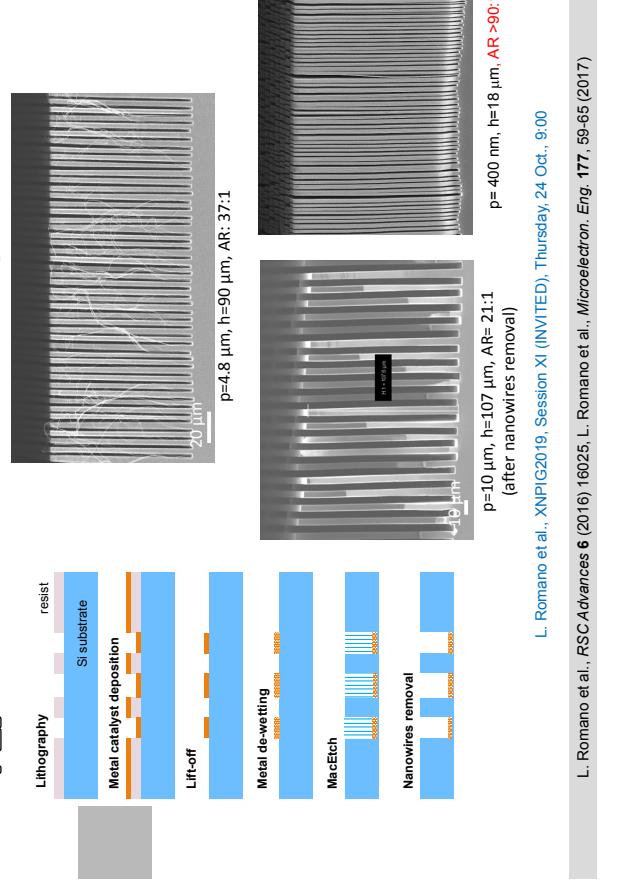
Courtesy of K. Jefimovs

K. Jefimovs et al., Proc. SPIE **10146**, 10146L (2017), M. Kaggas et al., Phys. Rev. Lett. **116**, 093902 (2016)

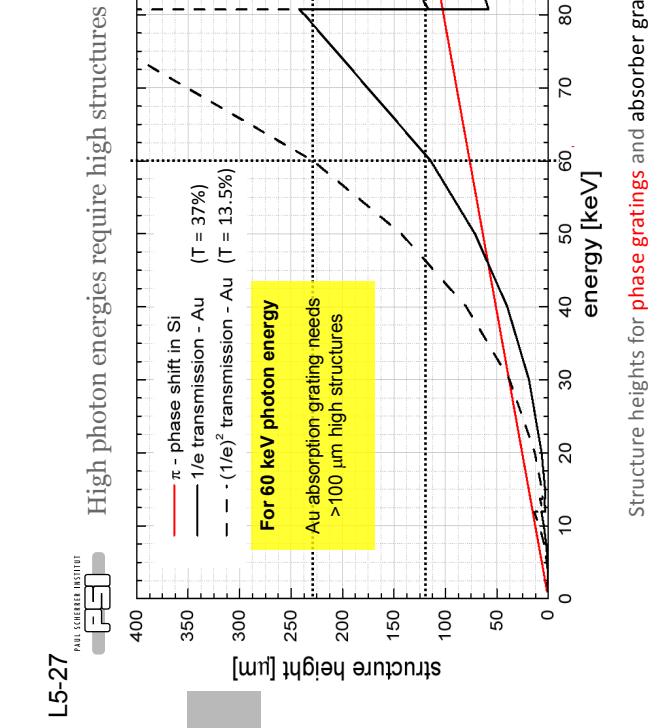
L5-25  
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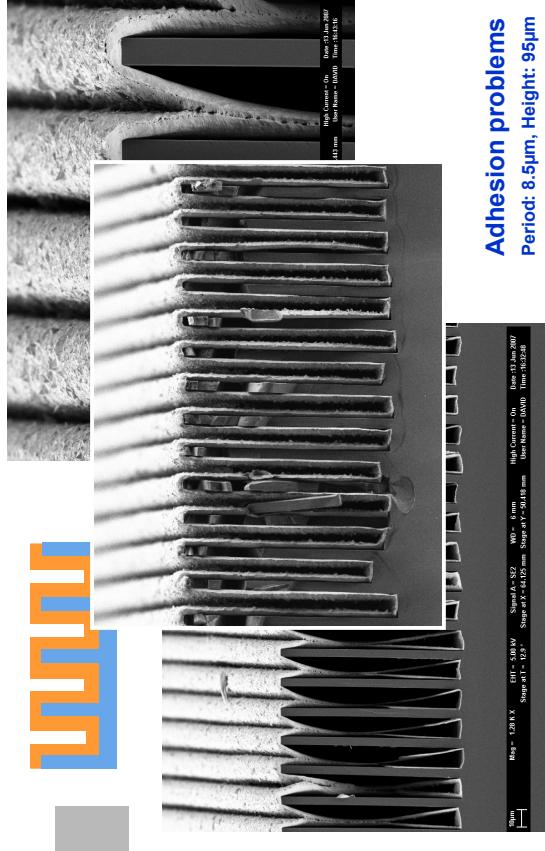
L5-26  
PAUL SCHERER INSTITUT



L5-27  
PAUL SCHERER INSTITUT



L5-28  
PAUL SCHERER INSTITUT



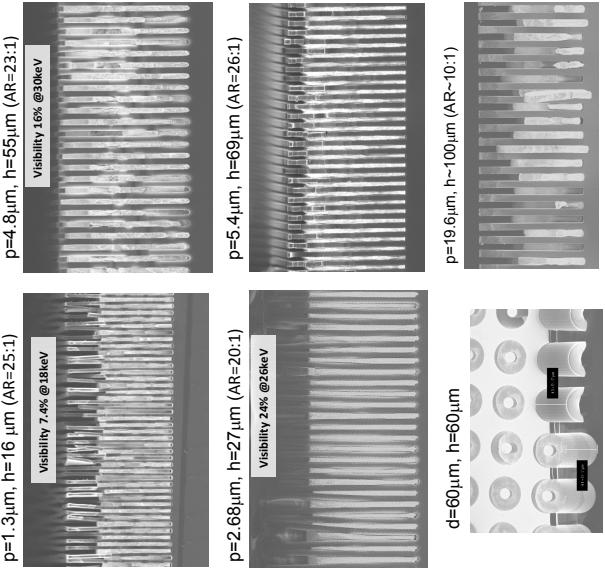
Structure heights for **phase gratings** and absorber gratings

Adhesion problems  
Period: 8.5 μm, Height: 95 μm

T. Donath, *Review of Scientific Instruments* **80** (2009) p. 053701-4

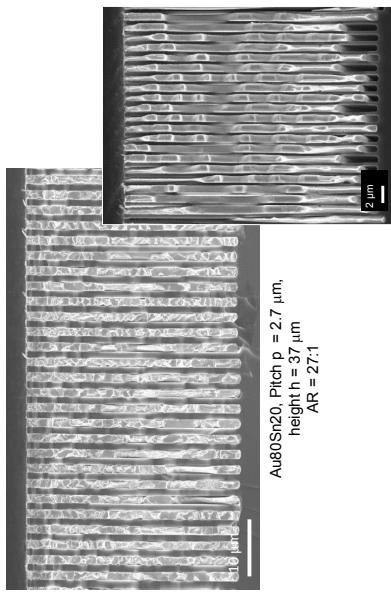
Courtesy F. Pfeiffer

## Seedless Au electropolating



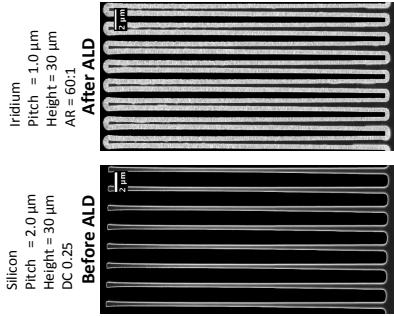
D. Noda, et al., AIP Conference Proceedings **1466**, 187 (2012)  
 K. Jefimovs et al., XNPiG2019, Poster P8,  
 Monday 21 Oct., 17:00  
 M. Kaggas et al., Mater. Sci. Semicond.  
 Process. **92** (2019) 73-79

## Metal casting



L. Romano et al., Microelectron. Eng. **176** (2017) 6-10; L. Romano et al., J. Vac. Sci. Technol. B **35** (2017) 06G302

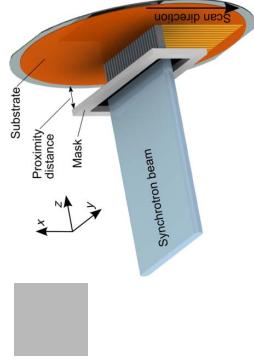
## Fabrication of gratings by Silicon RIE and Iridium ALD



J. Vila-Comamala et al., XNPiG2019, Session X, Wednesday 23 Oct., 11:40  
 M. Kaggas et al., XNPiG2019, Session XI, Thursday, 24 Oct., 9:50

J. Vila-Comamala et al., Microelectron. Eng. **192** (2018) 19-24

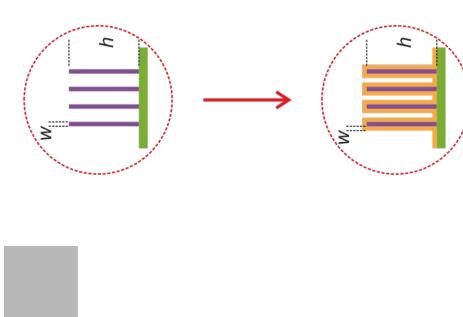
## The LIGA technique



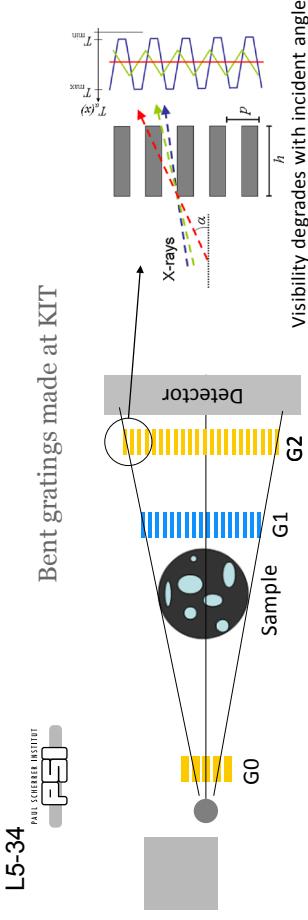
step 3 Au electroforming  
 step 2 wet development  
 step 1 X-ray exposure  
 Schematic view of the process steps of the LIGA process.

## L5-33

Fabrication of atomic layer deposited Iridium to coat the silicon structures.



J. Mohr, et al., AIP Conference Proceedings **1466** (2012) 41



LIGA gratings are commercially available  
from microworks GmbH  
see oral presentation by J. Schulz, Thursday 9:30h

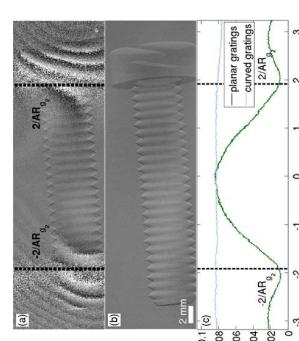
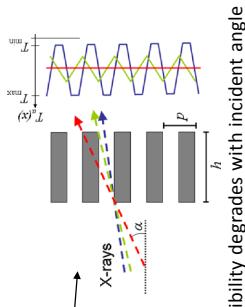
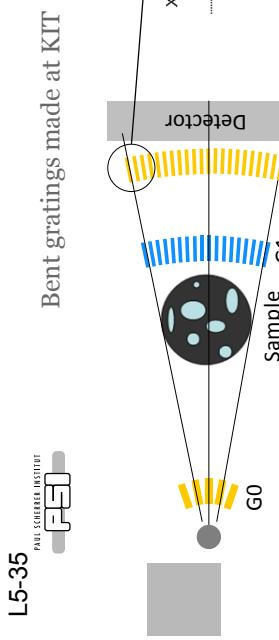


Karlsruhe Institute of Technology



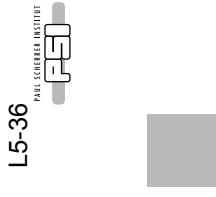
Made by LIGA technology at IMT, Karlsruhe Institute of Technology

E. Reznikova, J. Mohr, M. Börner et al., Microsyst. Technol. **14** (2008) 1683



Gratings made by KIT on flexible titanium substrates.  
Left: GO grating with 30 mm radius. Left: G2 grating

T. Thüring, P. Modregger, T. Grund, J. Kenner, C. David, and M. Stampanoni, Appl. Phys. Lett. **99**, 041111 (2011)



T. Thüring, P. Modregger, T. Grund, J. Kenner, C. David, and M. Stampanoni, Appl. Phys. Lett. **99**, 041111 (2011)

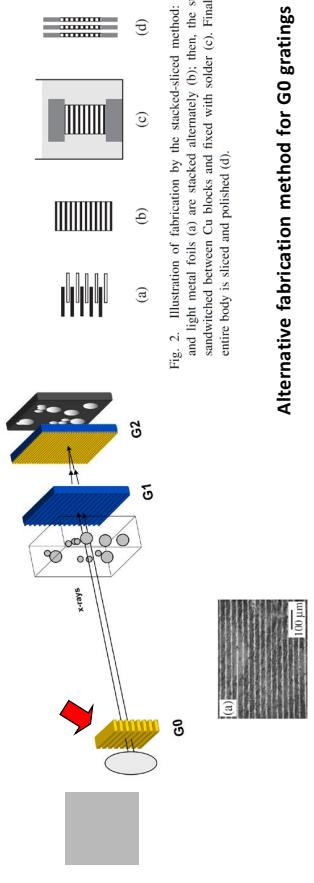


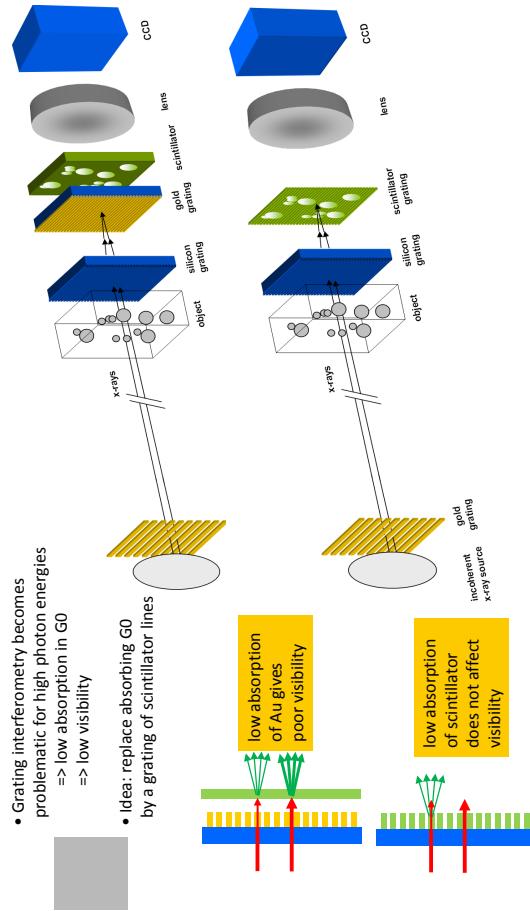
Fig. 2. Illustration of fabrication by the stacked-sliced method: Heavy and light metal foils (a) are stacked alternately (b); then, the stack is sandwiched between Cu blocks and fixed with solder (c). Finally, the entire body is sliced and polished (d).

#### Alternative fabrication method for G0 gratings

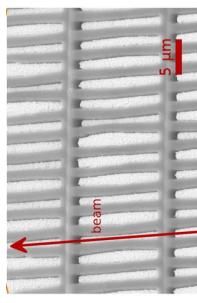
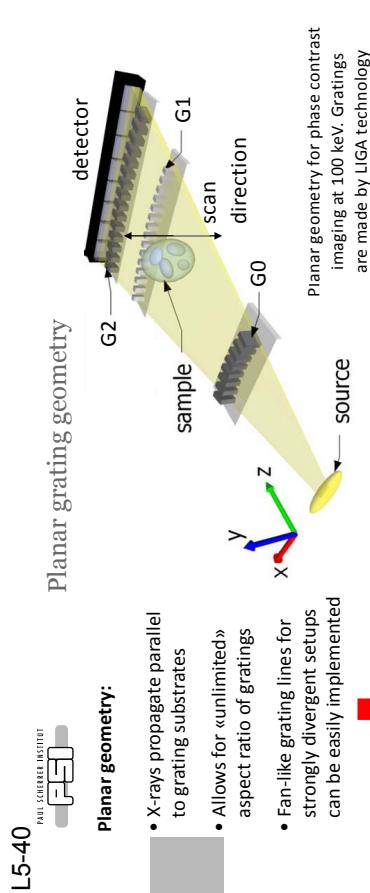
- Stacking of absorbing and transparent metal foils (Ta, 20 μm thick and Al, 10 μm thick)
- Pressing, fixation, cutting and polishing
- Results in G0 gratings with 30 μm pitch and 600 μm thickness

Fig. 3. (a) Optical microscopy image of the surface of the multiple slit in which the dark lines denote Ta and white lines denote Al. (b) X-ray projection image of the multiple slit measured using a micro-focus W source. (c) Normalized intensity profile on the white line in (b).

K. Wan, Y. Takeda, W. Yashiro and A. Momose, *Jpn. J. Appl. Phys.* **47** (2008), 7412

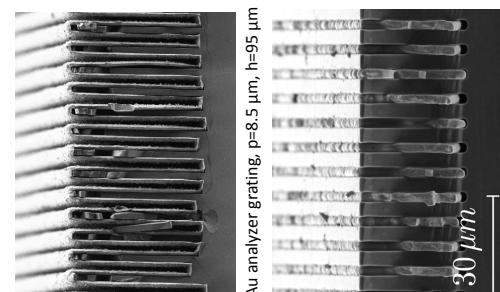


S. Rutishauser, I. Zanette, T. Donath, A. Sahrlholm, J. Linros, and C. David, *Appl. Phys. Lett.* **98**, 17 [2011], 171107

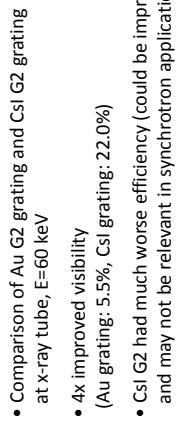


SEM image of grating (by Microworks GmbH).  
Height h=100 μm, pitch p2=2.8 μm.

T. Thuring, et al., *Scientific Reports* **4** (2014) 5198



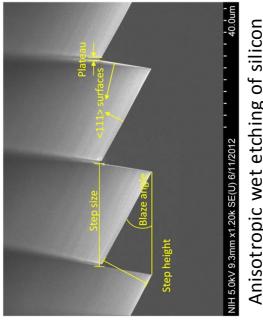
Au analyzer grating, p=8.5 μm, h=95 μm  
(made by Scint-X, Stockholm)



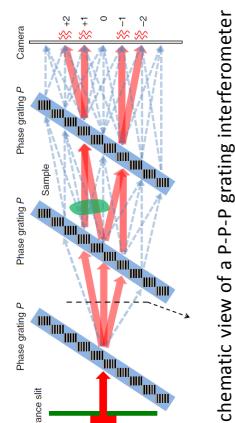
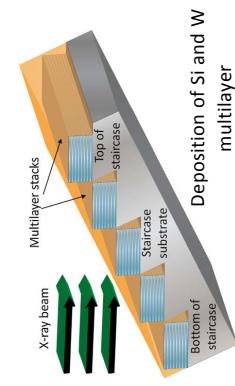
- Comparison of Au G2 grating and CsI G2 grating at x-ray tube, E=60 keV
- 4x improved visibility (Au grating: 5.5%, CsI grating: 22.0%)
- CsI G2 had much worse efficiency (could be improved, and may not be relevant in synchrotron applications)

S. Rutishauser, I. Zanette, T. Donath, A. Sahrlholm, J. Linros, and C. David, *Appl. Phys. Lett.* **98**, 17 [2011], 171107

## Gratings made by multilayer deposition



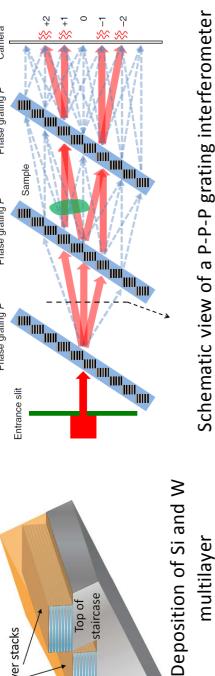
- Fabrication of gratings with very small pitches and very high aspect ratios
- Anisotropic etching of Si substrate to form «staircase»
- Deposition of Si/W multilayer with 200 nm pitch
- Extreme aspect ratios can be made ( $\Delta h > 200$ )
- Implementation of three identical gratings in a P-P-P configuration



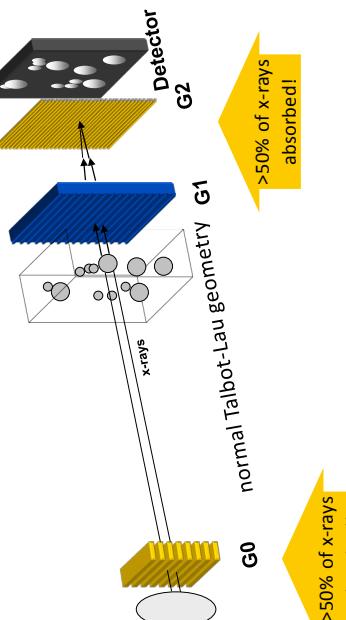
Schematic view of a P-P-P grating interferometer

Lynch, S. K. et al., J. Micromech. Microeng. 22 (2012), 105007. H. Wen, et al., Nature Comms. 3659 (2013)

## The best grating is no grating?



## The best grating is no grating?

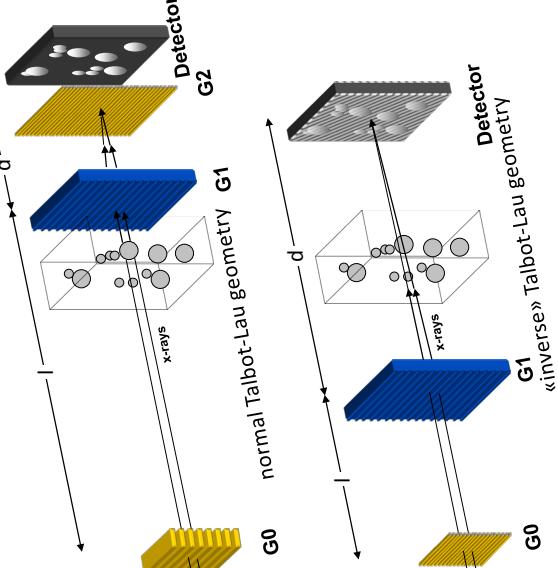


- >75% of photons are absorbed in G0 & G2

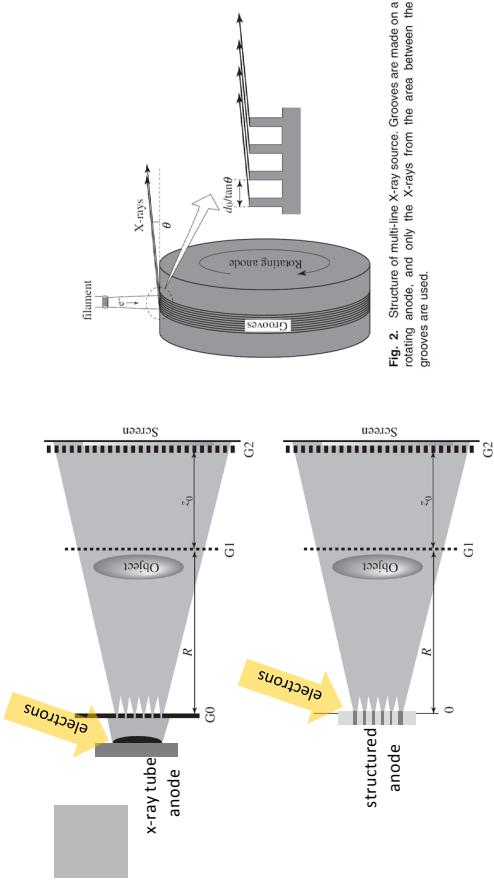
How can we get rid of them?

## «Inverse geometry»:

- $l \ll d$
- $p_2 \gg p_0$   
The grating with biggest area has biggest pitch
- Interference fringes become big enough to be resolved by detector
- $G_2$  is no longer required!



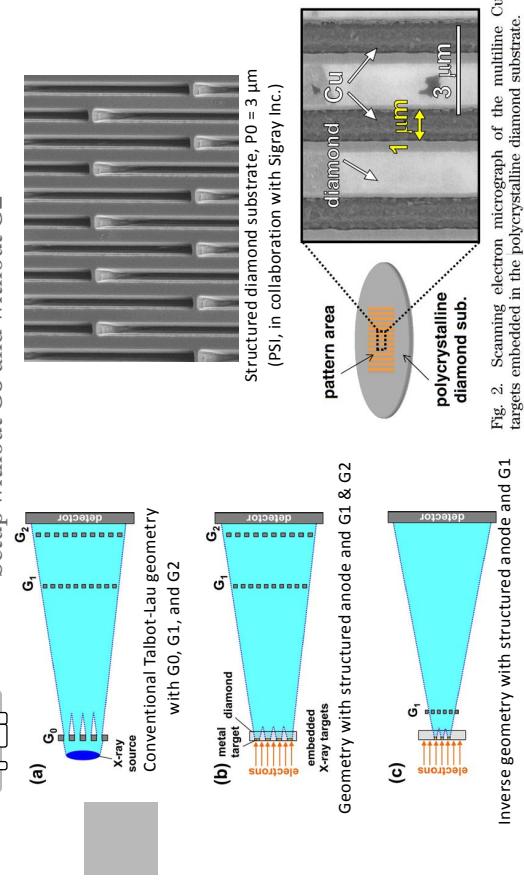
Setup without Go – structured anode of x-ray tube



For progress on structures sources see XNPiG session X, Wednesday morning

A. Momose, W. Yashiro, H. Kuwabara, and K. Kawabata, Jpn. J. Appl. Phys. **48** (2009) 076512

Setup without Go and with G2



For progress on structures sources see XNPiG session X, Wednesday morning

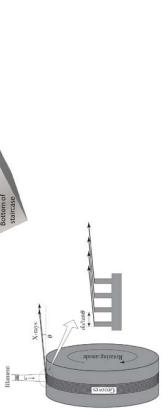
N. Morimoto, S. Fujino, K. Ohshima, J. Harada, T. Hosoi, H. Watanabe, and T. Shimura, Opt. Lett. **39**(15) 4297-4300 (2014)

### Summary and conclusion

- Gratings for x-ray phase contrast imaging require:
  - Small pitch for angular sensitivity
  - High contrast for x-rays

- Lithographic techniques have been developed based on wet-etching, dry etching, and x-ray lithography (LIGA).

- Gratings for hard x-rays become very challenging due to extreme aspect ratios.
- Alternative strategies are pursued.



- New developments towards making absorber gratings (G0, G2) obsolete.